

University of Saskatchewan IEEE Student Branch

ELECTRICAL ENGINEERING 3rd YEAR EXAM FILE

(Term 1)

2003 Edition

Includes:

EE 301

EE 323

EE 331

EE 351

EE 372

Prepared for you by the IEEE

Additional exams available on class web sites and at http://ieee.usask.ca

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EE301 Midterm

October 25, 2001

Welcome to the EE301 Midterm. This is an open book examination. You may refer to your textbook but not to any other material such as notes or other books. You may also

Each problem is worth 20 points; if subparts are weighted differently, the points for each are shown in parentheses. Show your work; credit will be given only if the steps leading to the answer are clearly shown. If a symmetry argument is used, it is sufficient to write "By symmetry we know that...". Partial credit will be given for partially correct answers.

You are to answer a total of five problems. Work the first three problems and any two of the last three.

None of the problems require intricate mathematical manipulations. Several integrals are given on the last page that you might or might not find useful. Cartesian coordinate triples are always (x, y, z).

Answer each of the first three problems.

Problem 1

At the point P given by the Cartesian coordinates (3, 4, 0) there exists two vectors:

$$\vec{A} = 2\vec{a}_x + 2\vec{a}_y + \vec{a}_z$$
 and $\vec{B} = -\vec{a}_x + 2\vec{a}_y + 2\vec{a}_z$.

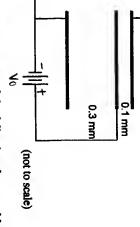
- a) Calculate $\vec{A} \cdot \vec{B}$.
- **b)** Calculate the angle between \vec{A} and \vec{B} .
- c) What is the point P in spherical coordinates?
- d) Convert vector \vec{A} to spherical coordinates.

Problem 2

A charge of 10 nC is placed at the origin. Charges of -5 nC are placed at the Cartesian coordinates (0, 0, 1) and (0, 0, -1) (all measurements in meters). Determine the electric field vector at the point (1, 0, 1) in Cartesian coordinates.

Problem 3

A parallel plate capacitor consists of three plates 10 cm on a side (see diagram). The gap from the center plate to the upper plate is 0.1 mm and the gap to the lower plate is 0.3 mm. The outer plates are connected together by a wire and form one terminal and the center plate forms the other terminal. A voltage is connected across the terminals such that the total charge on the inner plate is +1 nC. What are the charges on the other plates?



Answer any two of the following three problems.

Problem 4

A capacitor consists of two concentric metallic spherical shells of smaller radius r_1 and larger radius r_2 . The space between the shells is filled with an insulator with dielectric constant ε_R .

- a) (17) Determine a formula for the capacitance.
- b) (3) A charge of Q is placed on the inner shell and the outer shell is left uncharged. A wire is carefully inserted that shorts the inner shell to the outer shell. How does the charge Q redistribute between the two shells? That is how much charge flows to the outer shell and how much remains on the inner shell? Explain the reasoning behind your answer. (This part requires no calculations, only thinking).

Problem 5

Space is filled with a charge density η that varies with the distance from the z axis according to the formula (in cylindrical coordinates)

$$\eta = Ae^{-p}$$

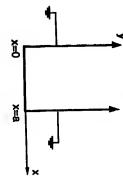
Note: the charge density is called η to avoid confusion with the radial coordinate ρ . Determine the electric field due to this space charge.

Problem 6

An open ended trough consists of three walls (see diagram). The walls at x = 0 and x = a are metallic and extend to infinity in the +y direction. Both are grounded. The bottom of the trough at y = 0 is specially designed such that the potential varies as a function of x (say by making it out of a resistive material and passing a current through it; the details are not important). The potential along this wall follows a sine function:

$$V(x,0) = V_0 \sin(\frac{\pi}{a}x)$$
 for $0 < x < a$

All the walls extend infinitely far in the z direction. Determine the potential between the walls by solving Laplace's equation.



Some random integrals

$$e^{-x}dx = -e^{-x}$$

$$\int xe^{-x} dx = -(x+1)e^{-x}$$
$$\int x^2 e^{-x} dx = -(x^2 + 2x + 2)e^{-x}$$

$$\int_{R}^{R} \int e^{-\eta jx + jz \sin x} dx = J_{n}(z) \text{ where } J_{n}(z) \text{ is a Bessel function of the first kind}$$

EE301 Final Examination

December 17, 2001

Welcome to the EE301 Final. This is an open book examination. You may refer to your textbook but not to any other material such as notes or other books. You may also use a

Answer five of the eight problems. You must do at least one of the transmission line problems (6, 7, 8). You must also do at least one of the magnetic field problems (3, 4). All of the problems contain subparts; the subparts are weighted equally.

clearly shown. If a symmetry argument is used, it is sufficient to write "By symmetry we know that...". Partial credit will be given for partially correct answers.

None of the problems require intricate mathematical manipulations. If you get stuck with

Show your work; credit will be given only if the correct steps leading to the answer are

None of the problems require intricate mathematical manipulations. If you get stuck with an impossible integral or equation, you are likely doing the problem incorrectly. Several formulas are given on the last page that you might or might not find useful.

The next two problems are on static magnetic fields. You must do either problem 3 or problem 4 (or both if you wish).

roblem 3

A cylindrical wire of radius a contains a cylindrical cavity of radius b offset from the center by a distance d (see illustration). The solid area of the wire carries a uniform current density $\bar{J} = J_0 \bar{a}_z$. Determine the magnetic field everywhere inside the cavity. To do this, use superposition—the current distribution can be thought of as a solid wire with current density \bar{J} superimposed on a smaller wire the size of the cavity with current density $-\bar{J}$. The solution has been broken down into the following steps.

- a) Determine the magnetic field inside a solid cylindrical wire with uniform current density \vec{r}
- b) Convert the above expression for the field from cylindrical coordinates to Cartesian coordinates.
- c) Use the above result to write down the field for a solid wire with current density $-\bar{J}$ of the shape and at the location of the cavity. Because the cavity is offset from the center you will have to modify the expression from b) in a simple way.
- d) Use the superposition principle to obtain the field in the cavity, i.e. add the fields from the big wire and small wire together.

Are you surprised by the result?



Problem 1

Given the two vectors: $\vec{A} = -\vec{a}_x + 2\vec{a}_y + 3\vec{a}_z$ and $\vec{B} = \vec{a}_x + 3\vec{a}_y + \vec{a}_z$.

- a) Calculate $|\vec{A}|$, $|\vec{B}|$, and $\vec{A} \cdot \vec{B}$.
- b) Calculate the angle between \vec{A} and \vec{B} .
- c) Determine a unit vector perpendicular to both \vec{A} and \vec{B} .

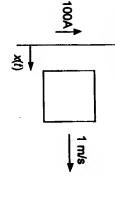
Problem 2

- a) A charge distribution expressed in cylindrical coordinates depends only on the variable ρ . What does that symmetry imply about the electric field due to this charge $\tilde{E}(\rho,\phi,z)$?
- b) Two parallel plate capacitors have identical dimensions but one is filled with a dielectric with $\varepsilon_R > 1$ and the other is not, i.e. $\varepsilon_R = 1$. Both are attached to a battery and charged to the same voltage V. In which capacitor does the electric field have the greater magnitude? Which capacitor has the greater charge on the plates? For both answers, a correct explanation is required.

Problem 4

An infinite straight wire carries a current of 100 Amps.

- a) What is the formula for the magnetic field due to this current?
- b) A square loop of wire 50 cm on a side is oriented in the plane containing the straight wire with the nearest edge parallel to the wire (see illustration). What is the flux through the loop if the distance from the nearest edge to the straight wire is x?
- c) The loop has total resistance of 10 Ω . The loop of wire starts with x(0) = 0 and moves away from the straight wire at constant velocity of 1 m/s. Determine the current in the loop as a function of time.



mblem !

An electromagnetic wave in free space has an electric field given by

$$\vec{E} = 100(\vec{a}_x + \vec{a}_y)e^{j(\alpha x - kz)} \text{ V/m}.$$

- a) Describe the polarization of the electromagnetic wave (i.e. the direction of the electric field).
- b) Determine the magnetic field of the wave.
- c) What is the average power density in the wave?

The next three problems are about transmission lines. You must do at least one of these three problems (or more if you wish). Since your text does not include all the transmission line equations, some additional equations are listed at the end.

Problem

- a) The dielectric used in a coaxial cable has $\varepsilon_R = 2.5$ and $\mu_R = 1$. What is the velocity of propagation in the cable at high frequencies?
- b) A transmission line has inductance 0.2 μ H/m and capacitance 100 pF/m. What is the characteristic impedance?
- c) A 50 Ω lossless transmission line has a velocity of propagation of 2×10^8 m/s. What are L and C?

Problem 7

A 50\Omega transmission line is terminated with an open (i.e. no load).

- a) What is the reflection coefficient at the load?
- b) What is the input impedance if the line has length !?
- c) What length should the transmission line be such that the input impedance is equal to that of a 50pF capacitor at 100MHz (express the length in wavelengths)? $(Z_C = 1/(j\omega C))$ but you knew that).

Problem 8

A step generator producing a 1 V step and with an internal impedance of 50Ω is connected to 2 m of 150Ω transmission line. The transmission line is terminated with a 250Ω load. The velocity of propagation in the transmission line is 1×10^8 m/s.

- a) What is the reflection coefficient at the load?
- b) What is the reflection coefficient at the generator?
- c) Draw a bounce diagram for 100 ns after the step is applied and label each bounce line with the height of the step.
- d) Graph the voltage at the generator end of the transmission line as a function of time for the first 100 ns.

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Some potentially useful information

Constants

$$\varepsilon_0 = 8.85 \times 10^{-12} \text{ F/m}$$

$$\mu_0 = 4\pi \times 10^{-7} \text{ N/A}^2$$

Transmission line equations.

Answer each of the first three problems.

Given the electric field (in spherical coordinates)

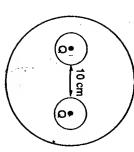
$$\vec{E} = Q\left(\frac{1}{r^2} - \left(\frac{1}{2} + \frac{1}{r} + \frac{1}{r^2}\right)e^{-r}\right)\vec{a}, \qquad \begin{cases} |-\binom{1}{2} \\ |-\binom{1}{2} \end{cases}$$

- b) Express the electric field vector at the point r = 1, $\theta = \pi/4$, $\varphi = \pi/4$ in Cartesian a) Calculate the charge density

Problem 2

cavities have diameters 10 cm and are separated by 10 cm of metal as shown. The metal illustration shows the sphere in cross section. The sphere has a diameter of 40 cm; the has no net charge. Into the center of each hollow is placed a charge Q. Determine A metal sphere has two spherical cavities inside it the same distance from the center; the

- a) The field inside the metal and inside the cavities. (5 points)
- b) The force that acts on each charge. (5 points)
- c) The field outside the metal sphere. (10 points)



University of Saskatchewan Department of Electrical Engineering

October 23, 2002

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EE301 Electricity, Magnetism and Fields Midterm Examination Professor Robert E. Johanson

books. You may also use a calculator. The examination lasts 2 hours. your textbook (Hayt and Buck) but not to any other material such as notes or other Welcome to the EE301 Midterm. This is an open book examination. You may refer to

to the answer are clearly shown. If a symmetry argument is used, it is sufficient to write are shown in parentheses. Show your work; credit will be given only if the steps leading "By symmetry we know that..". Partial credit will be given for partially correct answers Each problem is worth 20 points; if subparts are weighted differently, the points for each

You are to solve a total of 5 problems. Answer the first three problems and any two of

triples are always (x, y, z). None of the problems require intricate mathematical manipulations. Cartesian coordinate

FOR THE Tieee, usask.ca 2001 EXAMS,

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December 13, 2002

University of Saskatchewan Department of Electrical Engineering

EE301 Electricity, Magnetism and Fields Final Examination Professor Robert E. Johanson

Professor Robert E. Johanson

Welcome to the EE301 Final. This is an open book examination. You may refer to your textbook but not to any other material such as notes or other books. You may also use a calculator. The examination lasts 3 hours.

Answer six of the eight problems. Do not answer more than six problems or severe penalties will apply. You must do at least two of the transmission line problems (6, 7, 8). You must also do at least one of the magnetic field problems (3, 4).

Show your work; credit will be given only if the correct steps leading to the answer are clearly shown. If a symmetry argument is used, it is sufficient to write "By symmetry we know that...". Partial credit will be given for partially correct answers but only if correct intermediate steps are shown. Each problem is weighted equally although subparts of a problem might be worth varying amounts depending on difficulty.

None of the problems require intricate mathematical manipulations. If you have of the problems require intricate mathematical manipulations.

None of the problems require intricate mathematical manipulations. If you get stuck with an impossible integral or equation, you are likely approaching the problem incorrectly. Several formulas are given on the last page that you might or might not find useful.

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Problem 3

A 1 nF capacitor is charged to 10 V.

a) How much energy is stored in the capacitor?

The capacitor is removed from the voltage source and then connected in parallel to an uncharged 2 nF capacitor.

- b) What is the voltage across the capacitors?
- c) What is the total energy stored in both capacitors?
- d) What happened to the missing energy?

Answer any two of the following three problems.

Problem 4

A charge of 10 nC is placed at the origin. Charges of -5 nC are placed at the Cartesian coordinates (0, 0, 1) and (0, 1, 0) (all measurements in meters). Determine the electric field vector at the point (1, 1, 1) in Cartesian coordinates.

Problem 5

A dielectric sphere of radius a and relative dielectric constant e_R has embedded within it free charge with density given by (in spherical coordinates)

$$\rho = A(1-r/a)$$

where A is a constant. Determine the electric field \vec{E} , the displacement field \vec{D} , and the polarization field \vec{P} inside the sphere.

Problem 6

A parallel plate capacitor of area A and small plate separation d contains a dielectric between the plates. The dielectric constant varies linearly from ε_1 at the bottom plate to ε_2 at the upper plate. Solve for the electric field \tilde{E} between the plates far from any edge when a voltage V is applied between the plates. Determine a formula for the capacitance.

You might be interested to know that

$$\frac{\pi}{2\pi} \int_{-\pi}^{\pi} \int_{-\pi}^{e^{-\eta/x + |z| \sin x}} dx = J_n(z) \text{ where } J_n(z) \text{ is a Bessel function of the first kind}$$

but probably not.

Problem 4

- **a)** A circular loop of wire has a current 1 flowing through it. The loop has radius a. Use the Law of Biot-Savart to determine the magnetic field at the center of the loop.
- b) A small circular loop of wire is now placed at the center of the above loop. The radius of the smaller loop is b, and b << a. The two loops lie in the same plane. If the current in the larger loop varies sinusoidally with time as $I = I_0 \sin \omega t$, determine an approximate expression for the induced current in the smaller loop. Such magnetically coupled loops are used in RFID smart card technology.

Problem 5

A survey team wants to use electromagnetic waves to detect buried metal objects. The idea is to broadcast a 200 Mhz plane electromagnetic wave into the ground and detect any reflected wave. The receiving system can detect the reflected wave only if the electric field has an amplitude greater than 10 mV/cm. The conductivity of the soil is 10^{-3} S/m, and $\mu_{\kappa} = 1$. You may assume that the buried object acts like a perfect mirror reflecting all the power incident back towards the surface.

- a) What is the skin depth for the plane wave in the soil?
- b) What electric field amplitude of the transmitted electromagnetic wave is needed in order to detect objects buried 3 m deep?

The next three problems are about transmission lines. You must do at least two of these three problems (or all three if you wish). Since your text does not include all the transmission line equations, some additional equations are listed at the end.

Problem 6

- a) A lossless transmission line has an inductance of 0.5 μH/m and a capacitance of 50 pF/m. What is the characteristic impedance and the velocity of propagation?
- b) A cellular telephone antenna has an impedance of $50 + j10\Omega$ at 900 MHz. It is directly connected (i.e. no matching network) to a 2 m length of 50Ω transmission line. What is the reflection coefficient off the antenna? What is the input impedance of the transmission line with the antenna connected? The velocity of propagation in the transmission line is 2×10^4 m/s.

Problem 1

At the point P = (1, 1, 1) (in Cartesian coordinates) there are two vectors $\vec{A} = -\vec{a}_x - \vec{a}_y - \vec{a}_z$ and $\vec{B} = 2\vec{a}_x + 2\vec{a}_y - \vec{a}_z$.

- a) Calculate $|\vec{A}|$, $|\vec{B}|$, and $\vec{A} \cdot \vec{B}$
- b) Express the vector \vec{A} in spherical coordinates.
- c) Determine a unit vector perpendicular to both \vec{A} and \vec{B} .

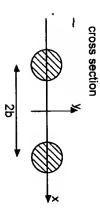
Problem 2

- a) A point charge of 100 μ C is located at the origin. What is the total electric flux passing through the plane parallel to the x-y plane but offset to z = 1?
- b) A parallel plate capacitor uses 15 μ m thick mylar as a dielectric. Mylar has a relative permittivity of 3.2 and a dielectric strength of 1.5×10^6 volts per cm. The dielectric strength is the maximum electric field that can exist in the dielectric without breakdown (breakdown would likely destroy the device). If the area of the plates is 100 cm², what is the maximum amount of energy that can be safely stored in the capacitor?

The next two problems are on static magnetic fields. You must do either problem 3 or problem 4 (or both if you wish).

Problem 3

Two infinitely long, straight wires each with radius a are parallel to each other and separated by a distance 2b (see cross section below). A current I flows in each wire but in opposite directions. Determine an equation for the magnetic field everywhere along the x-axis (including inside the wires. You may assume the current density is uniform within the wires. (hint: use superposition)



4.

Some potentially useful information

Constants

$$\varepsilon_0 = 8.85 \times 10^{-12} \text{ F/m}$$

$$\mu_0 = 4\pi \times 10^{-7} \text{ N/A}^2$$

 $\Gamma = \frac{Z_L - Z_0}{Z_L + Z_0}$

Transmission line equations.

$$T = \Gamma + 1$$

$$Z_{in} = Z_0 \frac{Z_L + jZ_0 \tan \beta l}{Z_0 + jZ_L \tan \beta l} \qquad l \ge 0$$

$$Z_{in} = Z_0 \frac{1 + \Gamma e^{-j2\beta l}}{1 - \Gamma e^{-j2\beta l}} \qquad l \ge 0$$

 $\beta = 2\pi/\lambda$

Problem 7

An antenna with impedance $20 + j100\Omega$ receives a power feed over a 75 Ω transmission line. Design a matching scheme (you choose the type) so that no power is reflected from the antenna. Work out your matching scheme on the Smith chart.

roblem 8

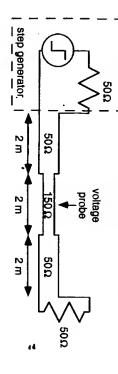
A step generator producing a 1 V step and with an internal impedance of 50 Ω is connected to a transmission line consisting of a 2 m length of 50 Ω line joined to a 2m length of 150 Ω line that is then joined to another 2m length of 50 Ω line (see diagram). The whole transmission line is terminated with a 50 Ω load. The velocity of propagation in the transmission line is 1×10^8 m/s.

- a) Determine the reflection and transmission coefficients at each junction.
- b) Draw a bounce diagram for 100 ns after the step is applied and label each bounce line with the height of the step.

c) Graph the voltage at the center of the 150\O line for 100 ns after the step is

applied.

d) What will the voltage eventually reach at this point after a long time?



EE 331 Midterm Examination October 21, 2002

2 Hours

Open Book

Two pages

20 Marks (5 marks each)

(a) Describe the differences between these instruction sequences? R1,#80H

MOV

inc 80H

(b) Briefly describe the 5 memory spaces provided by the 8751 architecture and explain how you would access data from each of these regions.

(c) Describe unsigned binary, two's complement numeric representation? What support does the 8751 architecture provide for performing the four basic arithmetic operations on single-byte values in these representations.

(d) Given that the first byte of each of the following instructions is at location 3F0H, what are the ranges of addresses which could be reached by each of the instructions?

om jap ALABEL ALABEL

20 Marks (4 marks each) What will be the value of the accumulator, the carry bit, and the overflow bit after an 8051 executes each of the following instruction sequences? Note that some values may be

(d) mov (b) mov rr add (c) mov cjne (a) clr mov aubb ٧Om A, #22H A, #24H, 100 A, #0F2H A A, #70H A, #0D2H A, 20H 20H, #20H A, #OFFH

(e) clr mov djnz mov

PSW 0,#1 R0,70 A.R0

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20 Marks
 20 Praw the schematic of a circuit to add 16 kbytes of external program memory and 8 kbytes of external data memory to an 87C51 system.

All external memory devices should be 8k×8.

- The addresses must be fully decoded but the only components available are inverters and 3-input
- The external program memory should appear at locations 8000H to BFFFH.
- The external data memory should appear at locations C000H to DFFFH.

Marks
 Write a simple 'walking-I' memory-test subroutine for the above system:

- (a) Write 00H to all external data memory locations.
- (b) Write 01H to the first external data memory location.
- (c) Verify that reading the first external data memory location returns 01H and that all other memory locations still contain 00H. If not, your subroutine should return with a value of 0 in the
- (d) Write 02H to the first external data memory location.
- (c) Verify that reacting the flat external data memory location returns 02H and that all other mem-rory locations still contain 00H. If not, your subrounne should return with a value of 0 in the accumulator.
- (f) Repeat until all bits of the first external data memory location have been tested.
- (g) Repeat from step (b) for all external data memory locations.

If the tests succeed your subroutine should return with a value of I in the accu mulator.

Your program should be adequately commented so that it can be readily understood. The purpose and location of all variables should be described.

Hint: Write a teat. Ham subroutine which takes two arguments – the 16 bit value of the external memory address which should contain the non-zero value, and the 8 bit value which should be at that

Write an 8051 assembly-language aubrousine which multiplies two 8-bit, signed (two's complement) values and returns a 16-bit signed result. One argument is passed to the subcontine this excumulator and other is passed to the subcontine should return with the most-significant byte of the product in SFR B and the least-significant byte of the product in the

int: Use the 87C51 MUL AB instruction to multiply the absolute value of the arguments then negate

Benau queation (4 marks): Write your subroutine so that it uses no resourc es other than the accumu-lator, SFR B, and the processor status word.

END



1.



```
CODE
                                                                                                              1.1800 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576 | 576
   0017 FF
0018 B401F5
001B A3
001C E583
001E B4EDEF
0021 7401
                                                                                                                                                                                                                                                                     R7,A
A,$1,BITLOOP
DPTR
A,DPH
A,#[(MEMGASE-
A,#1
                                                                                                                                                                  HOV
CJNE
INC
NOV
CJNE
HOV
DOMENEHORYTEST:
                                                                                                                                                                                                                                                                                                                                                                              ; Return success/fellura code
                                                                                                                                                                                teetMem subroutine
                                                                                                                                                                                                          leter aseignments

R4 - Reschack check value

R5 - Low byte of test location

R6 - High byte of test location
                                                                                                                                                                               Return value
0 - Feilure &
1 - Succese
                                                                                                                                                                                                                   1 - SULCEUM

test Location <- test value

for(all memory locations)

if(location = test location)

readback check value = test value

else

readback check value = 0

if((test location) := readback check value)

return 0
                                                                                                                                                                                                                                  Write test value into test location
   0024 EP
0029 PO
                                                                                                                                                                                                                     HOVE
                                                                                                                                                                                                                                                                     A,R7
MOPTR,A
                                                                                                                                                                                                                                                                                                                                                                           ; Get test value ; Store test value in test location
                                                                                                                                                                                                                       ; Loop over all locations
                                                                                                                                                                                                                                                                     RS.DPL ; Remember took location
R6.DPE
DPTR.BMEMBASE ; Start of beginning of memory
 0026 AD62
0028 AE63
002A 90C000
                                                                                                                                                                                                                     ; Determine readback check value
                                                                                                                                                                                                                                                                   R4.80 ; Assume it's not the test locet;
A.85 ; Skip if low bytes don't match
A.86 ; Skip if high bytes don't match
A.988,MOTESTLOC
; Skip if high bytes don't match
A.988,MOTESTLOC
; Test location -- readback is to
002D 7C00
002F ED
0030 R54206
0033 EE
0034 R58302
0037 EF
                                                                                                                                                                                                                                                                                                                                                                                ; Assume it's not the test location ; Skip if low bytes don't match
```

000E F0C000 000E 7F01 0013 600E 0013 60E ADDE CODE 00000 Absembly process 900000 liet / Constants / MEMBASE EQU MEMSIZE EQU BOURCE Return velue 0 - Feilure 1 - Buncese Welking-1 memory test Verlables Register easignments R7 . The single non-zero test value in memory Memory test subroutine for(all memory logstions)
ast logstion = 0
for(all memory logstion)
for(all memory logstions)
for(all bit values)
set test logstion = value
cell Memoryher
lf (return value le sero)
fif testin value le sero) H ON THE MON CAN MONEY Loop over all locations TRETHEN

| Tast this location
| DobmissosTEST | Rad news - report failure
| Anary | Gat test value
| Anary | Mart bit
| Anary | Mart bit | Anary | Mart bit | Anary | Anary | Mart bit 27, 61 DTTR, #MEMBASS ; Set pointer to external , set value to write to axternal m spyra, A (Clear one byte care to extraoral m to the control of the control of the control of the control of the care to the control of the care to the DPTR, MYZMASZ , First value to test / Mumber of locations to test

S4.LS

0021 22	0017		001B	0010	0017	0014	0013		0011	4000	000C 63FOFF	0009 307707		0007 B2D5	0006 04	0005 1	0002 30E704	0000									ADDX	Assant
3	0570	5002	2401	437077	7	0014 30D50A	*		B2D5	0570	53F0FF	107707		92D5	*	74	30E704	C205									CODE	Assambly process list:
, <u>,</u>	25	24	23	22	21	20	17	1	17	1	15	ï	13	12	11	10	•	-	7	• •		•	u	a)	-		LINE	liet.
DONE;								300E					APOE -						B1GNEDMUL.			•	-	, eign	•	-	BOURCE	
1	INC	SHC.	ADD	XRL	CPL	JNB	ğ		CPI	INC	XRL	CHIC		CP.	INC	CPL	JNB	CLA	ğ		Na contract	Multipl	Form ab	d 0-bit				
	8	DONE	>,#1	E, #077H	,	FO, DOWN	2		3	-	B, #OFFH	B. 7, BPOE		70	>	>	Acc. 1, APOS	Po		A	result if one on	Multiply absolute values	Form absolute value of operands	eigned e-bit multiplication				•
					, Otherwise negata result	/ Skip if result >= 0	/ Multiply absolute values		, And complement negata-result flag		/ Otherwise negsts 3	, Skip if B is >= 0		, And complement negata-result flag		/ Otherwise negeta A	, Skip if A is on 0	/ Clear negata-rasult flag			Manager Tabilit 16 Day Operand was personive		operands					

.(

003) E0 0031 6C 0031 6C 0030 740 002D 740 002D 72 0040 A3 0041 E563 0041 P365 0041 P365 0042 P480CA ADDR CODE HOUNCE

HOVE MAIA

HOTTBETICG:

VOLLY MANDEY 16

HOYN A. BOPTR

MAIA

MAIA

MODE A. BOPTR

HOY A. 40

HOY A. 50

HOY A. 5 TR / Rand autarnal memory
Yoss it match the autarnets
Yoss after return value
Note and return value
Note pointer to met location
Get high byte of pointer
HEMBARS-MEMISS, ETTLOSY / Loop till all cleared
Note and the second status

S4.LST

EE 331 Midterm Examination October 24, 2001

The second secon

2 Hours

Open Book

· Two pages

25 Marks (5 marks each)

(a) Describe the differences between this instruction

inc A

and this instruction

(b) Briefly describe the \$7C51 immediate, direct and indirect addressing modes. Given an example

of each. Which memory locations are accessible by these modes?

(c) Describe the binary Gray Code and it's applications.

(d) What will be the value of the accumulator, the carry bit, and the overflow bit after an \$051 executes each of the following instruction sequences? Note that some values may be indetermined.

```
mov
subb
ii. clr
mov
subb
iii. mov
cjns
iv. mov
add
rlc
inc
                                                              i clr
                      A, #20H
                                  A, FFFH
           A, 412H
A, 477H
                                         A, #F2H
                                                    A, #F2H
                                                          A, #70H
```

(e) Describe the differences between the three versions of the just instruction

ajmp ALABEL 1jmp ALABEL

2. 25 Marks data memory to an 87CS1 system. Draw the achematic of a circuit to add 8 toytes of external program memory and 16 toytes of external

- All external memory devices should be 8k×8.
- The address but should be fully decoded using only invertors and 4-lagut NAND gates. The external program memory should appear at locations 2000H to NATH.
- The external data memory should appear at locations 0000H to 3FFFFI.

Write an 87C51 subroutine which reverses, in place, a block of internal data memory and returns a value indicating whether or not the block of memory was palindromic (i.e. that the contents after reversal are the same as before. The arguments to the subroutine are:

- In the accumulator, the length of the block of memory.
- In R0, the address of the first location of the block of memory

On return from your subroutine, the contents of the block of memory should be reversed. The carry flag (C) should be set to 1 if the block of memory was a palindrome and set to 0 if the block of memory was not a palindrome. The contents of the accumulator and registers should be the same as when the subroutine was called.

For example, suppose the subroutine was called with the accumulator set to 5 and R0 set to 40H, and the contents of the five memory locations beginning at location 40H were 01H, 02H, 23H, 12H, 30H. On return from the subroutine the five memory locations beginning at location 40H would contain 30H, 12H, 23H, 01H and the carry fing would be clear.

used for the 87C51 registers. You may assume that the block of memory to be reversed will not overlap any of the memory locations

4. 25 Marks

Write an 8751 assembly-language subroutine which performs binary to ASCII hexadecimal conversion on unsigned binary values of arbitrary length. The arguments to the subroutine are:

- R0 Pointer to the N-byte value to be converted to ASCII hexadecimal representation. The value is stored most-significant-byte first.
- R1 Pointer to the 2N-byte output buffer where the ASCII values are to be stored.
- A The number of bytes to be converted.

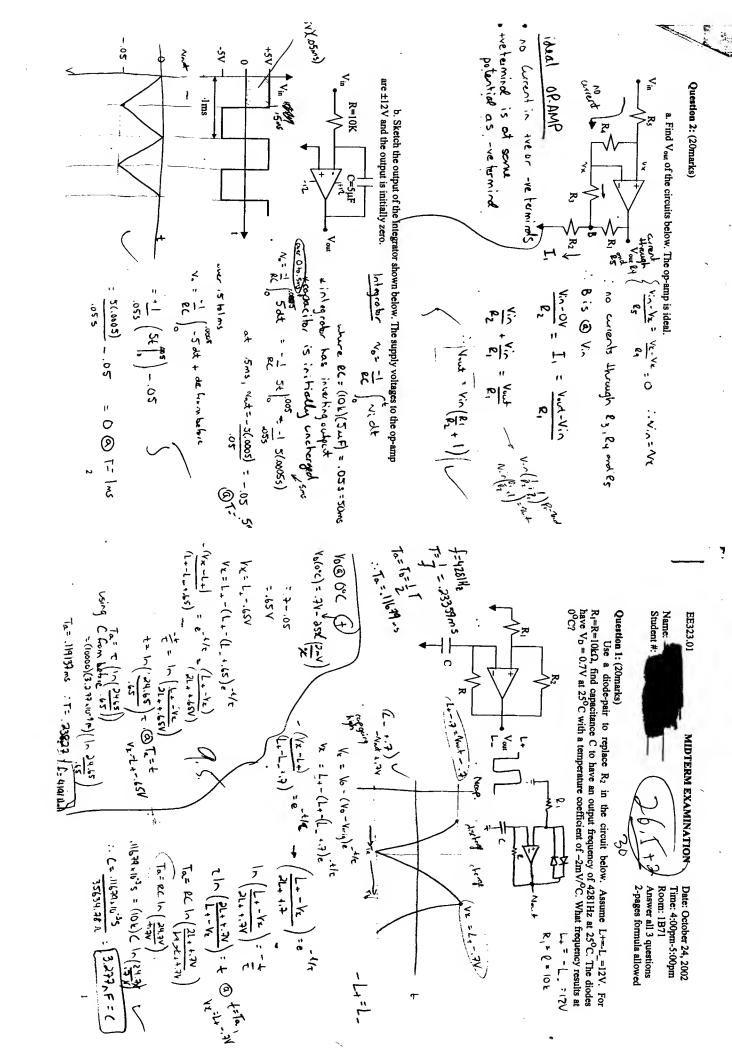
Leading zeroes should be converted to ASCII space characters.

END

(unt: 10 kicthan 17 MU A, QRO lesselluni mav Qe, A+'o'-#10n MOU (wat, A ANL A, #OFL Cync A, #OAh, out MOV @RI, A+'A'-#104

300

1 no dec count



Instructor: A. Dinh EE323.3 (01)

Final Examination

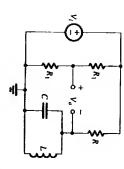
Date: December 10, 2002

Room 165, Physic Time: 9:00am - 12:00pm

Answer all 6 questions in 4 pages. State clearly appropriate assumptions (if any) in your answers. 4-page formula sheet and calculator are allowed.

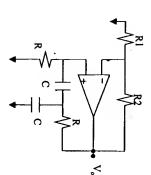
Question 1: (20 marks)

Derive the transfer function, $V_{\nu}V_{\nu}$, of the all-pass filter below. For a given R, L, C, find frequencies at which the output undergoes a phase shift of 90° and 180° (i.e., frequencies are functions of R, L, C). Find sensitivity of the 90° frequency with respect to the inductor L.



2. Question 2: (20 marks)

Find R2/R1 for oscillation. For the circuit below, find the loop gain L(s), L(j\o), and the frequency for zero loop-phase.



the minimum closed loop gain of this op. ANA when y binder -we know that oscillation con occur when the Gregues of hours oscillation can occur when the Gregues of hours oscillation and the six in the company of input is increased to be a second of the company o

gain that correlates the minimum gain and not oscillating

A=9.08

Question 3: (20marks)

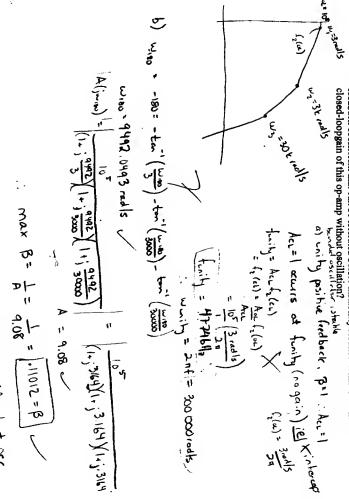
An op-amp has the following open-loop transfer function:

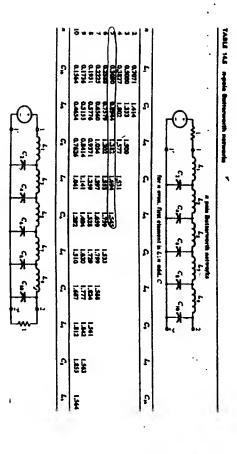
$$A(j\omega) = \frac{v_{\text{OH}}}{v_{\text{in}}} = \frac{10^5}{(1+j\frac{\omega}{\omega_1})(1+j\frac{\omega}{\omega_2})(1+j\frac{\omega}{\omega_3})}$$

$$A(j\omega) = \frac{v_{\text{OH}}}{v_{\text{in}}} = \frac{1}{\omega_1} \frac{v_{\text{oH}}}{\omega_2} = \frac{v_{\text{oH}}}{\omega_3} = \frac{v_{\text{oH}}}$$

where $\omega_1 = 3 \text{ rad/s}$, $\omega_2 = 3 \text{ krad/s}$, and $\omega_3 = 30 \text{ krad/s}$.

- The op-amp is connected in a unity positive feedback configuration. What is the output frequency of the op-amp?
- The op-amp is connected in a negative feedback configuration. What is the maximum feedback coefficient that can be tolerated before instability results? What is the minimum



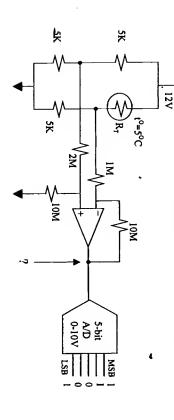


Question 5: (20 marks)

span of 0 to 10V saturation of $\pm 12V$. The A/D is a 5-bit successive-approximation A/D converter type with an analog Consider the circuit in a temperature measurement below. The op-amps have an output

- Find the input voltage of the A/D converter.
- The thermistor, R_T , has a resistance of 2K Ω at 20°C. Find the coefficient β of the thermistor if its temperature in the circuit is 5°C.

Formula:
$$R(T) = R(T_0)e^{\beta(1/T-1/T_0)}$$
 where β and T are in K .



3. Question 3: (20 marks)

Provide (very) short answers to the following questions:

- Name 4 physical effects contribute to the voltage generated in a thermal couple.
- Why standards and calibration are required in instrumentations?
- from extrinsic noise? List intrinsic noise sources in instrumentation circuits. How to protect circuits
- ₹ What are the benefits and what are the drawbacks in using digital instrumentations?
- the users. thermistor as a sensing element and current temperature is sent over the internet to Draw a block diagram for a remote temperature measuring system using
- ŗ A capacitive displacement sensor is calibrated using the bridge network below. The bridge d=0.1mm, and $\varepsilon_0=8.8542 \times 10^{-12}$ F/m. sensor. It is known that the sensor has a capacitance of $C = \frac{5c_0bx}{1}$, where b=1cm, is balanced when the input frequency is adjusted to 8MHz. Find displacement ,x, of the
- l E=10V f=8MHz 10E 22 10 23 23 sensor 10kS 10ES 1.2μΗ

Question 4: (20 marks)

converter. The filter should have a cut off, ω_p , at Nyquist frequency with an A_{max} of IdB and A_{min} of a sampling rate of 20Ksample/second. Find the Nyquyst frequency of the analog signal from the transducer. Design a Butterworh response RLC filter for anti-aliasing purpose in front of the A/D 10eB at a frequency of 1.5 times Nyquist frequency. Use 50Ω resistor at the filter input. In a digital instrumentation system to measure velocity of a fluid pipe, the A/D converter has

$$A(\omega_s) = 10 \log[1 + \varepsilon^2 (\frac{\omega_s}{\omega_p})^{2N}]$$

Formulae:

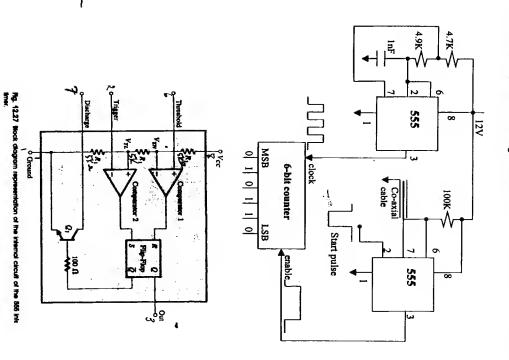
 $A_{MAX} = 20\log(\sqrt{1+\epsilon^2})$ and

ε= √10 10

L

6. Question 6: (20 marks)

A group of students set up the circuit below to measure the length of a cable for their 4th year project. The co-axial cable is a capacitor having 5.2pF/m. The 6-bit counter is enabled from a monostable circuit and its clock is from an astable circuit. If the final count from the counter is 010110 as shown, calculate the length of the cable.



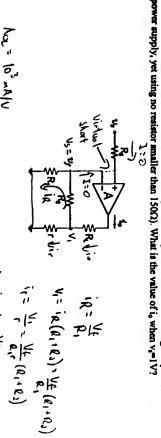
MIDTERM

Open books, open notes. Answer all questions.
Use the other site of the paper if you require more space.

1. Question 1 (15 marks) (47/50

branchiset on J

of R₁, R₂, and r to make $i_{\ell}/v_s = 10 \text{ mA/V}$, (while allowing the voltage across R_L to be as large as possible for and zero output resistance. For input v, and output io, find an expression for the feedback factor $\beta = v/i_0$. For a paper loop gain $A = 10^3$ mA/V, what must β be for a closed-loop gain of 10 mA/V? For this β , find values In the non-inverting voltage-to-current converter shown, the basic op-smp has infinite input resistance



NOL = 103 MA/V

Act: Noc

For ALL= 1-Small

10 103-01V 10-164 + 104 m Ah2 (p) = 10 mAlv 104ma76.1(8) = 990.01/2

B= Nt = Nt (0+0:) 10=18+11= Nf Vf (8+92)

T+B, 181

F + A 1 1 A 2

the material comply: For Up, to be a moy, by much be a mingrice. It serveptes their, choose [1-150] and find min, positive volves to Reand Rd.

18= 140,1021 150AR1

14050 n2 + 90 nd, +94 nd2 - 150 nd.

99221= SIZZ1-1485022 H= 0.515 R1-1502

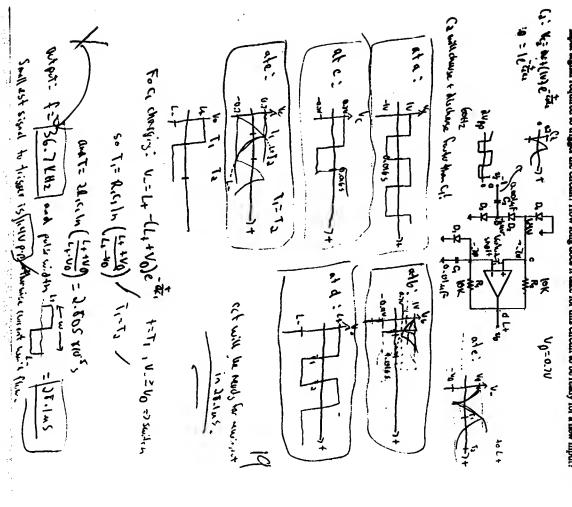
Chose 12=1502

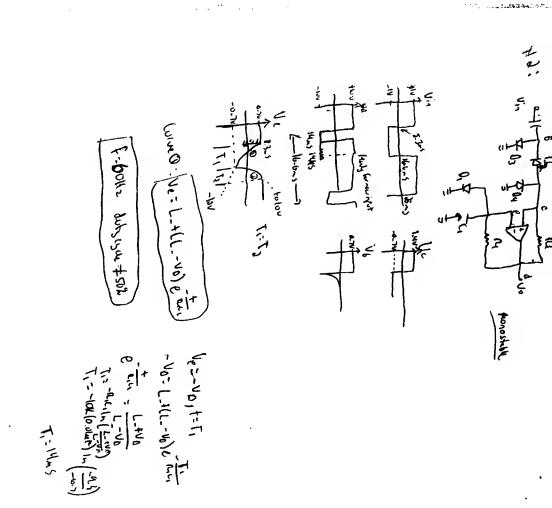
that 3002= 0.515 R1 12 - 5832 X

If Act = 10mply and Us=1V, +4m:

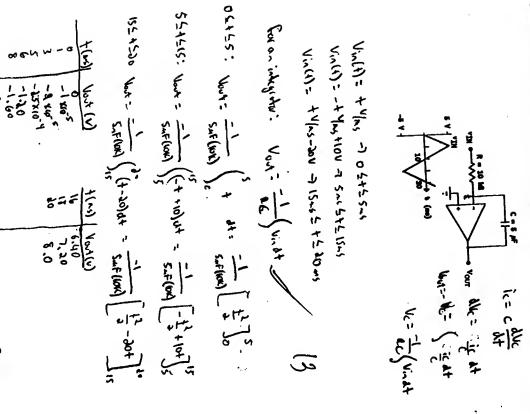
10= ACCUS = 10-A/V(10) 10= 10-1

Consider the circuit shown, using diodes which conduct at $V_D = 0.7V_c$ and an amplifier seturating at $\pm 10V_c$ with R1 = R2 = 10 K and C1 = 10C2 = 0.01 µF. Find the output pulse width and frequency, if v_1 is a 60 Hz square wave of 2Vpp samplitude. Sketch the waveforms at nodes a through c. What is the smallest input signal required to trigger the circuit? How long does it take for this circuit to be ready for a new input?



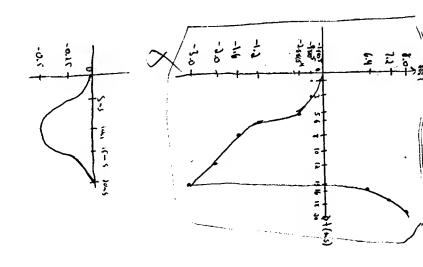


A 5V peak triangular voltage with a period of 20ms, depicted on the axis shown below, is applied to an ideal op-smp integrator. Sketch v_{our} as a function of time. The capacitor has zero initial charge.



0.6-

(owo)



Instructor: A. Dinh

Final Examination

Date: December 11, 2001 Time: 9:00am - 12:00pm

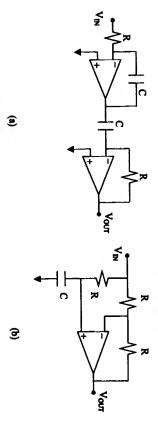
Answer 5 out of 6 questions.

Open books, open notes.

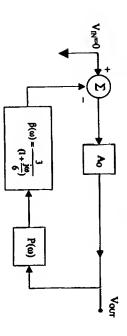
Good luck and have a Merry Christmas.

Question 1: (20 marks)

For the circuits (a) and (b) below, derive transfer functions V_{OUT}/V_{IN} as a function of frequency. For R=10K and C=15.9nF, aketch amplitude and phase response of V_{OUT}/V_{IN} .



2. Question 2: (20 marks)

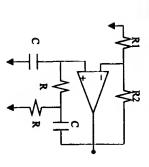


- ೮೬ Find the frequency of oscillation.

 Find the minimum value of A_O needed to maintain oscillation.

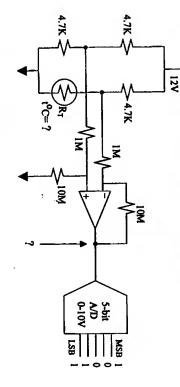
Question 3: (20 marks)

For the circuit below, find the loop gain L(s), L(jes), the frequency for zero loop-phase. Find R2/R1 for oscillation.



Question 4: (20 marks)

approximation A/D converter type with an analog span of 0 to 10V, find the input voltage of the A/D converter. The thermistor, R_{T} , has a resistance of 2K at 20°C and the coefficient β is assumed to be constant at 3650, find temperature of the thermistor. Consider the circuit in a temperature measurement below. The A/D is a 5-bit successive-

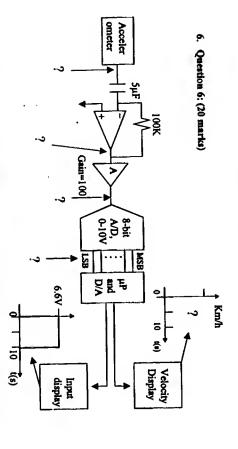


5. Question 5: (20 marks)

In a digital instrumentation system to measure velocity of a fluid pipe, the A/D converter has a sampling rate of 20Ksample/second. Find the Nyquyst frequency of the analog signal from the transducer. Design an active filter for anti-aliasing purpose in front of the A/D converter. The the filter passband and only 10K resistors are available to realize the filter. Since the output signal of the transducer has a wide range of frequency, no ripple is allowed in filter should have a cut off frequency at Nyquist frequency with a selection of F₅₀/F₃ is at least 3.

Table 13-1, Design State for Chalquister Films Thequatry — deaths frequency — 1.0

	American Conta	a va a 40 0	Andre of section
	기간	2525223	7 1 2
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	22		2
2 5555 55555	er er		2
eladelelel	22	12811 12811	0
	22	25 C F	2
		ee e	2
	98	5 £	087
i i	27	5	2
	1		



The above arrangement is used to measure velocity of a vehicle (not a good design). The waveform shown at the input display is the output of the D/A converter (data from A/D connects directly to D/A). Ignore quantization error, find the A/D output word. Sketch analog input voltage waveform at the A/D converter, the amplifier A input and the accelerometer output. The accelerometer has an inversion factor of 0.25V/m/s² (i.e., 250mV corresponds to 1m/s²), find final velocity of the vehicle if its initial velocity is 100Km/h and sketch the vehicle velocity.

University of Saskatchewan Department of Electrical Engineering EE 330/EE 452 Instrumentation Midterm Examination

October, 2001

Instructor: R.E. Gander

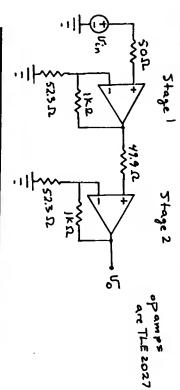
Duration: 50 minutes

Note: One bound textbook, course notes, calculator and assig

One bound textbook, course notes, calculator and assignments allowed.

Answer BOTH questions. The questions are of equal value.

In Assignment #3 you designed an amplifier with a gain of 400. An alternate approach is shown below. Determine the equivalent voltage noise at the input for the system. Assume that the ambient temperature is 35 °C and assume a noise equivalent bandwidth of 50 Hz at a center frequency of 2 kHz. What is the relative contribution of each stage to the total noise?



operating characteristics at specified free-air temperature, VCC± ± ±15 V

	Š	2	AH.		s	(Adba)		~		\$			
Property of the Party of the Pa	bandwidth	(see Figure 3)	Total harmonic distortion	CLAMBAR	Equivalent input noise	trans note volume	(2 auth. eat) shape.	Equinations input motor				PARAMETER	
PL - 2100, C1 - 100 pF	PL - 210	AL - 2100 CL - 1009F	See Note 5	1 . I BA	- 8H	1 = 0.1 Hz to 10 Hz	Hg = 100 D, 1 = 1 HH	Pg - 100 Q, 1 - 10 Hz	See Figure 1	FL - 210. CL - 100 FF.		TEST CONDITIONS	TAN
28°C	28.0	28°C	28°C	:	38.5	25°C		28	Full range	29°C	3	=	
ŧ	8	7 13	**************************************	0.4	15	850 250	2.6 4.6	3.3 6	1.2	1.7 2.8	XVIII dal MINI	TLEM27C	100
S,	8	• 13	× 0.002%	0.4 0.6	1.8	50 130	2.6 3.5	3.9 4.5	1.2	1.7 2.8	MAN TYP MAX	TLE2027AC	
	Ę	F		THAM		۸.	THE MAIL		į		9		

OTE 5: Measured distortion of the source wasd in the analysis was 0,002%

for this transdancer so that the output is 0 to 10 V over the temperature range 0 to 100 °C. Your design abould strive to maximize the sensitivity, but it should not cause a selfof 0.4 Ω/Ω/K, and a thermal dissipation constant of 5 mW/K. Design an interface circuit A platinum ICID pashe has a resistance of 1000 Ω at 25 °C, a temperature co-efficient, α

Department of Electrical Engineering EE 452/EE830 - Instrumentation University of Saskatchewan

Final Examination

December 2001

Instructor: R. E. Gander

3 Hours

Calculator, one bound textbook, published Course Notes, individual course notes and assignments allowed.

Answer ALL questions.

Marks

& A cable (wire rope) manufacturer is interested in measuring the force exerted on and the cable. Discuss 3 possible ways of measuring each of the two parameters (that is, force should also decide which of the proposed methods seems to be the most promising. and velocity). Provide sketches to clarify any mechanical mounting or interfacing. Your discussion should include advantages and disadvantages of each method. You velocity of the cable as it is pulled through the machine used to wind the strands of the

g 'n A resolver is to be used to measure angular displacement over the range ±25°. The resolver has two outputs available:

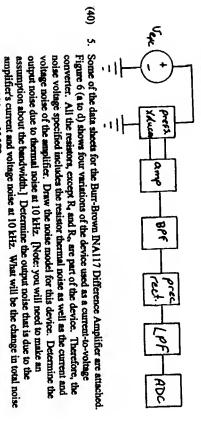
where aver = 10 Vmm $v_2 = av_{\rm max}\cos\theta$ VI = avadin 0

output voltage with respect to angle. The sketch should be sufficiently accurate to required to achieve this resolution if the signal is digitized? indicate any nonlinearity in the relationship. What voltage resolution will be required output, what will be the rms voltage range? Sketch the expected transfer function of the to achieve 0.1° angular displacement resolution? What is the minimum word size Explain which output would be better to use over the specified range. For the selected

3 3. A civil engineer is using a microcomputer-based data acquisition system to record engineer is using a function generator to feed a sinusoidal signal to all 8 channels multiplexer, a sample and hold circuit, and a 12-bit analog to digital converter. The vibrations at 8 points on a bridge truss during load testing. The load test simulates the flow of traffic across the bridge. The data acquisition board has an 8-channel line up properly". How would you explain to her that the sampling process causes this shifting? (Incidentally, how much phase shift do you expect?) Is this phase shift a 500 Hz prior to being connected to a multiplexer input. In order to test this set-up, the signals is passed through a low-pass, anti-aliasing filter with a cutoff frequency of maximum acquisition rate is 40,000 samples per second. Each of the eight vibration reason for concern in her application? when she uses a frequency close to the cutoff frequency, the waveforms displayed "don' simultaneously. At low frequencies, everything seems to work properly. However,

Mada

Ê . The instrumentation system shown below is to be used to measure fluid pressure in a hydraulic actuator. The pressure signal has a bandwidth of 10 Hz. A 5-kHz, 5-Vm., sinusoidal voltage source is used to excite the transducer bridge. The bandpass pass filter are used to obtain a de voltage proportional to the pressure signal. The low-pass filter must pass the voltage signal due to pressure variation with no more than 1% filter of order greater than 2 is required, provide the detailed design for one secondattenuation, but it must attenuate the 10-kHz rectifier ripple by at least 60 dB. Design a low-pass filter with the necessary passband and stopband characteristics. [Note: if a filter/amplifier is used to amplify the bridge output. The precision rectifier and low-



mony Chustones!

at +125 °C? at -55 °C?



High Common-Mode Voltage DIFFERENCE AMPLIFIER

in many applications, whose galvanic includes is not executed, the IPA/117 can explain includes as qualities. This can eliminate could justice the power supplies and their associated rigade, make and quiescent current. The IPA/117's 0000'th anniformity and 20006'th bendwidth are squarier to those of current thank locksion amplifiers. The INA117 is available in 8-pin plants mini-DIP and SO-8 neufron-mount packages, specified for the O'C to +7V°C temperature range. The mount TO-99 models are available specified for the -23°C to +85°C and -55°C. The INA117 is a precision and amplifier with very high common range. It is a single monolitaic precision op map and integral partwork. It can accurately means PROTECTED BIPUTE: ±500V Common-Mode ±500V Differential · CHARLE BEAR BEER MONLHEADITY: 0.001% mest O UNITY GAST: 8.02% Cain Error met ±200V. The BKAII7 FEATURES COMMONANCE BAPUT RANGE: SIGNAL ACQUISITION IN NOISY ENVINONMENTS **O PACTORY AUTOMATION** · NALL MULTINA • GROUND BREAKER **O BATTERY CELL-VOLTAGE MONTOR APPLICATIONS** INSTRUMENTATION AMPLIFIERS

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Burr-Brown IC Data Book-Linear Products

For immediate Assistance, Contact Year Local Subspenses

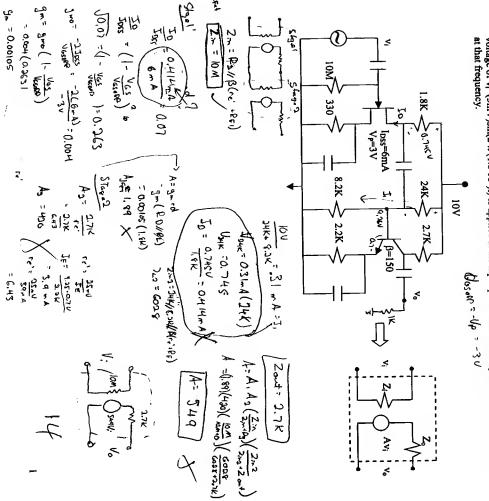
Date: February 13, 2001 Time: 1:00pm-2:30pm

Student name:

Answer 3 out of 4 questions. Use the other side of the paper if you need more space. Student number.

Question 1 (20 marks)

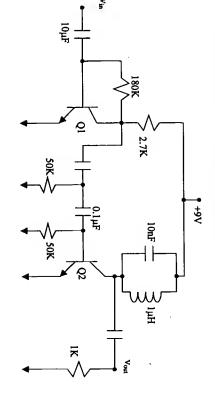
voltage of v_i =(5mV)sin(2. π ·(1.6·10°)t) is applied at the input port. Assume all capacitors are short circuit a. Represent the multistage amplifier on the left as a two-port device shown on the right b. A 1K load is connected to the output port, write the expression of the output waveform if



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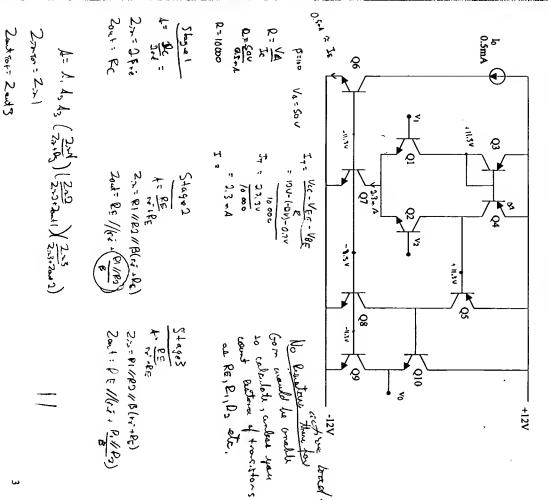
Question 2 (20marks)

For the circuit below, write the expression and sketch the waveform of the output voltage, (v_{out}), if v_{in} =(5mV)sin(2. π :(1.6·10⁶)t). The transistors have β_{DC} = β_{ac} =200 and V_{BE} =0.7V. Assume the class C amplifier (Q2) generates a full output voltage swing from 9V supply.



Question 3 (20marks)

impedances. All of the transistor pairs are matched. The transistors have β =100, V_{BE} =0.7V and early voltage V_A =50V. What does the gain become with a 1K load? For the amplifier shown below, find the ac voltage gain $\frac{v_0}{v_2-v_1}$, the input and output



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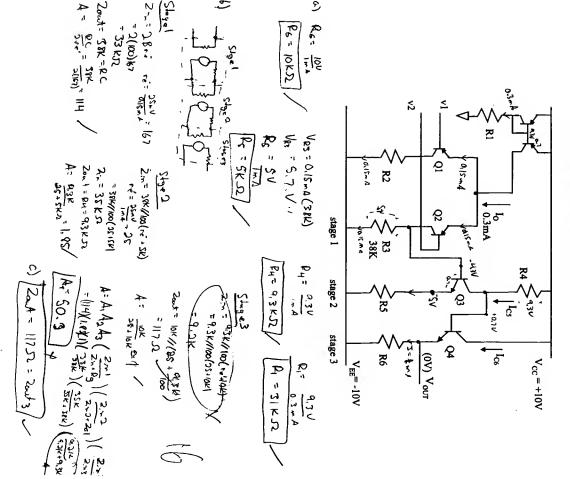
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Question 4 (20marks)

zero. Assume the transistors have $V_{BE}=0.7V$ and $\beta=100.$ Q1 and Q2 are matched. a. Find R1, R4, R5 and R6 to achieve the desired bias parameter. The circuit below is to be biased so that $V_{OUT} = 0$ Volt and $I_{C5} = I_{C6} = 1$ mA when the inputs are

b. Find total gain of the amplifier.

c. Find output impedance of the overall amplifier.



Shop

University of Saskatchewan College of Engineering EE 321.3 Final Examination

Instructor: J.E. Morelli

Date 14 April, 2000 Time: 3 hours (09:00 - 12:00)

Notes: All questions have equal value One page of notes may be brought into the examination. Hand held calculators are permitted. Answer only 5 of the 6 questions

State any assumptions and justify all of your answers.

Budget your time wisely as this is a long examination.

1b and 1. A FET transistor circuit is shown in Figure 1a. Also shown are the output characteristic and the transfer characteristic in Figures ic respectively

gg V

behaviour is produced. how this transistor works and how the output characteristic a What type of FET is used in this circuit? Briefly describe

the following values: Given that basic equation for this FET, ID = k (Vas -V_i)², find

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vii. V_{DQ} / Show all of the steps in your calculations and be sure to explain what you are doing. Hint, it is not necessary to find the above

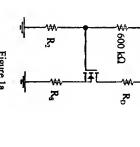


Figure 1a

12 mA

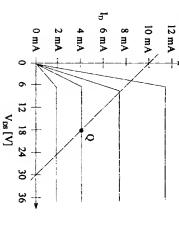
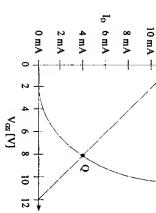


Figure 1b

Figure 1c



EE 321 Final Examination - April 14th 2000 - Page 2

- analog circuits. The differential amplifier is in turn made up of basic BJT amplifier units that are 2. The differential amplifier is the device at the core of the operational amplifier which is used in many appropriately biased. Biasing is commonly accomplished with the use of current sources
- a. Describe briefly how the current source in Figure 2a works
- and have a static forward current gain of 200. b. Find the current sourced by the current source in Figure 2a, assuming that Q3 and Q4 are identical
- dashed box in Figure 2b. Sketch the output characteristic of the current source by itself (this is a sketch The current source in Figure 2a can be modeled effectively by the components shown within the
- of the current, L_O, the versus voltage V_{AB}).

 d. Consider the a.c. signals v_{M1} and v_{M2} to be decomposed into differential, v_D, and common mode, v_C, signals. What are the expressions for v_D and v_C?
- e. Let $v_{\rm al} = 0.1 \sin{(1000t)} + 2.0 \sin{(377t)} [mV]$ and $v_{\rm ad} = 2.01 \sin{(377t)} [mV]$, which might represent a two-wire voltage signal sent from a sensor to a factory control room in a strong 60 Hz environment. Estimate the output voltage signal, $v_{\rm out}$ if the transistors Q1 and Q2 are identical and have a static forward current gain of 150 and $r_{\rm rl} = r_{\rm r2} = 4 k\Omega$.

 f. Estimate the CMRR of this differential amplifier.

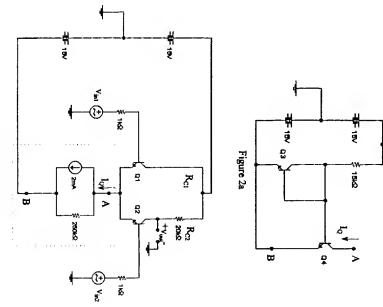


Figure 2b

3. The amplifier circuit shown below in Figure 3 is biased in such a way that both of the Bipolar Junction Transistors are operating in their active regions. Using a D.C. multimeter, the following values were recorded in the laboratory:

 $\begin{array}{c} I_{B1}=80.5~\mu A~~I_{c1}=16.1~mA~~V_{c1}=17.1~V~~V_{E1}=1.6~V\\ I_{E2}=1.51~mA~~I_{c3}=302~mA~~V_{B2}=17.1~V~~V_{E2}=15.2~V\\ \end{array}$ The internal temperature of the transistors can be assumed to be 25 °C.

Is this a good operating point? Why?

b. Sketch the simplified high frequency small signal a.c. model of this amplifier circuit given that $C_{\rm RR1} = C_{\rm RR2} = 19.5$ pF and $C_{\rm RC1} = C_{\rm RC2} = 9.63$ pF. (c) Calculate the approximate high cut-off frequency of the amplifier by completing Table 3.a. d. Calculate the approximate low cut-off frequency of the amplifier by completing Table 3.b.

<u> </u>	Capacitance		C SEE		Capacitance
46 D	Regi	Table 3.a	690 12	203 E	Rφo
173 Hz	Top.		24 MHz	40.2 MHz	ģ
~>	ē.			~>	f _{CH}

Table 3.b

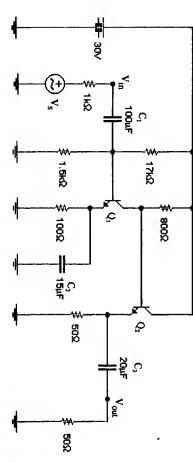


Figure 3

Figure 4b

4. Show that the circuit in Figure 4a can be represented by the block diagram in Figure 4b. That is, find the forward gain G = v₂ / v₁ by considering the portion of the circuit enclosed within the dashed box, and find feedback gain H = v₁ / v₂ by considering that portion of the circuit outside the dashed box. Hint, solve for H in terms of the reactances X₁, X₂ and X₁.

As H is clearly frequency dependent it should not be surprising that for a certain frequency range H < 0, and therefore feedback is no longer negative. For the special case when H is a negative real number (that is the imaginary part of H = 0), and GH > 1 this circuit will begin to oscillate at a unique frequency, ω₆, which can be determined from these two conditions.

For the case where R₁ = 10 kd, R₂ = 100 kd, C₁ = 1 nF = C₂, L = 2 mH and R = 100 Ω, show that

H = -1 and find ω_0 .

^< ۲, ಶ \mathbb{H} Figure 4a ℥ **₹** 5 ال ار ۲ × **⋆ ∨**₂ S

EE 321 Final Examination - April 14th 2000 - Page 6

- 6. For the cascode amplifier circuit in Figure 6 both npn BJT transistors are biased in the active region, and have the following parameters at the quiescent point: $r_{r,l} = 805 \,\Omega \quad r_{r,2} = 813 \,\Omega \quad \beta_l = \beta_2 = 100 \quad C_{HF,l} = C_{RP2} = 0.2 \, pF \quad C_{HF,l} = C_{RP2} = 0.5 \, pF$ a. Sketch the mid-band, small-signal a.c. model for this circuit.

- a. Sketch the mid-band, small-signal a.c. model for this circuit.
 b. Find the midband voltage gain, G_V = V_{out}/V_{ii}.
 c. Find the input resistance seen by the source.
 d. Sketch the high frequency a.c. model for this circuit.
 c. Find the equivalent resistance seen by the capacitance C_{BE2}, and find the corresponding cutoff frequency.

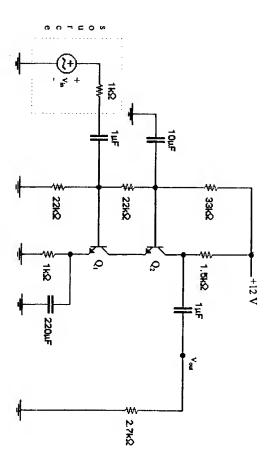
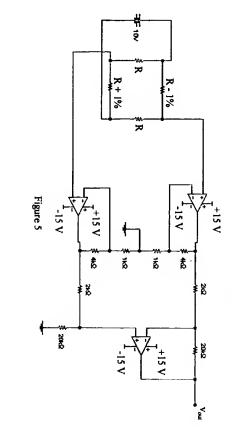


Figure 6

EE 321 Final Examination - April 14th 2000 - Page 5

circuit is converted into an instrumentation amplifier with the two buffer input stages. Assuming this instrumentation amplifier is used to measure a strain gauge bridge such as might be used by a structural engineer on a support beam, calculate the output of the instrumentation amplifier, v_{ost}, as the beam is loaded given that the unstressed resistance of the strain gauge, R = 2 kQ, and the strain gauge resistance changes by -1% on the top and +1% on the bottom of the beam as the beam is loaded. Show all the steps 5. Operational amplifiers are the usual way that differential amplifiers are applied in practice. Even though they are differential amplifier devices themselves, they are often built into higher level linear differential amplifier circuits such as the one shown in Figure 5. In this circuit, a differential amplifier of your calculations. Assume that all of the operational amplifiers are ideal



EE 321 3 Midterm Examination University of Saskatchewan Thursday 18 February, 1999 College of Engineering

Notes, 80 minutes

2 or 3 sheets of notes allowed

A two stage transistor amplifier circuit is shown in Figure 1.

- What type of transistor is used in i) the first stage, and ii) the second stage?
- ೮ ೨ In which configuration is the transistor in i) the first stage, and ii) the second stage connected?
- Find the operating point of each transistor.
- 90 Draw the a.c. small signal model (at midband) for this transistor amplifier circuit. The high frequency model for the BJT, JFET, and MOSFET may be found in Figures 2a),b), and c) respectively.
- MOSFET has a transconductance g_a = 2 mS.

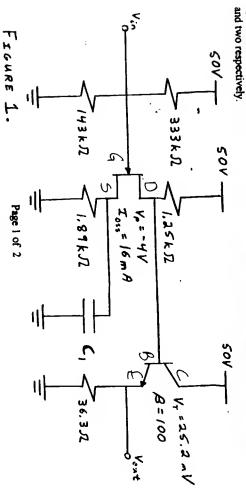
 a) Draw the small signal a.c. model (at midband) for the circuit shown in Figure 3. For the amplifier circuit shown in Figure 3, assume that the n-channel enhancement mode
- 55 Find the voltage gain, $G_V = V_{\bullet \bullet} / V_{\bullet \bullet}$ the input resistance, $R_{\bullet \bullet}$ and the output
- ೨೦ Redraw the small signal model assuming that C2 is removed resistance, R.
- Determine the voltage gain of the circuit in Figure 3 with C_2 removed.

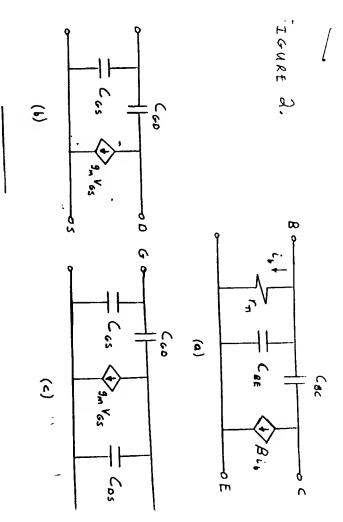
EGURE 3.

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Bonus Question.

For the Darlington cascade in Figure 4, show that when both transistors are active: $I_C = \beta I_B$, where $\beta = (\beta_1 + 1)(\beta_1 + 1) - 1$. β_1 and β_2 are the static current gains for transistors one





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Department of Electrical Engineering Midterm Examination EE 321.3

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Feb. 1998

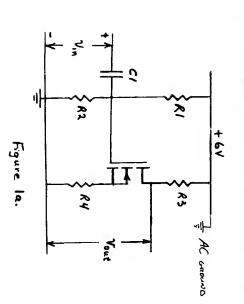
- inst: H. Wood Time: 85 minutes Notes: Clased book; 2 pages of notes may be used
- The transistor circuit shown in Figure 1e is to be used as an amplifier. For the transistor, the threshold voltage is +3 Volts. The output characteristic for the transistor is shown in Figure 1b.

a) Describe the type of the transistor and explein how it works to function as a voltage controlled current

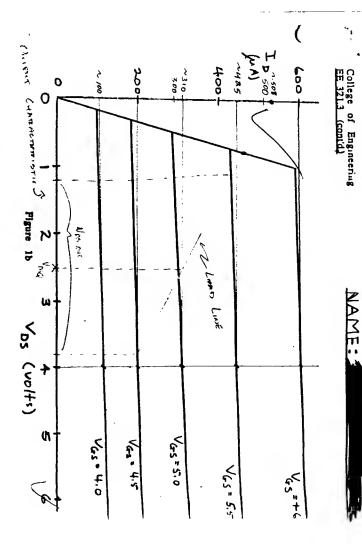
- b) Does Figure 1b accurately represent the behaviour of the transistor in the chmic renge? Why or why not? What use can be made of this type of transistor operating in the chmic range? (Describe an original application)
- c) Draw in the space provided in Figure 1c the transfer characteristic for this transistor for a drain-source potential of +4 volts.
- d For this transistor, evaluate the constant (k) in the expression for drain-source current in the saturation region at maximum current. Describe what physical parameters this constant represents.
- f) For the same values of resistors as in part e), plot the bias line on the appropriete Figure (1b or 1c). What is the effect on the bias line when the value of R4 is changed? e) For values of R1=100k, R2=1100k, R3=10.13k, R4=1.67k, plot the load line on the appropriate Figure (1b or 1c).
- g) What is the operating point for this circuit? (Find graphically or analytically)

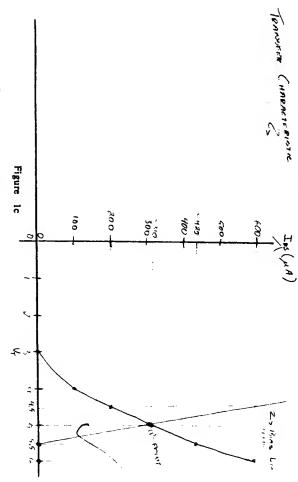
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h) What is e ressonable range for an input AC voltage? What is the corresponding range of output voltages for this input range? Sketch the voltage transfer function for this range of inputs and comment on its shepe.



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University of Saskatchswan Coilege of Engineering BE 321.3. Midtern Examination

Notes:

85 minutes (one question)
2 or 3 sheets of notes silowed

March 1997

A transistor amplifier circuit is shown in Figure 1a. The output characteristic of the transistor is shown in Figure 1b.

a) Briefly describe the type of the transistor and how it works.

b) Draw in the space provided in Figure 1c the transfer characteristic of this transistor for a drain-source potential of 3.0 V.

c) Given that the operating (quiescent) point for this amplifier is point A in Figure 1b, find the value of resistor R1 in Figure 1a.

d) Draw the load line for the amplifier.

e) Draw a small signal equivalent circuit for this amplifier.

f) Calculate the amall signal voitage gain for a signal frequency of 6 kHz.

Note that the coordinates of point A on the output characteristic are (3 V, 306 microA) and the coordinates of point B on the same line are (6 V, 316 microA.).

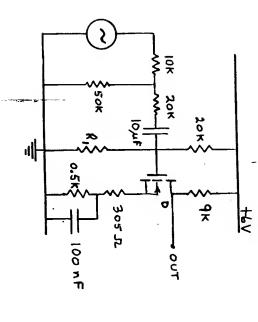
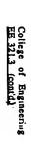
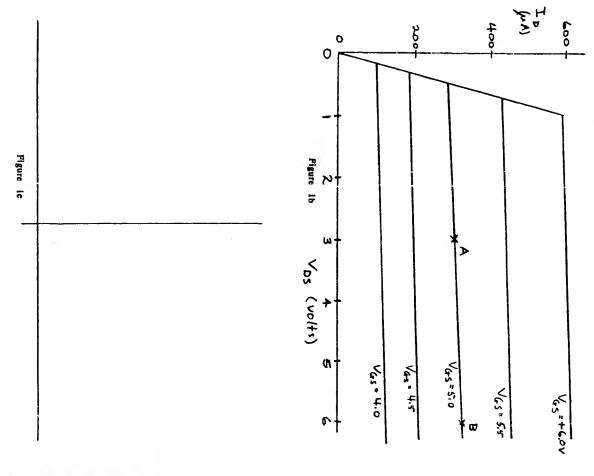


Figure i.







17 April, 1999

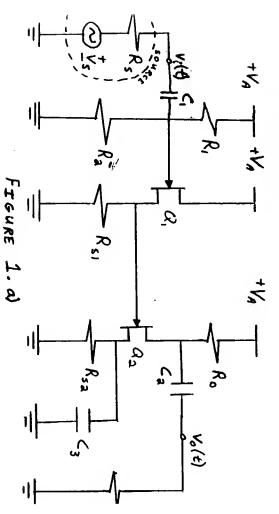
Instructor: J.E. Morelli

Time: 3 hours (09:00 - 12:00).

Notes: All questions have equal value,
Answer any 5 of the 6 questions,
Closed book examination,
Hand held calculators are allowed.,
Justify all your answers.

- In the circuit of Figure 1.a), both transistors are identical. Their high frequency a.c. model is shown in Figure 1.b).
- Knowing that capacitors C₁, C₂ and C₃ behave like short-circuits at mid-band, sketch the mid-band, small-signal a.c. model of the circuit and calculate its voltage gain v_a(t)/v_i(t) as a function of the circuit's components and parameters.
- gain v_a(t)/v_i(t) as a function of the circuit's components and parameters.

 b) Sketch the high frequency a.c. model of the circuit and calculate the equivalent resistance seen by capacitance C_{co} of transistor Q₁ as a function of the circuit's components and parameters.



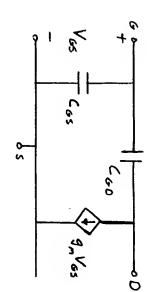


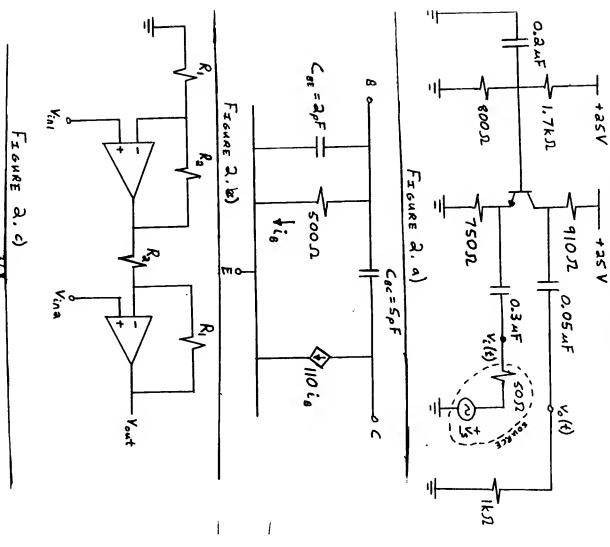
FIGURE 1. 6)

- a) For the common base amplifier circuit shown in Figure 2.a) the transistor is biased
 in the active region. The high frequency a.c. model of the transistor is given in
 Figure 2.b).
- Sketch the simplified high frequency small-signal a.c. model of the circuit.

 Calculate the high cut-off frequency of the amplifier by completing the
- ii) Calculate the high cut-off frequency of the amplifier by completing the following table:

£	1.6 kHz	2 00S	_D	C ₃	
f~ = 13 kHz	1. 7 kHz	1.91 kΩ	fa.	C_2	
	9.7 kHz	54.5 Q	£.	Cı	
Ž.	66 MHZ	480 Ω	fдн	C _{RC}	
÷ = 5	?	?	fсн	Cggg	ì
(2nR _{up} C ₁) ¹ Cut-off frequencies	(2xR _{uj} C ₁) ¹	7	Cut-off frequency affected	Capacitance	

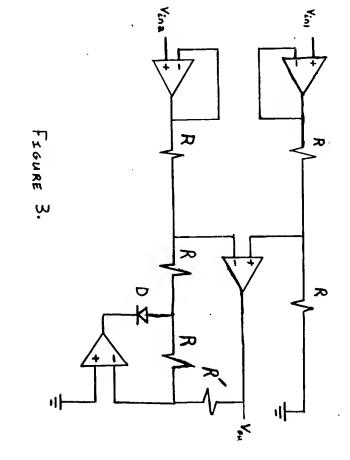
Express v_{est} as a function of v_{el}, v_{el} and the components of the circuit of Figure 2.c). Hint: all feedback is negative.



EE 321 Final Examination 17 April, 1999

Consider the circuit of Figure 3. What condition must v_{ni} and v_{n2} satisfy for the diode be forward biased (i.e. the diode is on)? Hint: when the diode is forward biased, all feedback is negative).

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$$I_C = \beta I_S(e^{\frac{V_{\underline{M}}}{V_T}} - 1) \approx \beta I_S e^{\frac{V_{\underline{M}}}{V_T}}$$

where I_z is the inverse saturation current in the base of the transistor, β is the static current gain (β » 1), and V_T is the thermal voltage (V_T = 25.2 mV at 20 °C).

We first notice that when $V_n > 0$ and $V_{ner} * 1$ volt, then Q_1 and Q_2 are active and the feedback on both operational amplifiers is negative. Moreover, we see from Ohm's Law

$$I_{R2} = \frac{V_{REF} - V_{A}}{R_{2}}$$

- Show that $I_{C2} = \left(\frac{\mathbf{p}}{\mathbf{p}+1}\right)I_{\mathbf{p}2}$. Since $\beta > 1$ conclude that $I_{C2} = \frac{V_{\mathbf{p}2} - V_{\mathbf{p}}}{p}$.
- Show that $L_{c_1} = V_h / R_t$. Use the results of a) and b) to show that:
- ೮೨

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$$V_{BCI} = V_T \ln\left(\frac{V_{in}}{\beta I_S R_i}\right)$$

$$V_{BCI} = V_T \ln\left(\frac{V_{ACT} - V_i}{\beta I_S R_i}\right)$$

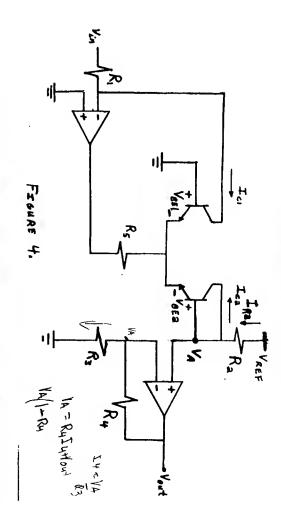
of V_m and the circuit's components and parameters. Show that when $V_{RDT} \gg V_A$, V_{cm} is given by: By noticing that $V_A = V_{BE2} - V_{BE1}$, use the result of c) to express V_A as a function

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c)

$$V_{out} = \frac{-V_T(R_3 + R_4)}{R_3} \ln(\frac{R_2}{R_1} \frac{V_m}{V_{RET}})$$

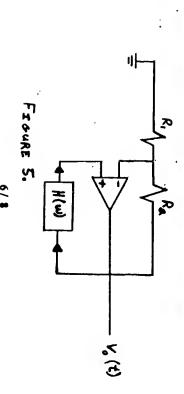
EE 321 Final Examination 17 April, 1999



response is given by: In the circuit of Figure 5, $H(\omega)$ represents a linear time-invariant system whose frequency

$$H(\omega) = \left(\frac{\omega}{4\omega_e}\right)\left(\frac{2 + J(\frac{\omega}{\omega})}{8 + J(\frac{\omega}{\omega_e})^2}\right)$$

determine the condition that R, and R, must satisfy for the circuit to oscillate. where $\omega_s = 2\pi \cdot 10^3$ rad/s. Calculate the frequency at which the circuit can oscillate, and



6. The circuit of Figure 6.a) is an astable oscillator. The relation between $v_{x}(t)$ and $v_{t}(t)$ is given by:

$$v_2(t) = \frac{-1}{RC} \int v_1(t) dt$$

and the relation between $v_i(t)$ and $v_j(t)$ is sketched in Figure 6.b). Express the oscillating frequency of the circuit as a function of the circuit's components and parameters.

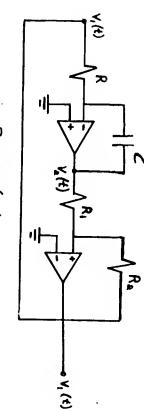
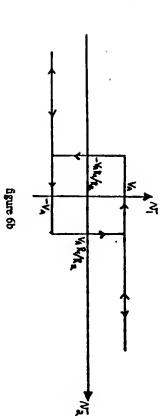


FIGURE 6. 4)



END

HAVE A NICE SUMMER

University of Saskatchewan EE 342

MIDTERM EXAMINATIONS

Time: 1.5 hours

Note: A formula sheet(s) allowed.

and in per unit) seen from the primary side when the transformer hank is connected (a) Ythe secondary of the bank. Determine the Y-equivalent per-phase impedance (in ohms transformer bank. A balanced Y -connected load of 5 ohms per phase is connected across having a leakage reactance of 0.05 per unit, are connected together to form a three-phase Y, (b) Y- Δ , (c) Δ -Y, and (d) Δ - Δ 1. Three identical single-phase transformers, each rated 1.2kV/120 V, 7.2 kVA and

as in the original design? should be the spacing between adjacent conductors in order to obtain the same inductance the line with horizontal spacing (D₁₎ = $2D_{12}$ = $2D_{23}$) The conductors are transposed. What 2. A three-phase line is designed with equilateral spacing of 16 m. It is decided to build

relation of the induced voltage with respect to the power line current. is 150A, find the voltage per kilometre induced in the telephone line. Discuss the phase Spacing between the centres of these conductors is 1.0 m. If the current in the power line a horizontal cross arm 1.8m directly below the power line as shown in the figure below. equivalent equilateral spacing is 3m. A telephone line is also symmetrically supported on cross arm. Spacing of the conductors of the power line is D₁₃ = 2D₁₂ = 2D₂₃, and 3. A three phase 60 Hz overhead power line is symmetrically supported on a horizontal

UNIVERSITY OF SASKATCHEWAN COLLEGE OF ENGINEERING EE 342 - Power Systems I

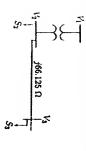
Final Examination

December 2001

Instructor: T. Sidhu

Formula sheet permitted All questions are of equal value

Q1. The one-line diagram of a three-phase power system is as shown in Figure 1. The impedance is $Z = j66.125\Omega$. The load at bus 2 is $S_2 = 184.8$ MW + j6.6 Mvar, and at bus 3 is $S_3 = 0$ MW + j20 Mvar. It is required to hold the voltage at bus 3 at 115.20° kV. Working in per-unit, determine the voltage at buses 2 and 1. transformer reactance is 20 percent on a base of 100 MVA, 23/115 kV and the line 4 21.61 C 36.57 ×



္မ One circuit of a single-phase transmission line is composed of three solid 0.5-cm arrangement of conductors is as shown in Figure 2. Applying the concept of the GMD and GMR, find the inductance of the complete line in milliheary per kilometer. radius wires. The return circuit is composed of two solid 2.5-cm radius wires. The

- 3 A three-phase transposed line is composed of one ACSR 159,000-cmil, 54/19 Lapwing conductor per phase with flat horizontal spacing of 8 m as shown in Figure 3. The GMR of each conductor is 1.515 cm.
- (a) Determine the inductance per phase per kilometer of the line

Department of Electrical Engineering Final Examination - EE 342 Page 2

3 conductor in the bundle? conductors in the bundle is 40 cm. If the line inductance per phase is to be 77 This line is to be replaced by a two-conductor bundle with 8 m spacing measured percent of the inductance in part (a), what would be the GMR of each new from the center of the bundles as shown in Figure 4. The spacing between the 1.324/1/

$$\frac{\overset{\circ}{\smile} - D_{12} = 8 \,\mathrm{m} - \overset{b}{\longleftrightarrow} - D_{23} = 8 \,\mathrm{m} - \overset{c}{\longleftrightarrow}}{-}}{D_{13} = 16 \,\mathrm{m} - \overset{c}{\longleftrightarrow}}$$
Fig. 3

Fig. 4

The ABCD constants of a lossless three-phase, 500-kV transmission line are

$$A = D = 0.86 + j0$$

 $B = 0 + j130.2$

Ξ Obtain the sending end quantities and the voltage regulation when line delivers 1000 MVA at 0.8 lagging power factor at 500 kV. $\% \sim 57.8$

constants become each phase of the transmission line. As a result of this, the compensated ABCD To improve the line performance, series capacitors are installed at both ends in

$$\begin{bmatrix} A' & B' \\ C' & D' \end{bmatrix} = \begin{bmatrix} 1 - 1/2 D X \\ 0 & 1 \end{bmatrix} \begin{bmatrix} A & B \\ C & D \end{bmatrix} \begin{bmatrix} 1 - 1/2 D X \\ 0 & 1 \end{bmatrix} \begin{bmatrix} A & B \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 1 - 1/2 D X \\ 0 & 1 \end{bmatrix}$$

Where X_c is the total reactance of the series capacitor. If X_c = 100 Ω

- (b) Determine the compensated ABCD constants.
- Determine the sending end quantities and the voltage regulation when line delivers 1000 MVA at 0.8 lagging power factor at 500 kV.

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Department of Electrical Engineering Final Examination - EE 342 Page 3

- A three-phase 420-kV, 60-HZ transmission line is 463 km long and may be assumed lossless. The line is energized with 420 kV at the sending end. When the load at the receiving end is removed the voltage at the receiving end is 700 kV, and the per phase sending end current is 646.6 \(\times \) 90°A.
- (a) Find the phase constant β in radians per km and the surge impedance Z_i in Ω.
 (b) Ideal reactors are to be impedance as to be impedance.
- (b) Ideal reactors are to be installed at the receiving end to keep $|V_S| = |V_R| = 420 \, kV$ when load is removed. Determine the reactance per phase and the required three-phase kvar.

UNIVERSITY OF SASKATCHEWAN ELECTRICAL ENGINEERING 304.3 POWER SYSTEMS I

Midterm Examination

Feb. 2001

Time: Instructor: 1.5 hours T.S. Sidhu

Notes:

Formula sheet(s) is allowed.

Answer all questions.

1. The one-line diagram of an unloaded power system is shown in Figure 1. Reactances of the lines are shown in the diagram. The generators and transformers are rated as follows:

Generator 1: 30 MVA, 18kV, X = 20% Generator 2: 20 MVA, 18 kV, X = 15% Generator 3: 20 MVA, 15 kV, X = 20%

Three-phase Y-Y transformers: 20 MVA, 138Y/20Y kV, X=10% Three-phase Y- Δ transformers: 15 MVA, $138Y/13.8\Delta \text{ kV}$, X=10%

- (a) Draw an equivalent circuit representation of this power system using ohmic values and ideal transformers.
- (b) Convert the circuit in part (a) to one where the parameters are expressed in per unit. Use a base value of 100 kVA, 138 kV in the 40 Ω line.

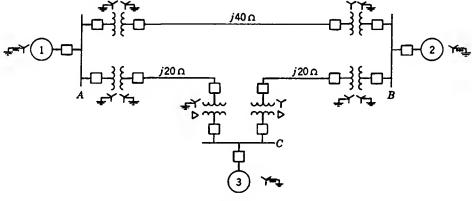


Fig. 1.

- 2. A balanced delta-connected load consisting of pure resistances of 18 ohms per phase is in parallel with a purely resistive balanced wye-connected load of 12 ohms per phase. The combination is connected to a three-phase balanced supply of 346.41 V rms (line-to-line) via a three-phase line having an inductive reactance of j3.0 ohms per phase. Taking the phase voltage V_{an} as reference, determine
- (a) The current, real power, and reactive power drawn from the supply.
- (b) The line-to-neutral and the line-to-line voltage of phase 'a' at the combined load terminals.
- 3. A three-phase 60-Hz line has its conductors arranged in a triangular formation so that two of the distances between centers of the conductors are 10 m and the third distance is 15 m. Each conductor is composed of seven equal strands. The diameter of each strand is 0.5 is a conductor in the conductor of the conductor is composed of seven equal strands.
- (i) Show that the GMR for the conductor is 2.177 times the radius of each strand.
- (ii) Find the inductance of the line in mH/km.
- (iii) It is decided to build the line with horizontal spacing $(D_{13} = 2D_{12} = 2D_{23})$. The line is transposed. What should be the spacing between adjecent conductors in order to obtain the same inductance as in the original design described earlier.

University of Saskatchewan College of Engineering Power Systems I EE 304.3

Final Examination

Instructor: T.S. Sidhu

Time: 3 hrs.

Notes: A formula sheet is allowed.

April 2001

3

Figure 1 are given below. The three-phase power and line-line ratings of the electrical power system shown in

$$\begin{array}{c|c}
C & \xrightarrow{V_g} & \xrightarrow{I_1} & & \\
& & & \\
\end{array}$$
Line
$$\begin{array}{c}
1 & & \\
2 & & \\
\end{array}$$

$$\begin{array}{c}
V_m \\
M
\end{array}$$

Figure 1

Line:	Ξ.	T ₂ :	≓.	ဌ
	43.2 MVA	50 MVA	50 MVA	60 MVA
200 kV	18 kV	200/20 kV	20/200 kV	20 kV
Z = 120 + j2	X = 8% 0.1	X = 10%	X = 10%	X = 9%
200 D 0. 3.1 0.5	a. is	ė	ာ င်	0.15

- <u>a</u> Draw an impedance diagram showing all impedances in per-unit on a 100-MVA base. Choose 20 kV as the voltage base for generator.
- ਭ The motor is drawing 45 MVA, 0.80 power factor lagging at a line-to-line terminal voltage of 18 kV. Determine the terminal voltage and the internal emf of the generator in per-unit and in kV. \mathcal{F}^{MFG} , $\mathcal{E}_{\mathcal{A}}$ - $\mathcal{L}_{\mathcal{Q}}$, $\mathcal{T}_{\mathcal{V}}$ 0, 3.3 0,332-027 60

16 = 6.95£35,3 KV 16 = 0.35958-35,0 Pu

Ņ

conductor per phase with flat horizontal spacing of 8 m as shown in Figure 2. The GMR of each conductor is 1.515 cm. A three-phase transposed line is composed of one ACSR 159,000-cmil, 54/19 Lapwing

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University of Saskatchewan College of Engineering EE 304.3 – Power Systems I Final Examination

- **a** Determine the inductance per phase per kilometer of the line
- each new conductor in the bundle? is to be 77 percent of the inductance in part (a), what would be the GMR of between the conductors in the bundle is 40 cm. If the line inductance per phase measured from the center of the bundles as shown in Figure 3. The spacing This line is to be replaced by a two-conductor bundle with 8 m spacing アーこの とも人不の

$$GM^{0 < 1, 1Ucm}$$

$$GD_{12} = 8 \text{ m} \xrightarrow{b} D_{23} = 8 \text{ m} \xrightarrow{c}$$

$$D_{13} = 16 \text{ m}$$

Figure 2

Figure 3

the line. method of GMD, determine an expression for the capacitance per phase per meter of sharing the balanced load equally. The conductors of the circuits are identical, each having a radius r. Assume that the line is symmetrically transposed. Using the corner of a hexagon as shown in Figure 4. The two circuits are in parallel and are The conductors of a double-circuit three-phase transmission line are placed on the

Figure 4

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University of Saskatchewan College of Engineering EE 304.3 - Power Systems I Final Examination

The ABCD constants of a lossless three-phase, 500-kV transmission line are

$$A = D = 0.86 + j0$$

 $B = 0 + j130.2$
 $C = j0.002$

8 MA 8' HE 7 589 - SA Obtain the sending end quantities and the voltage regulation when line delivers 1000 MVA at 0.8 lagging power factor at 500 kV

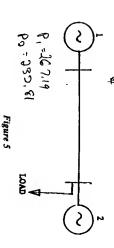
To improve the line performance, series capacitors are installed at both ends in each phase of the transmission line. As a result of this, the compensated ABCD constants become

$$\begin{bmatrix} A & B \\ C & D \end{bmatrix} = \begin{bmatrix} 1 & -\frac{1}{2}JX, \\ 0 & 1 \end{bmatrix} \begin{bmatrix} A & B \\ C & D \end{bmatrix} \begin{bmatrix} 1 & -\frac{1}{2}JX, \\ 0 & 1 \end{bmatrix}$$

where X_c is the total reactance of the series capacitor. If $X_c = 100 \Omega$

- ਭ
- Determine the sending end quantities and the voltage regulation when line delivers 1000 MVA at 0.8 lagging power factor at 500 kV.

Ņ Two plants are interconnected by a transmission line as shown in Figure 5. The only load is located at plant 2. When 350 MW is transmitted from plant 1 to plant 2, power loss in the line is 20 MW. Compute the required generation 500 MW. from plant 1 and plant 2 for economic operation if the load to be supplied is



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University of Saskatchewan College of Engineering EE 304.3 - Power Systems I Final Examination

Assume the incremental fuel costs can be given as follows:

$$\frac{dF_1}{dP_1} = 0.01 P_1 + 9.0 \$ / MWH$$

$$\frac{dF_2}{dP_2} = 0.015 P_2 + 8.0 \$/MWH$$

9 Determine the required generation from plant 1 and plant 2 to supply a load of 500 MW when the transmission losses are not included in "economic scheduling". However, these losses are to be supplied by the plants.

*** The End ***

University of Saskatchewan College of Engineering EE 304 - Power Systems I **Midterm Examination**

February 2000

Time: 1.5 hrs.

All questions are of equal value.

- Consider a single-phase load with an applied voltage $v(t) = 150 \cos(\omega t + 10^{\circ})$ volts and load current $i(t) = 5 \cos(\omega t - 50^{\circ}) A$.
- **a** being absorbed or supplied. Determine the real and reactive power. Show and indicate if each power is
- 3 Find the power factor and specify whether it is leading or lagging.
- Calculate the reactive power supplied by capacitors in parallel with the load that changes the power factor to 0.9 lagging.
- 5 Three identical single-phase transformers, each rated 1.2 kV/120V, 7.2 kVA and from the primary side when the transformer bank is connected as: A balanced Y-connected load of 5Ω per phase is connected across the secondary of the having a leakage reactance of 0.05 per unit, are connected for form a three-phase bank. bank. Determine the Y-equivalent per-phase impedance (in ohms and in per unit) seen
- B Ϋ́
- 9 Y-V
- <u>o</u> Δ-Y, and
- <u>e</u> Δ-Δ
- 'n Ξ A 60 Hz single-phase, two-wire overhead line has solid cylindrical copper configuration with 0.5 m spacing. Calculate in mH/km: conductors with 1.5 cm. diameter. The conductors are arranged in horizontal
- the inductance of each conductor due to internal flux linkages only
- ਭ inductance of each conductor due to both internal and external flux linkages, and
- the total inductance of the line
- (ii) Redo (i) if the diameter of each conductor is:
- increased by 25% to 1.875 cm,
- ਭ decreased by 25% to 1.125 cm, without changing the phase spacing. Compare the results with those of (i).

University of Saskatchewan College of Engineering EE 304.3 Power Systems I

Final Examination

April 2000

Instructor: T.S. Sidhu

Time: 3 hrs.

Notes: Formula sheet(s) is allowed.

Show all the steps used for arriving at the solution. Answer all questions; all questions are of equal value.

B ratings are as follows: The single-line diagram of the power system is shown in Figure 1. Equipment

Generator 1: 750MVA, 18kV, X = 0.2 p.u. 750MVA, 18kV, X = 0.2 p.u. 1500MVA, 20kV, X = 0.2 p.u.

Syn. Motor 3: Generator 2:

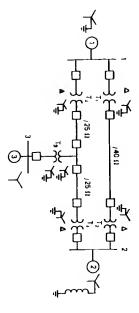
3-phase Δ-Y transformers: 750MVA, 500kV Y/20kVA, X = 0.1 p.u.

 (T_1, T_2, T_3, T_4)

3-phase Y-Y transformers:

1500MVA, 500kV Y/20kVY, X = 0.1 p.u.

Draw the reactance diagram and determine the per unit reactances by using a base of 100MVA and 500kV for the 40-ohm line.

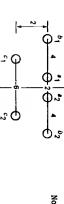


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College of Engineering EE 304.3 - Power Systems I Final Examination University of Saskatchewan

- 3 For the power system in Problem 1(a), the synchronous motor absorbs 1200MW at 0.8 power factor leading with the bus 3 voltage at 18kV. Determine the bus 1 and bus 2 voltages in kV. Assume that generators 1 and 2 deliver equal real powers and equal reactive powers. Assume a balanced three-phase system.
- 'n **E** terms of a (the envelope radius). Find the GMR of each of the unconventional conductors shown in Figure 2 in $\frac{1}{2}$, $\frac{1}{2}$, terms of a (the envelope radius).

3 The radius of each conductor is 0.03 m. Determine the inductance in H/Km of the double-circuit line shown in Figure 3.



Note: -Assume that the line is transposed.

-All distances in

Figure 3

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Page 3 College of Engineering EE 304.3 – Power Systems I Final Examination University of Saskatchewan

B impedance $z = 0.03 + j0.35\Omega/km$ and a shunt admittance $y = j4.4 \times 10^{-6} v/km$. A 500-km 500-kV, 60-Hz three-phase uncompensated line has a series

'n

- Calculate: (i) (ii)
- the exact ABCD parameters of this line
- ਭ Calculate: At full load, the line in Problem 3(a) delivers 1000MW at unity p.f. and at 475 kV. the sending-end voltage,
- (ii) the sending-end current,(iii) the sending-end power factor and(iv) the percentage voltage regulation.
- the percentage voltage regulation.
- compensation. The reactors are removed at full load. installed at both ends of the line during light loads, providing 70% total Recalculate the percentage voltage regulation when identical shunt reactors are
- æ A power system has only two generating plants, and power is being dispatched economically with $P_1 = 140MW$ and $P_2 = 250MW$. The loss coefficients are:

4.

$$B_{11} = 0.10 \times 10^{-2} \text{MW}^{-1}$$

 $B_{12} = -0.01 \times 10^{-2} \text{MW}^{-1}$
 $B_{22} = 0.13 \times 10^{-2} \text{MW}^{-1}$

Find: (a) (b) To raise the total load on the system by IMW will cost an additional \$12 per hour. the penalty factor for plant 1, and

- the additional cost per hour to increase the output of this plant by 1MW
- output of this plant is increased by 1MW? of 12KW for the system, what is the approximate additional cost per hour if the incremental cost of \$12.5 per megawatt hour. If raising the output of plant 2 by A power system is operating on economic load dispatch with a system 100KW (while other outputs are kept constant) results in increased $|I|^2R$ losses

*** The End ***

UNIVERSITY OF SASKATCHEWAN ELECTRICAL ENGINEERING 304.3 POWER SYSTEMS I

Midterm Examination

March 1999

Time: 2 hours
Instructor: T.S. Sidhu
Notes: Formula shee

Formula sheet(s) is allowed.

Answer all questions.

1. A balanced delta-connected load consisting of pure resistances of 18 ohms per phase is in parallel with a purely resistive balanced wye-connected load of 12 ohms per phase as shown in Fig. 1. The combination is connected to a three-phase balanced supply of 346.41 V rms (line-to-line) via a three-phase line having an inductive reactance of j3.0 ohms per phase. Taking the phase voltage V_{an} as reference, determine

- (a) The current, real power, and reactive power drawn from the supply.
- (b) The line-to-neutral and the line-to-line voltage of phase 'a' at the combined load terminals.

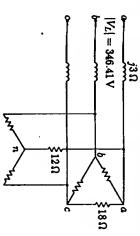
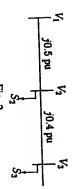


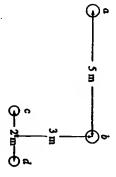
Fig. I.

2.(a) The one-line diagram of a three-phase power system is shown in Fig. 2. Impedances are marked in per-unit on a 100-MVA, 400-kV base. The load at bus 2 is S₂=15.93 MW-j33.4 Mvar, and at bus 3 is S₃=77 MW+j 14 Mvar. It is required to hold the voltage at bus 3 at 400 \(\times 0 \) kV. Working in per unit, determine the voltages at buses 2 and 1 (in per-unit and in kV).



3. A three-phase, 60-Hz transposed transmission line has a flat horizontal configuration as shown in Fig. 3. The line reactance is 0.486 ohms per kilometer. The conductor geometric mean radius is 2.0 cm. Determine the phase spacing D in meters.

4. A 60-Hz single-phase power line and a telephone line are parallel to each other as shown in Fig. 4. The telephone line is symmetrically positioned directly below conductor b. The power line carries an rms current of 226 A. Assume zero current flows in the ungrounded telephone wires. Find the magnitude of the voltage per kilometer induced in the telephone line.



F16. 4

University of Saskatchewan College of Engineering EE 304 - Power Systems I Midterm Examination

February 1998

Instructor:
Time Allowed:

T.S. Sidhu 2 hours

Note:

Answer all questions; formula sheet is allowed.

Marks

- 1. The one-line diagram of a three-phase system is shown in Figure 1. The ratings and impedance values of various elements are also shown in this figure.
 - (a) Draw an equivalent circuit representation of this power system using ideal transformers and ohmic values of impedances.
 - (b) Convert the circuit in part (a) to one where the parameters are expressed in per unit. Use a base of 100 MVA and 15 kV in the motor circuit.
- 2. A balanced three-phase load consisting of an impedance of 30 + j30Ω/phase is connected to a 12.47-kV three-phase, four wire wye-connected source. A power factor correction capacitor bank having an impedance of -j74Ω/phase is connected to the load bus in parallel with the load. The feeder supplying this load has an impedance of 1.5 + j4.0Ω/phase.
 - (a) Line current in phases A B and C of the feeder.
 - (b) Line to neutral voltage of phase A at the load.
 - (c) Active and reactive power consumed at the load bus.
 - (d) Active power loss per phase occurring in the feeder.

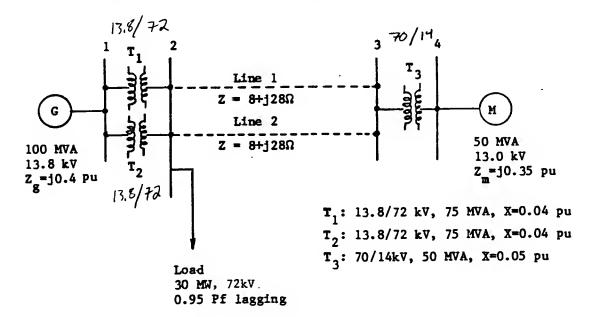


Figure 1

University of Saskatchewan
College of Engineering
EE 304 - Power Systems I
Final Examination

April 1999

Instructor: T.S. Sidhu

Time Allowed: 3 hours

Notes:

All questions are of equal value.

Show all the steps used to arrive at the solution

Formula sheet(s) are allowed.

Q1. The three-phase power and line-line ratings of the electric power system shown in Figure 1 are given below:

$$G_1$$
: 60 MVA, 20 kV, $X = 9\%$

$$_{1}$$
: 50 MVA, 20/200 kV, X = 10%

$$T_2$$
: 50 MVA, 200/20 kV, $X = 10\%$

ine:
$$200 \text{ kV}, Z = 120 + \text{j} 200 \Omega$$

- (a) Draw an impedance diagram showing all impedances in per-unit on a 100-MVA base. Choose 20 kV as the base voltage for generator.
- (b) The motor is drawing 45 MVA, 0.8 power factor lagging at a line-to-line terminal voltage of 18 kV. Determine the terminal voltage and the internal EMF of the generator in per-unit and in kV.

$$\begin{array}{c|c}
C & V_g & T_1 \\
\hline
C & + \\
C & + \\
\hline
C & + \\
\hline$$

rigure 1

S

A three-phase, 60-Hz untransposed transmission line runs in parallel with a telephone line for 20 km. The power line carries a balanced three-phase rms current of $L = 320/0^{\circ}$ A, $L = 320/-120^{\circ}$ A and $L = 320/-240^{\circ}$ A. The line configuration is as shown in Figure 2. Assume zero current flows in the ungrounded telephone wires. Find the magnitude of the voltage induced in the telephone line.

Figure 2

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University of Saskatchewan EE 304 - Final Examination Page 2

Q3. (a) Two single-phase lines are running parallel to each other as shown in Figure 3

The radius of each conductor is r meters. Other distances are as marked in Figure 3 and are in meters. Consider that the charge on conductors of Line 2 is half of that of the conductors of Line 1. Derive an expression for capacitance to neutral for Line 1 in terms of conductor radius (r) and other distances (i.e. D₁, D and D₂).

(b) Using the expression derived in (a), determine the value of capacitance to neutral of Line 1 if

- Q4. A 230-kV, three-phase transmission line has a per phase series impedance of $z = 0.05 + j 0.45 \Omega$ per km and a per phase shunt admittance of $y = j 3.4 \times 10^6$ siemens per km. The line is 80 km long. Using the nominal- π model, determine:
- (a) The transmission line ABCD constants.
- (b) Find the sending-end-voltage and current; voltage regulation, the sending-end-power and the transmission efficiency when line delivers 200 MVA, 0.8 lagging power factor at 220 kV.
- (c) Shunt capacities are installed at the receiving end to improve line performance. Determine the total Mvar and the capacitance per phase of the Y-connected capacitors when sending end voltage is 220 kV. The line delivers 200 MVA, 0.8 lagging power factor at 220 kV.

Q5. The fuel-costs in \$/h for two 800 MW thermal plants are given by:

$$F_1 = 400 + 6.0 P_1 + 0.004 P_1^2$$

 $F_2 = 500 + \beta P_2 + \gamma P_2^2$

where P₁ and P₂ are in MW.

- (a) If the incremental cost of power (λ) is \$8/MWh when the total power demand is 550 MW neglecting losses, determine the optimal generation of each plant.
- (b) If the incremental cost of power (λ) is \$10/MWh when the total power demand is 1300 MW neglecting losses, determine the optimal generation of each plant.
- (c) From the results of (a) and (b) find the value of coefficients β and γ for the fuel-cost of the second plant.

The End

University of Saskatchewan College of Engineering EE 304 - Power Systems I **Final Examination**

April 1998

Instructor: T.S. Sidhu

Time Allowed: 3 hours

Formula sheet(s) allowed.

Answer all questions; all questions are of equal value. Show all the steps used to arrive at the solution.

sections of transmission lines are shown in the diagram. The generators and transformers The one-line diagram of a three-phase system is shown in Figure 1. Reactances of the two are rated as follows:

Generator 1: 15 MVA, 13.8 kV, X = 0.15 p.u

Generator 2: 30 MVA, 15 kV, X = 0.2 p.u.

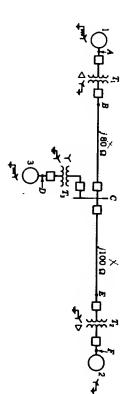
Generator 3: 20 MVA, 20 kV, X = 0.2 p.u.

\$\fransformer 1: 20 MVA, 13.8/220kV, Delta-Wye, X = 10%

Transformer 2: Single-phase units each rated 10 MVA, 18/127 kV, X = 10%

XTransformer 3: 30 MVA, 20/220 kV, Wye-Wye, X = 10%

Draw the circuit diagram showing impedances in per unit and marked with letters to indicate points corresponding the one-line diagram. Choose a base of 100 MVA, 13.8 kV in the circuit of Generator 1.



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*University of Saskaichewan EE 304 - Final Examination Page 2

Calculate the inductance and capacitance of the double-circuit, bundled three-phase line shown in Figure 2. All distances in the figure are marked in meters. Neglect the effect of ground. Consider that the radius of each conductor in the bundle is 0.015 m.

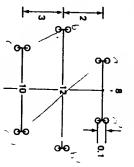


Figure 2

 \sim The AB&D constants of a three-phase transmission line are:

$$A = 0.9 / 0.95^{\circ}$$

 $B = 100.0 / 80^{\circ} Ω$ D = A

The magnitudes of the sending end and receiving end voltages are 500 and 490 kV respectively. The real power being received is 1000 MW.

- \mathbf{z} Calculate the C constant of the line.
- ક Calculate the phase angle displacement between the voltages at the sending end and receiving end of the line.
- S How much complex power will the line deliver if the phase displacement between the sending- and receiving-end voltages is 35°?
- 8 Calculate the maximum power that can be delivered by the line



A power system has two generating units operating on economic dispatch. The operating costs of these units are given by

$$F_1 = \begin{cases} 2P_1 + 0.02P_1^2 (\$/hr) \text{ for } 0 < P_1 \le 100 \text{ MW} \\ 6P_1 (\$/hr) \text{ for } P_1 > 100 \text{ MW} \end{cases}$$

$$F_2 = 0.03 P_2^2 (\$/hr)$$

where P_1 and P_2 are in MW.



Determine the power output of each unit that minimizes the total operating cost as total required power (P_R) varies from 200 to 700 MW.

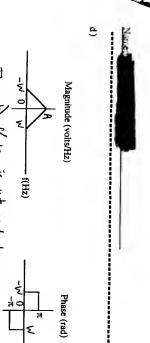
Neglect transmission losses.

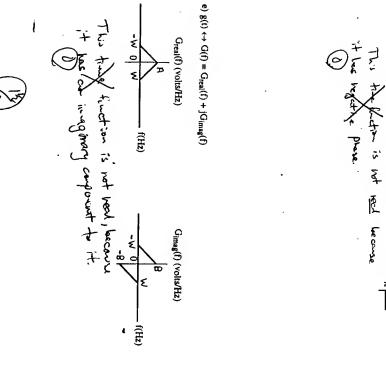


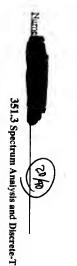
If the total transmission losses for the system are given by

$$P_L = 2 \times 10^4 P_1^2 + 1 \times 10^4 P_2^2$$
 (MW).

Perform economic dispatch calculations for a total required power of 290 MW.







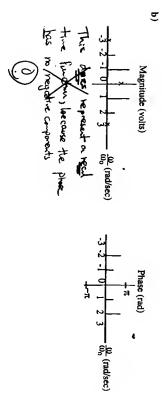
351.3 Spectrum Analysis and Discrete-Time Systems

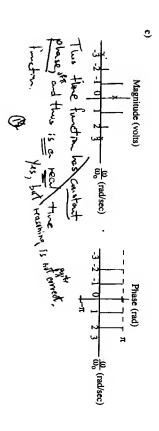
Term Test, October 22/02, Time: 2 hours; Closed Book

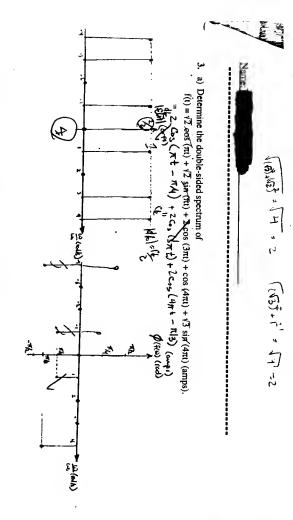
All questions are of equal value but not necessarily of equal difficulty. Please label and scale your graphs and do not forget units. Finally explain and justify your solutions.

1. Which double-sided spectrum represents a real time function. Marks are given only for your

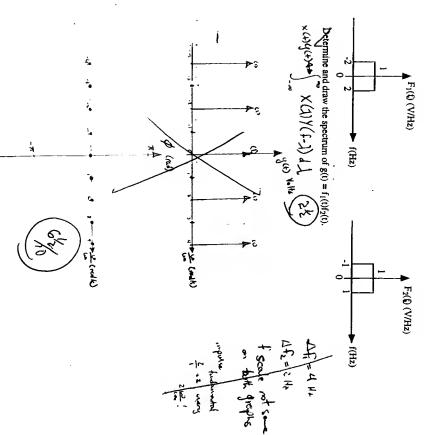
positive on the other, which edds an imaginary down Magnitude (volts) become, the phase imporement is not represent a tred time - ω (rad/sec) Phase (rad)



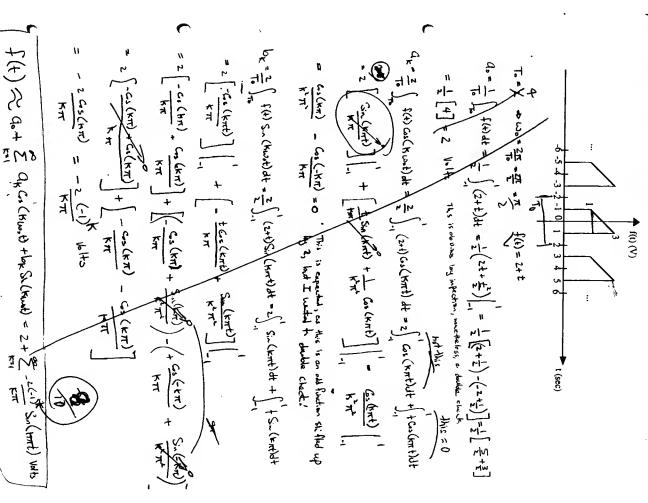




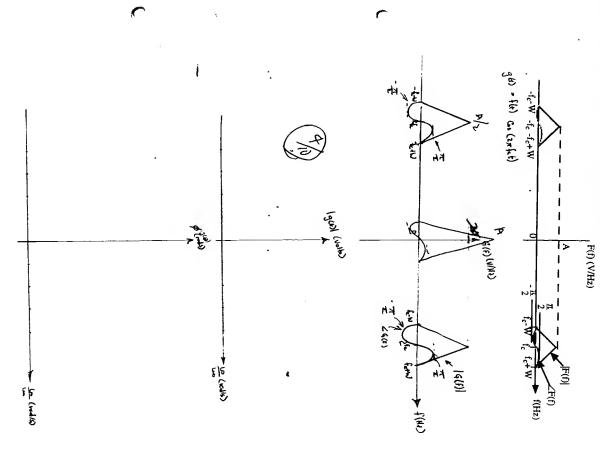
b) Consider two time functions $f_1(t)$, $f_2(t)$ with Fourier transforms $F_1(f)$, $F_2(f)$ shown below.



Determine the Fourier series, trigonometric form, of the periodic function below. Simplify the coefficients as much as possible.



4. Given the amplitude density spectrum of f(t) shown below determine the spectrum of $g(t) = f(t) \cos{(2\pi f_c t)}$ and draw a neatly labelled graph of G(t)



1

Fourier coefficients of f1(t)

$$a_0 = \frac{2(2)}{4} = 1(v)$$

$$a_k = \frac{2}{T_0} \int_{T_0} f(t) \cos{(k\omega_0 t)} dt = \frac{2}{4} \int_{-1}^1 2 \cos{(k\omega_0 t)} dt = 2 \int_0^1 \cos{(k\omega_0 t)} = \frac{2 \sin{(k\omega_0 t)}}{k\omega_0} \left[\frac{1}{2} \cos{(k\omega_0 t)} + \frac{1}{2} \sin{(k\omega_0 t)} \right]^2$$

 $=\frac{2}{\pi k\omega_0}\sin(k\omega_0)$

$$\left(\omega_0 = \frac{2\pi}{4} = \frac{\pi}{2}\right)$$

$$a_k = \begin{cases} \frac{4}{\pi k} & k = 1, 5, 9, ... \\ 0 & k = 2, 4, 6, ... (k \text{ even}) \end{cases}$$
$$\begin{cases} -\frac{4}{\pi k} & k = 3, 7, 11, ... \end{cases}$$

Fourier coefficients of f2(t)

$$b_k = \frac{2}{4} \int_{-1}^{1} t \sin(k\omega_0 t) dt = \frac{\cos(\frac{k\pi}{2})}{\frac{k\omega_0}{2}} + \frac{\sin(\frac{k\pi}{2})}{\frac{k^2\omega_0^2}{2}}$$
$$= 0 \text{ k odd} \quad = 0 \text{ k even}$$

$$b_{k} = \begin{cases} \frac{1}{k\omega_{0}} & k=2,6,10,...\\ -\frac{1}{k\omega_{0}} & k=4,8,12,...\\ \frac{1}{k^{2}\omega_{0}^{2}} & k=1,5,9,...\\ -\frac{1}{k^{2}\omega_{0}^{2}} & k=3,7,11,... \end{cases}$$

$$f(t) = a_0 + \sum_{k=1}^{\infty} \left[a_k \cos\left(k\omega_0 t\right) + b_k \ \sin\left(k\omega_0 t\right) \right] a_0, \, a_k, \, b_k, \, \omega_0 \, as \, found \, above.$$

One could approach the problem directly by observing that in the interval $t \in [-1, 1]$, f(t) = t + 2

351 - TERM TEST - Solution

- If the magnitude spectrum is even and the phase odd then the spectrum represents a real time
- a) magnitude even; phase odd ⇒ real time function
 b) magnitude even; phase even ⇒ complex time function
- c) magnitude even; though phase looks even this is a special case, since $\pi = -\pi$ phase is odd
- d) magnitude even; phase odd ⇒ real time function
- here the spectrum is given in 'cartesian' form. However either argue that

of Great(f) and Gimag(f) $|G(f)| = \sqrt{G_{real}^2(f) + G_{Imag}^2(f)}$ is even and $\angle G(f) = tan^{-1} \left(\frac{G_{Imag}(f)}{G_{real}(f)}\right)$ is odd from the graphs

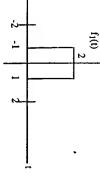
or note that
$$G(f) = \int_{-\infty}^{\infty} g(t) e^{-j2\pi ft} dt = \int_{-\infty}^{\infty} g(t) \cos(2\pi ft) dt - j \int_{-\infty}^{\infty} g(t) \sin(2\pi ft) dt$$

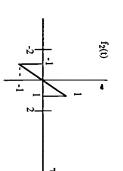
$$\Rightarrow G_{real}(f) = \int_{-\infty}^{\infty} g(t)\cos(2\pi ft) dt - \text{an even function in f when } g(t) \text{ is real.}$$

$$G_{imag}(f) = \int_{-\infty} g(t) \sin(2\pi f t) dt - an odd-function in f when g(t) is real.$$

Therefore g(t) is real because Great(f) is even and Gimag(f) is odd.

2. Express f(t) as a sum of two functions f₁(t), f₂(t) as shown below



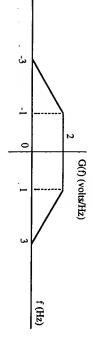


 $f_2(t)$ is odd \Rightarrow only b_k coefficients present $f_1(t)$ is even \Rightarrow only a_k coefficients present

b) Spectrum of g(t) is the convolution of the two spectra, $F_1(f)$, $F_2(f)$,

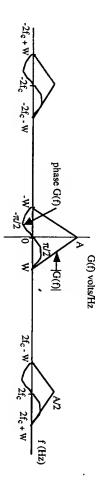
$$i.e.,G(f) = \int_{-\pi}^{\pi} F_1(\lambda) F_2(f \cdot \lambda) d\lambda = \int_{-\pi}^{\pi} F_1(f \cdot \lambda) F_2(\lambda) d\lambda$$

Doing the convolution graphically gives:



4. Multiplying f(t) by $\cos(2\pi f_c t)$ shifts the spectrum up by f_c , down by f_c , and divides it by 2.

Therefore
$$G(f) = \frac{F(f - f_c) + F(f + f_c)}{2}$$
.



integrand in the 1st integral is odd, therefore the integral equals zero. So $a_k = \frac{2}{T_0} \int_{-1}^{1} 2\cos(k\omega_0 t) dt$

(as above). Similarly
$$b_k = \frac{2}{T_0} \int_{-1}^1 t \sin(k\omega_0 t) dt + \frac{2}{T_0} \int_{-1}^1 2 \sin(k\omega_0 t) dt$$
. Now the 2nd integral

disappears and $b_k = \frac{2}{T_0} \int_{-1}^{1} t \sin(k\omega_0 t) dt$ (again as before).

(ALL ROADS LEAD TO ROME)

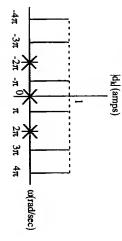
3. a) $f(t) = 2 \cos(\pi t \cdot 45^0) + 2 \cos(3\pi t) + 2 \cos(4\pi t \cdot 60^0)$ (amps)

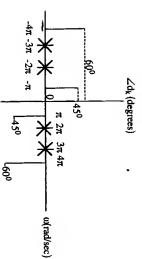
By inspection $\omega_0 = \pi$ rad/sec. Have 3rd and 4th harmonics.

$$c_0 = 0$$
; $c_1 = 2$; $c_2 = 0$; $c_3 = 2$; $c_4 = 2$

 $\phi_1 = -45^{\circ}; \ \phi_2 = 0^{\circ}; \ \phi_3 = 0^{\circ}; \ \phi_4 = -60^{\circ}$

$$|d_k| = \frac{c_k}{2}; \ \angle d_k = \phi_k$$





University of Saskatchewan, Electrical Engineering EE 351.3 Spectrum Analysis and Discrete Time Systems Midtern Examination October 30, 2001

Note: 2 hour open-book exam. Instructor: K. Takaya

 (30) Two rectangular waves shown in Fig.1 are fsod(t) and fsod(t) defined respectively by

$$f_{SOM}(t) = \begin{cases} -1 & \text{if } -\pi \le t < -\frac{\pi}{2} \\ 1 & \text{if } -\frac{\pi}{2} \le t \le +\frac{\pi}{2} \\ -1 & \text{if } +\frac{\pi}{2} < t \le +\pi. \end{cases}$$

$$f_{SOM}(t) = \begin{cases} -1 & \text{if } -\pi \le t < -\frac{\pi}{2} \\ 1 & \text{if } -\frac{\pi}{2} \le t \le +\frac{\pi}{2} \\ -1 & \text{if } +\frac{\pi}{2} < t \le +\pi. \end{cases}$$

The two waveforms are similar but different only in their duty cycle (or on-time). Obtain only a_n (No need to find b_n) as both of the waveforms are symmetric. Then, compare the obtained a_n for 50% and that for 20% of the duty cycle, to find which waveform has greater high frequency components. Make your statements based on your calculated a_n .

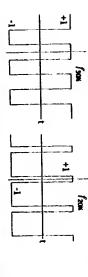


Fig. 1 Rectangular waveform of 50% duty cycle (left) and 20% (right).

(30) The distortion factor η indicates how much a given waveform
is distorted from the sinusoidal wave of the same frequency. It is
defined by using the exponential Fourier series D_n and D_{-n}.

$$\eta = \frac{\text{Total Power} - |D_0|^2 - |D_1|^2 - |D_{-1}|^2}{|D_1|^2 + |D_{-1}|^2}$$

or by using the compact Fourier series C_n , Total Power – $|C_0|^2 - |C_1|^2$

$$\eta = \frac{\text{Total Power} - |C_0|^2 - |C_1|^2}{|C_1|^2}.$$

Calculate the distortion factor η of the clipped sine wave, given by

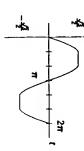


Fig. 2 Clipped sine wave.

3. (20) First, sketch the graph of

$$f(t) = \begin{cases} e^{-t} & \text{if } t \ge 0 \\ -e^{t} & \text{if } t < 0 \end{cases}$$

Then, obtain the Fourier transform of f(t) defined by

$$F(\omega) = \int_{-\infty}^{\infty} f(t)e^{-j\omega t}dt$$

Then, sketch only the imaginary part of $F(\omega)$

2. Why do we use negative frequedes to represent the spectrum of a real signal such as cos ω ?

3. What are the diferences between the Fourier Series and the Fourier Transform?

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- The END-

University of Saskatchewan, Electrical Engineering EE 351.3 Spectrum Analysis and Discrete Time Systems Final Examination, December 13, 2001

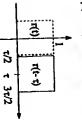
Note: 3 hour open-book exam. Marks for each question are as indicated. Instructor: K. Takaya

1. (10) A rectangular function r(t) is defined as

$$r(t) = \begin{cases} 1 & \text{if } -\frac{7}{2} < t < \frac{7}{2} \\ 0 & \text{othrwise} \end{cases}$$

Obtain the Fourier transform of $r(t-\tau)$ using the time-shifting property of the Fourier transform.

$$f(t-\tau) \Longleftrightarrow F(\omega)e^{-j\omega\tau}$$

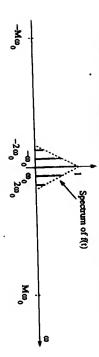


2. (10) The carrier suppressed AM (Amplitande Modulation) of a periodic signal f(t) having one cycle interval of T, i.e. $\omega_0 = \frac{2\pi}{T}$, modulated by a carrier frequency ω_c is given by

$$f_{AM}(t) = 2f(t)\cos\omega_c t$$
.

Where, $\omega_c = \omega_0 \times M$ is much greater than ω_0 . M is an integer.

- 1. Assuming that the exponential Fourier series of f(t) are already calculated as D_n and D_{-n} , express the exponential Fourier series of $f_{AM}(t)$ in terms of D_n and D_{-n} .
- 2. Sketch the spectrum of $f_{AM}(t)$ assuming that the spectrum of f(t), i.e. D_n and D_{-n} , is given as illustrated in the figure below.



- (15) Give brief explanations about "the sampling theorem" and "aliasing" (or spectrum folding) within 200 words.
- 4. (10) Find the z-transform of

$$0.5^{k+1}u[k-1]+0.5^{k-1}u[k]$$

5. (10) Find the inverse z-transform of

$$\frac{2z^2 + 0.25}{(z+1)(z-0.5)^2}$$

6. (10) Obtain the convolution sum between two functions f[k] and g[k],

$$c[k] = \sum_{m=0}^{k} f[m]g[k-m] = \sum_{m=0}^{k} g[m]f[k-m]$$

for $f[k] = (-1)^k u[k]$ and $g[k] = (0.2)^k u[k]$.

7. (15) Solve the following difference equation by using the z-Transform.

$$y[k] - 1.3y[k - 1] + 0.4y[k - 2] = f[k]$$

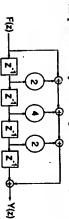
where,
$$f[k] = u[k-1]$$
, and $y[-1] = 1, y[-2] = 0$.

 (10) Draw a diagram that illustrates the structure of a discrete transfer function given by

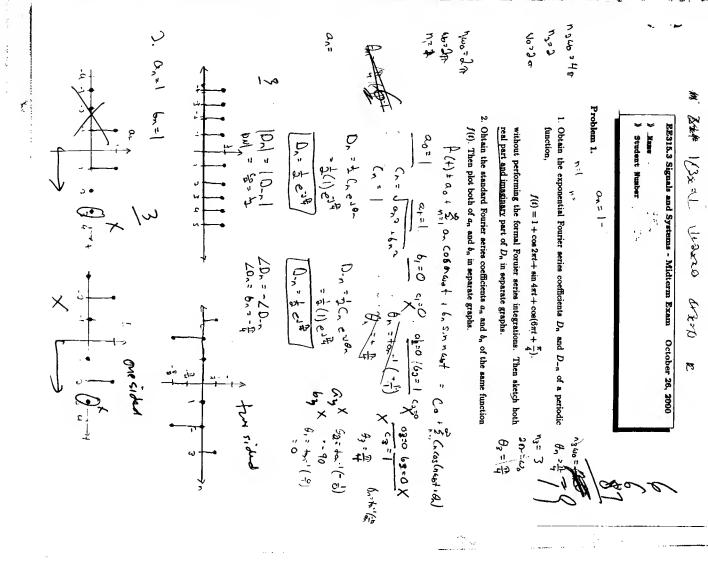
$$G[z] = \frac{1 - z^{-1}}{(1 - 0.5z^{-1})(1 - 0.8e^{-j\frac{\pi}{2}}z^{-1})(1 - 0.8\pi e^{-j\frac{\pi}{2}}z^{-1})}$$

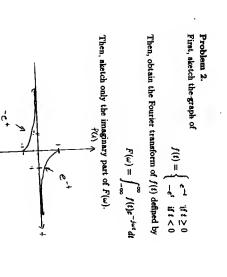
Three delay elements, i.e. z^{-1} , connected in series must be used in the diagram.

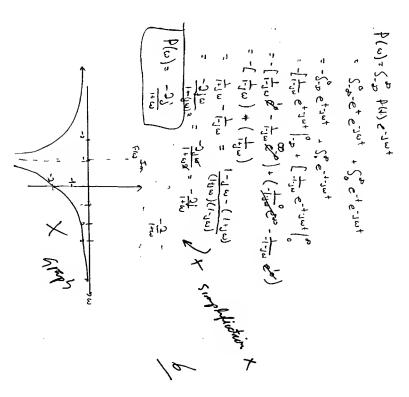
9. (10) Obtain the amplitude and phase response of the system shown below.



- The END-







The Fourier series of a sawtooth wave having one cycle period of $T=2\pi$,

$$f(t) = \frac{t}{\pi} \quad \text{where, } -\pi < t \le +\pi$$

is given by

$$D_0 = 0$$
, $D_n = \frac{(-1)^{n-1}}{j2n}$ and $D_{-n} = -\frac{(-1)^{n-1}}{j2n}$

Calculate the distortion factor η of this sawtooth wave according to the definition,

$$\eta = \frac{\text{Total power} - DC \text{ power} - |D_1|^2 - |D_{-1}|^2}{|D_1|^2 + |D_{-1}|^2}$$

Total Power + 5, p(+) 2+ 673 (73-(73) 673 (203) (273)(3) (73-C-23) 킹15 각 구 Oc power = 0,0 15/2 - 1-10 -1-1 0

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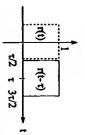
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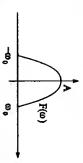
1. A rectangular function r(t) is defined as Note: 3 hour open-book exam. All questions are of equal value. Instructor: K. Takaya University of Saskatchewan, Electrical Engineering EE 315.3 Signals and Systems (I), Final Examination December 21, 2000 $r(t) = \begin{cases} 1 & \text{if } -\frac{1}{2} < t < \frac{\tau}{2} \\ 0 & \text{othrwise} \end{cases}$

property of the Fourier transform, Obtain the Fourier transform of $r(t-\tau)$ using the time-shifting

 $f(t-\tau) \Longleftrightarrow F(\omega)e^{-J\omega\tau}$



'n Determine the Nyquist sampling rate of a signal represented by its Fourier transform $F(\omega)$ as shown below. Where, $\omega_0=2\pi\times1000.$



If the time signal f(t) corresponding to $F(\omega)$ is sampled at a sampling rate exactly equal to the Nyquist sampling rate, what question spectrum? Sketch the spectrum after sampling, to answer the is the sampling frequency? how does this sampling affect the

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3. Find the zero input response of the difference equation,

$$y[k+2] - 0.25y[k] = f[k+2]$$

for a set of internal conditions y[-2] = -4 and y[-1] = -6. The z-transform is not allowed in this problem.

4. Find the z-transform of

$$0.5^{k+1}u[k-1] + 0.5^{k-1}u[k].$$

5. Find the inverse z-transform of

$$\frac{z(-5z+22)}{(z+1)(z-0.8)^2}.$$

6. Draw the block diagram of a discrete transfer function given by

$$G[z] = \frac{1 - z^{-1}}{(1 - 0.6z^{-1})(1 - 0.7z^{-1})(1 - 0.8z^{-1})}.$$

7. Obtain the convolution sum,

$$c[k] = \sum_{m=0}^{k} f[m]g[k-m]$$

for f[k] = u[k] and $g[k] = (0.2)^k u[k]$.

8. Explain what "aliasing" (or spectrum folding) is briefly within 100 words.

- The E N D -

Department of Electrical Engineering Midterm Examination EE 315.3

H. Wood

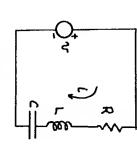
Notes: Formula sheet allowed

Marks: As shown; Do all three questions.

- For the circuit shown in Figure 1, 8 determine the differential equation that relates the current signal i(t) to the input voltage signal v(t). Show your work.
- For the values L=1H, R=5Q, C= 1/6 F, what is the D operator form for the zeroinput differential equation.
- Assuming i(t) has a solution of the form

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٩ t=0, and di/dt = -2 at t=0?



i(t) = c exp(-\lambda t), what is the characteristic zero-input solution if the current is zero at time

What is the unit impulse response h(t) of this system?

2. When a unit impulse signal $\delta(t)$ is applied to a system A, the response of the system is

$$y(t) = 3 \exp(-2t) u(t). \ge h(4)$$

- → a) Sketch this output signal giving care to the labelling of the axes
 b) Sketch an input signal given by
- ၉၀ Sketch the expected output of the system A when the input x(t) is applied Calculate the output of the system when x(t) is input, using convolution.

x(t) = 2(u(t-1) - u(t-3))

ı Fourier hypothesized that a periodic waveform f(t) could be represented by an infinite sum of harmonically related components,

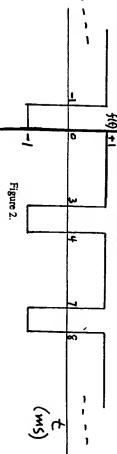
$$f(t) = a_0 + \sum_{d, a_1} (a_{a_1} \cos n w_{d_1} + b_{a_1} \sin n w_{d_1})$$

$$n=1$$
a) Describe how the coefficients a and became be described and the coefficients of any bedden any bedd

a) Describe how the coefficients an and bn can be determined, and give a mathematical expression for an and bn following from your description.

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- b) Show how the coefficients a, and b, can be evaluated for n=0,1,2 if the waveform f(t) is as shown in Figure 2.
- C Evaluate a, and b, for the waveform shown in Figure 2.



Electrical Engineering EE 315.3 Final Examination University of Saskatchewan

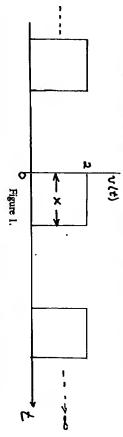
Inst'r: H. Wood Time: 3 hours

October 1999

December 1999

Notes: Closed Book; a few pages of notes are allowed Marks: Do all 5 questions; marks as shown.

- A data communications engineer has the task of determining the on/off time ratio of the periodic where a, and b, are the coefficients of the nth frequency component, and T is the period of the 0.25, 1/3, 0.5, or 2/3, and has assumed that the signal power is proportional to $a_n^2 + b_n^2$. components beyond the fundamental frequency in order to minimize interference with other fundamental component. Also, the analysis was limited to n < 5. signals in the customer's system. The engineer, however, can only select values of $x/\Gamma =$ The customer wants to minimize the fraction of the AC signal power contained in the harmonic signal shown in Figure 1, in order to meet certain specifications given by the customer.
- (a) What value of x/I best satisfies the customer requirement? Show your reasoning and calculations
- What is the DC signal component for each of the x/I values? Does this factor play a role in the efficiency of the communications system?
- ೦ If x/T could be any value, describe how you could determine the best possible value to meet need to calculate the actual optimum value, but for a bonus, you may if you wish. the customer requirement, within the same assumptions given above. Note::You do NOT

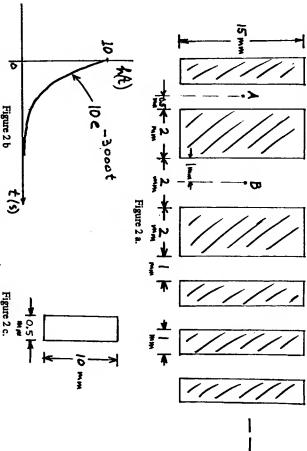


product can be identified from this coded pattern. The objective is to scan the bar code with a designed so that there is a unique pattern of wide and narrow strips, and spacings, so that any An engineer has the task of designing a laser scanning system for reading the bar codes printed Assume for this question that the strips are reflective and the spaces are not; the full width of on many products in stores. Part of a typical bar code is shown in Figure 2a. The bar code is laser beam and detect the pattern from the reflected light.

the bar code is 3.0 cm

ھ The engineer first decides to use a laser beam in the shape of a very small circular dot therefore very low and a large integration time was needed in the detector to produce any (<0.00001m diameter). Unfortunately, the amount of light reflected to the detector was significant output voltage. The measured impulse response of the detector was as shown in

EE315.3 cont'd, pg 2 of 3.



(a) Determine the output response of the detector as the laser dot moves from point A to point B in 1.0 ms in a straight line, at a uniform speed.

ii) If the detector output must fall by at least one-half of its maximum output during the narrowest spacing between strips in order to separate bars from spaces, what is the shortest time that the laser beam can take to scan the entire bar?

for the engineer then decides to use a larger laser source, with a beam in the shape of a rectangle as shown in Figure 2c. Alignment of the beam and the bar code strips is then an issue, although the larger laser means that a much faster detector can be used. In fact, the detector's impulse response is now "infinitely narrow".

i) What is the detector output now as the rectangular beam shape scans from A to B when the rectangle shape of the beam and the strips are parallel?
ii) If the har code becomes inclined by 15 degrees to the laser beam rectangle what is the

of done

 ii) If the bar code becomes inclined by 15 degrees to the laser beam rectangle, what is the detector output as the beam scans from A to B?

iii) Are these two cases, b i) and b ii) true examples of convolution? Why or why not?

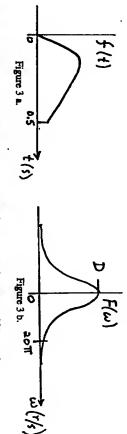
3. An engineer is designing a pulsed radar system to measure the distance to remote objects. The radar system transmits a pure sinusoidal RF signal at a frequency of 3.0 GHz (ie, 3.0 x 10° Hz) that is gated on and off to produce a finite duration pulse of RF energy. This pulse then travels through space to a stationary object and is reflected back to the radar antenna. The radar power output during transmission is 1.0 MW into a load of 100 Ohms.

EE315.3 cont'd, pg 3 of 3.

- a) If only the sinusoidal signal was being transmitted (continuously, without gating), what would the frequency spectrum be? Draw the time signal <u>and</u> plot the spectrum and calculate its amplitude and position.
- b) When the sinusoidal signal is gated on and off once with a gate that is 1.0 microseconds long, what is the resulting spectrum? (Assume the full width of the gate is 1.0 microseconds with the gate centered on zero in the time plot) Draw the time signal and plot the spectrum carefully and accurately in the frequency domain, giving all necessary labels () () ()
- c) If the engineer needs to design a receiver to measure the reflected signal, what should the center frequency of the receiver be and what should its bandwidth be to capture all of the reflected signal within the frequency region to the "first minimum" of the spectrum? (Hint—use only positive components of frequency for this calculation).

An engineer is trying to decide whether to use analog or digital electronic techniques to design a data communications system. Discuss the advantages and disadvantages of the digital method compared to the analog method.

5. The time limited signal shown in Figure 3a has a spectrum as shown in Figure 3b.



 a) Sketch the spectrum after the time signal has been sampled at a rate of 20 samples per second.

- b) Will there be much overlap in the spectrum at the above sampling rate? What would happen to the overlap if the sampling rate was reduced to 10 samples per second? Why?
- to the overlap if the sampling rate was reduced to 10 samples per second? Why?

 c) If the spectrum obtained in part a) above is itself sampled so that the spectral values can be stored in a digital computer, what is the effect on the time signal? Sketch the resulting time signal.
- d) What is the frequency spacing in the sampled spectrum so that there is 50% padding between successive time signals? What is the maximum allowable spacing between frequency samples so there will be no overlap in time.?
- e) How are the samples of the time signal and the samples of the frequency spectrum related to each other mathematically? Do not just give the equations, but explain what they mean in words.
- f) How does the FFT derive from the relationship defined in e)?

back to with

University of Saskatchewan, Electrical Engineering EE 315.3 Signals and Systems (I), Midterm Examination October 27, 1998

Note: 2 hour open-book exam. Instructor: K. Takaya

 \mathcal{X} . (20) A linear system is described by the differential equation,

$$(D^2 + 2D + 5)y(t) = (D + 4)f(t).$$

X. Write the characteristic equation, characteristic roots and characteristic modes of this system.

2. Obtain the zero-input response of this system for the initial (x,y) = 1 and (y,y) = 1.

3. Find the unit impulse response of this system, i.e. find y(t) for $f(t) = \delta(t)$.

2. (20) By using the convolution integral.

obtain the convolution of the causal functions g(t) and f(t) shown in Fig. 1. Where,

 $y(t) = \int_0^t f(t-\tau)g(\tau)d\tau = \int_0^t f(\tau)g(t-\tau)d\tau$

$$f(t) = \begin{cases} 0 & \text{if } t < 0 \\ t & \text{if } 0 \le t < 1 \\ 1 & \text{if } 1 \le t \end{cases}$$

and

$$g(t) = e^{-t}u(t).$$



Fig. 1 Functions f(t) and f(t) for Question 2.

3. (20) Two rectangular waves shown in Fig.2 are $f_{50\%}(t)$ and $f_{20\%}(t)$ defined respectively by

$$f_{50\%}(t) = \begin{cases} -1 & \text{if } -\pi \le t < -\frac{\pi}{2} \\ 1 & \text{if } -\frac{\pi}{2} \le t \le +\frac{\pi}{2} \end{cases}$$
$$-1 & \text{if } +\frac{\pi}{2} < t \le +\pi.$$
$$f_{20\%}(t) = \begin{cases} -1 & \text{if } -\pi \le t < -\frac{\pi}{5} \\ 1 & \text{if } -\frac{\pi}{2} \le t \le +\frac{\pi}{5} \end{cases}$$
$$-1 & \text{if } +\frac{\pi}{5} < t \le +\pi.$$

cycle (or on-time). Obtain only a_n (No need to find b_n and a_0) by treating the waveforms as symmetric. Then, compare the obtained two a_n , one for 50% and the other for 20% of the compoents. Write your answer with supporting reasons. duty cylce, to find which waveform has greater high frequency The two waveforms are similar but different only in their duty

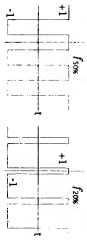


Fig. 2 Rectangular waveform of 50% duty cycle (left) and 20% (right).

4. (20) The distortion factor η indicates how much a given waveform is distorted from the sinusoidal wave of the same frequency. It is defined by using the exponential Fourier series D_n and D_{-n} as follows.

$$\eta = \frac{\text{Total Power} - |D_0|^2 - |D_1|^2 - |D_{-1}|^2}{|D_1|^2 + |D_{-1}|^2}$$

For the half sinusoidal wave shown in Fig. 3, obtain D_0 , D_1 and the total power P, defined by

$$D_0 = \frac{1}{T} \int_T f(t) dt, \ D_1 = \frac{1}{T} \int_T f(t) e^{-j\omega_0 t} dt, \text{ and } P = \frac{1}{T} \int_T f(t)^2 dt.$$

Using the relationship $|D_1| = |D_{-1}|$, calculate the distortion factor η of the half sinusoidal wave.

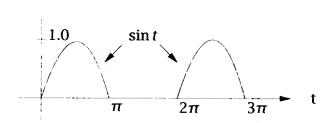


Fig. 3 Half sinusoidal wave.

- 5. (20) Answer the following questions briefly in two or three lines.
 - 1. What does $e^{j\omega_0 t}$ represent? (what is it?)
 - 2. Why do you need negative frequecies to represent a real signal such as $\cos \omega_0 t$ in the frequency domain?
 - 3. Determine the spectrum of $2\cos 2\omega_0 t \sin 2\omega_0 t$.

- The E N D -

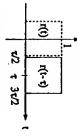
University of Saskatchewan, Electrical Engineering EE 315.3 Signals and Systems (I), Final Examination December 16, 1998

Note: 3 hour open-book exam. All questions are of equal value. Instructor: K. Takaya

- 1. Solve the following Fourier and Inverse Fourier problems.
- 1. A rectangular function r(t) is define as

$$r(t) = \begin{cases} 1 & \text{if } -\frac{7}{2} < t < \frac{7}{2} \\ 0 & \text{othrwise} \end{cases}$$

Obtain the Fourier transform of $\tau(t-\tau)$ and sketch the obtained Fourier transform in two separate graphs, (i) the magnitude versus ω and (ii) the phase versus ω .

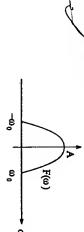


By using the time-shifting property of the Fourier transform,

$$f(t-\tau) \iff F(\omega)e^{-J\omega\tau}$$

obtain the inverse Fourier transform of $e^{-j\omega \tau} \tau \sin(\frac{\omega \tau}{2})$.

2. Determine the Nyquist sampling rate and the Nyquist sampling interval of a signal represented by its Fourier transform $F(\omega)$ as shown below.



 ω_0 corresponds to 1000Hz, i.e. $\omega_0 = 2\pi \times 1000$. Now, the time signal f(t) corresponding to $F(\omega)$ is sampled at a sampling rate exactly equal to twice the Nyquist sampling rate. What are the sampling frequency f_s and the sampling time interval T? Plot the Fourier transform of the sampled signal f(kT), where k is an integer sample number.

3. Find the zero input response of the difference equation,

$$y(k+2) - 0.25y(k) = f(k+2)$$

for a set of internal conditions y[-2] = -4 and y[-1] = -6. The z-transform is not allowed in this problem.

4. Find the z-transform of

$$2^{k+1}u[k-1]+0.5^{k-1}u[k].$$

5. Find the inverse z-transform of

$$\frac{2z^3 - 4z^2 + 5z}{(z-1)(z^2 - 2z + 4)}.$$

Draw a canonical representation of the discrete transfer function given by

$$G[z] = \frac{1 - z^{-1}}{(1 - 0.6z^{-1})(1 - 0.7z^{-1})(1 - 0.8z^{-1})}$$

Also, show the locations of poles and zeros involved in this transfer function G[z] in the complex plane. (pole-zero configuration in the z-plane).

 The spectrum of a periodic wave f(t) having one cycle time interval of T can be expressed by the exponential (two sided) Fourier series coefficients,

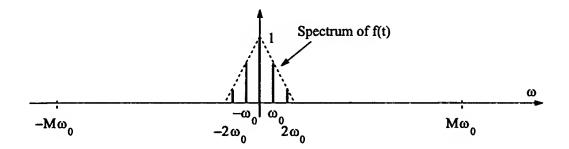
$$D_n = \frac{1}{T} \int_T f(t) e^{-Jn\omega_0 t} dt \text{ and } D_n = D_{-n}^*$$

Where, $\omega_0 = \frac{2\pi}{L}$. Carrier suppressed AM (Amplitaude Modulation) is a simple multiplication process of the baseband signal

f(t) and a carrier signal of frequency $\omega_c = \omega_0 \times M$. The carrier frequency ω_c is much greater than the fundamental frequency ω_0 of the baseband signal. The carrier suppressed AM is given by

$$f_{AM}(t) = 2f(t)\cos\omega_c t$$
.

Express the exponential Fourier series of $f_{AM}(t)$ in terms of D_n and D_{-n} of the original signal f(t). Then, sketch the spectrum of $f_{AM}(t)$ assuming that the spectrum of f(t) is given as illustrated in the following figure.



- The END-

1. Photoelectric Effect

a) Circle any of the following that can be determined by a photoelectric experiment.

The ratio of charge to mass for the electron

The metal's work function

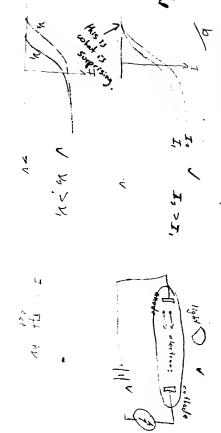
The uncertainty in the position of the electron

The photon's energy ty you set this - so it is already known 7

The value of Planck's constant

The electron's DeBroglie wavelength

- light and two different intensities. Indicate which is the longer wavelength and which is b) Sketch the apparatus and draw typical I-V curves for two different wavelengths of the greater intensity.
- c) Explain what is surprising about the I-V curves from the viewpoint of classical (prequantum) theory.



Susprising that the I. V curve charges for cliff ware brosing According to classical theory, it should only was and on irlors: 1/ X That max kin. energy is independent of intensity

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Department of Electrical Engineering University of Saskatchewan

EE372 Electronic Materials and Devices Professor Robert E. Johanson Midterm Examination



Welcome to the EE372 Midterm. The examination has two parts. Part A consists of questions that test knowledge of basic concepts, and part B requires more involved calculations. Part A is closed book and closed notes. When you finish part A, hand it in textbook (Kasap, any edition) but not to any other material such as notes or other books. (raise your hand) and then proceed to part B. Part B is open book; you may refer to your You may also use a calculator for both parts. The examination lasts 2 hours.

shown. Partial credit will be given for partially correct answers but only if correct simple answer; credit will be given only if the steps leading to the answer are clearly Each problem is weighted equally. Show your work if the question involves more than a intermediate steps are shown.

For part A, answer 4 of the 5 questions.

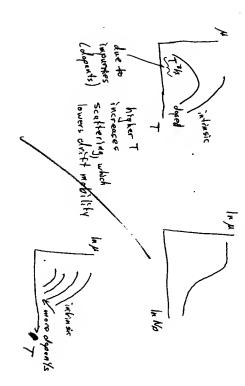
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October 25, 2002

PART A

3. Conduction in Semiconductors

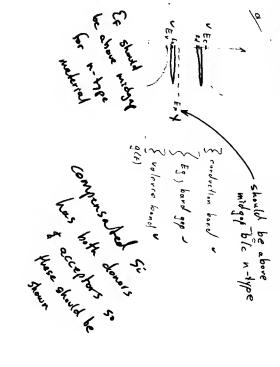
- a) Draw qualitatively the dependence of the drift mobility of a semiconductor on temperature and dopant concentration. Explain why the curves look the way they do.
- b) Explain why a completely full band does not conduct electricity.



always 0

2. Semiconductor Band Structure

a) Draw a qualitative density of states diagram for compensated silicon. Label all relavent energy levels with appropriate symbols, and name the important regions of the density of states. Indicate approximately the position of the Fermi energy if the material is overall n-type.



Lasers

- a) Explain the difference between spontaneous and stimulated emission.
- b) What condition is necessary for optical amplification and how is it achieved? Explain using a typical energy level diagram.
- c) Why is the light from a laser nearly monochromatic? Provide one explanation for why the laser's output has a small spread in wavelength.

Spontaneous emission is coused by an electropleraying from a higher every level (construction notactated) to a lower love / E, (would the quant state), releasing a photon in this process with the E2-E1. In stimulated emission this state change occurs when a photon collides with the atom, causing this energy change and a photon emission.

Necessary condition: Inversion of status - more atoms at a higher energy level those of around state - more atomotes)

- arternool by "purphy" - using a light or electrical method to bump electrone up to metastable states:

enoty 15 destroy or to the start of the star

Light is morachrometic ble of the quantized nature of the electron every levels - when stimulated the alam gives off the same amount of every every time, in the form of a pholon -> Both elements in laser are chosen to produce only one transition

Atoms moving toward the receiver will emit a stabilly in her a slightly in the receiver will emit a stabilly in her a slightly in the receiver and away will in the excited for a specific period away red shift are times reputting in an uncertainty in energy

4. Coulomb Potential

- a) What are the allowed values for each of the quantum numbers n, l, m_l, m_s ?
- b) How many electrons can occupy each of following subshells: 2s, 3p, and 4d?
- c) What would happen to an atom if the Pauli Exclusion Principle did not hold?d) Circle which level of the following pairs has the higher energy.
- 3p) or 3s v 2p or 4p) v
- N=1,2,3,...(n-1) N=0,1,3,...(n-1) N=0,21,27...28 N==±1/2

õ

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b) 25: 2 c 3p: 6 c

40:100

There could be many electrons wlosactly the some set of quantum numbers -> Since they would all try to be at the lowest energy state, you would only have one shell + one subshell for every atom.

Ly No valence e-ts so so bording the.

Ly Tf Hurd's rule still applied, they would all on the same spin -> Very mounting.

1. Semiconductor Statistics

- a) A silicon crystal is uniformly doped with 3×10^{17} cm⁻³ of donors. Calculate the position of the Fermi level with respect to the conduction band edge E_C at T = 300 K.
- b) The above silicon crystal is damaged by radiation. The damage causes new electron energy levels to appear at the center of the band gap with a density of 2×10^{17} cm⁻³ (each new level can contain only one electron). What is the density of electrons in the conduction band now? Calculate the new position of the Fermi level with respect to the conduction band edge E_C .

M= Nd= \$310¹⁷ cm⁻³ >> n;

N= Nd= \$10¹⁷ cm⁻³ >> n;

N= Nd= \$10¹⁷ cm⁻³ >> n;

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Nd= \$10¹⁷ cm⁻³
University of Saskatchewan Department of Electrical Engineering

EE372 Electronic Materials and Devices
Midterm Examination
Professor Robert E. Johanson

PART]



Welcome to the EE372 Midterm. The examination has two parts. Part A consists of questions that test knowledge of basic concepts, and part B requires more involved calculations. Part A is closed book and closed notes. When you finish part A, hand it in (raise your hand) and then proceed to part B. Part B is open book; you may refer to your textbook (Kasap, any edition) but not to any other material such as notes or other books. You may also use a calculator for both parts. The examination lasts 2 hours.

Each problem is weighted equally. Show your work if the question involves more than a simple answer; credit will be given only if the steps leading to the answer are clearly shown. Partial credit will be given for partially correct answers but only if correct intermediate steps are shown.

For part B, answer 3 of the 4 questions.

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PHYSICAL CONSTANTS

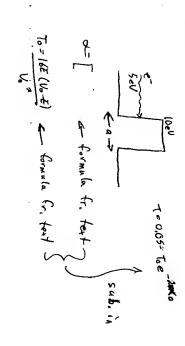
 $c = 2.9979 \times 10^8 \text{ m s}^{-1}$ $e = 1.6021 \times 10^{-19} \text{ C}$ $m_e = 9.1091 \times 10^{-31} \text{ kg}$ $h = 6.62608 \times 10^{-34} \text{ J s}$ $k = 1.3807 \times 10^{-23} \text{ J K}^{-1}$ $\varepsilon_o = 8.8542 \times 10^{-12} \text{ F m}^{-1}$

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October 25, 2002

Quantum Tunneling

of tunneling through the barrier is 0.05? electrons have an energy of 5 eV, how thick must the insulator be so that the probability An insulator in an electronic device presents a potential barrier that is 10 eV high. If the E-AV : He Poth 10+1



Hydrogen Atom

- energy level that the atom's electron can be raised to by the collision. a) An electron with energy 12.5 eV collides with a hydrogen atom. What is the highest
- b) Calculate all possible wavelengths of light that can be emitted by the above excited hydrogen atom as it returns to the ground state.

N = 3.5 -> N= 3 | since n is or integer

4. Photons and Photoelectrons

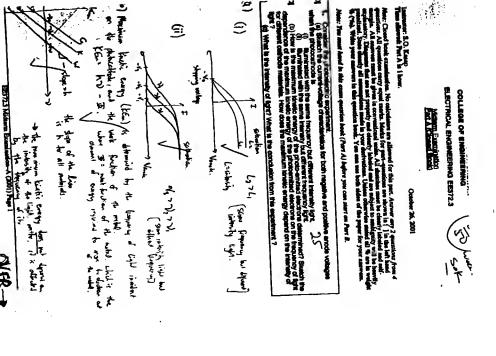
Light with intensity $10 \,\mathrm{mW/cm^2}$ and wavelength 430 nm illuminates a piece of metal with area $5 \,\mathrm{cm^2}$ in a photoelectric experiment. The metal's work function is $1.7 \,\mathrm{eV}$.

- a) Calculate the energy of a photon and the photon flux.
- b) Calculate the current of photoelectrons collected when a large positive bias is applied to the collecting electrode in the photoelectric experiment.
- c) What is the maximum velocity with which a photoelectron leaves the metal.
 d) How much negative voltage needs to be applied to the collecting electrode to eliminate the photocurrent.

I to entinguish the photocurrent,

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1 81.1-50



The intensity of the higher is the number of phytono out some frequency is that pass through a unit over

(andusions from this experiment:

1) Isometium on L

3) KEm is not alkala by the intensity

3) KEm is alkaled by the flagurary.
4) I (work fundion) is a property of the metal.

hight I photons

The BOWN !

values of n, ℓ , m $_{\ell}$ m $_{\rm S}$? Show the ordering of the energy levels for an electron in a many-electron (a) Explain briefly the significance of the quantum numbers n, ℓ , m_ℓ , m_s . What are the allowed

 Ξ

atom from n = 1 to n = 4 level (including n = 4).

Note: 4s is above 3p and below 3d; but 4p is above 3d.

Note: 4s is above 3p and below 3d; but 4p is above 3d.

(b) State the Pauli Exclusion Principle and Hund's rule.

(c) Draw the energy diagrams for the electronic structure of

atomic silicon (atomic number 14) and atomic nitrogen (atomic number 7).

Ensure that your diagrams are clear and that each electron can be assigned its quantum numbers appropriately [Note: You can use a box to represent an orbital wavefunction, $\psi_n \chi_m \ell$. Relative energies of

the boxes must, however, be shown]

Your Last Name

(a) Sketch the energy band diagram of a metal and identify the various significant features in

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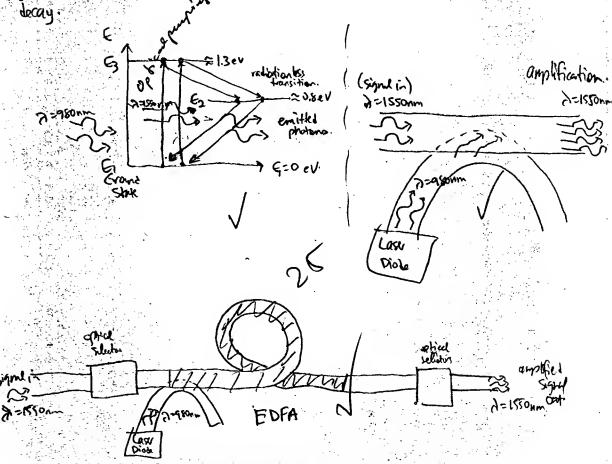
your diagram.
 (b) Sketch the energy band diagram of a metal when a voltage difference is applied across it.
 How does conduction occur? Why are metals conductors.
 How does conduction occur? Why are metals conductor and identify the various significant (c) Sketch the energy band diagram of a semiconductor and identify the various significant features in your diagram. Why are semiconductors insulators at low temperatures? What would happen if a photon of energy h_V > E_ρ is incident on this semiconductor?

First Name

Student N-

[25] 4. Explain with clear diagrams the basic principle of operation of the Er3+ ion doped fiber amplifier. Sketch schematically how this may be used in optical communications.

the E3T ian deped fiber amplifier works on the principle of stimulated emission. For stimulated emission to occur, population inversion has to be present. Population invosion is when there are more olectrons at an energy lead hid is above ground state, than there is not the ground state. Repulation investion is achieved by using a pumping prechanism. In the case of the E0FA; a last died emitting photons (2= 980 nm) acts as the pumping prechanism. The optical 2=980 nm photons excite the electrons at the ground state, causing them to move up to the third energy lovel (E3=1.3 ev), They quickly decay with a realisation last transition to E2 (0.8 ev). This is where the stimulated emission talks place. A photon of wavelength = 1550 nm contains the same energy as the electron on E2 (E3-E,= 0.8 ev), and influences the cladron to return to the ground state (E,=0 ev), when it because it releases a photon that is in phase with the wavelength= 1550 nm photon that caused its docay:



ELECTRICAL ENGINEERING EE372.3

Midterm Examination Part B (Open Book)

Instructor: S.O. Kasap
Time allowed: Part B is 1 hour

Note: Open book examination. Calculators are allowed. Answer any 2 questions from 3 questions. All questions carry equal marks. Marks for part-questions are shown in [] in the left hand margin. All answers must be given in conventional units. State clearly all assumptions made in your derivations. Method of solution must be clearly shown. Numerical mistakes, incorrect, unconventional or missing units will be heavily penalized. Mention the source of materials data used.

answer book. Important: You must hand in Part A before you can start Part B. Write your answers in the university

- [12] 1. a A multialkali metal (e.g. Sb-K-Na/Cs) metal is to be used as the photocathode material in a photocanissive electron tube. It is found that the longest wavelength radiation that gives photocanission is 420 mm. If violet radiation of wavelength 390 nm is incident on to this photocathode, what will be the kinetic energy of the photocanited electrons in electron volts? What is the effective work function of this photocathode materia? What should be the voltage required on the opposite electrode to extinguish the external photocurrent?
- b Suppose that the violet light of wavelength 390 nm has an intensity of 50 mW cm⁻². Suppose that the photocathode is a disk of diameter 4 mm. If the emitted electrons are collected by applying a positive bias of 50 V to the anode, what will be the photoelectric current assuming that the quantum efficiency (η) is 20%. What is the photocurrent when the anode voltage is doubled to 100 V?

Note: Quantum efficiency is defined by

Quantum efficiency = (Number of electrons emitted)/(Number of photons absorbed)

- ত্র Ņ of the excited electron. a A projectile electron with a velocity 2,000 km s⁻¹ collides with a hydrogen atom in a gas discharge e. Find to which n-th energy level the electron in the hydrogen atom gets excited to and the Bohr radius
- Ξ b Calculate the possible wavelengths of radiation (in \tilde{A}) that will be emitted from the excited H-storn in the above example as the electron returns to its ground state.

9 e In a gas discharge tube, He⁺ ions are to be further ionized to He⁺⁺ via impact ionization with electrons accelerated by an applied voltage. Calculate the minimum theoretical voltage required to achieve the

perature is 117 °C A particular He-Ne laser operating at 632.8 nm has a tube that is 50 cm long. The operating

- 3 Estimate the Doppler broadened linewidth (Al) in the output spectrum
- $\overline{\mathbf{z}}$ are therefore allowed? What are the mode number m values that satisfy the resonant cavity condition? How many modes

EE372.3 Midterm Exam-B (2001) Page 1

Reminder: 1/4 = 10-10 mg October 26, 2001

- 3 wavelength O What is the separation Δv_n in the frequencies of the modes? What is the mode separation Δl_n in
- d Show that if during operation, the temperature changes the length of the cavity by \(\delta \text{L}\), the wavelength of a given mode changes by \(\delta \text{L}\),...

3

$$\delta \lambda_{m} = \frac{\lambda_{m}}{2} \delta L$$

Given that typically a glass has a linear expansion coefficient $\alpha = 10^4 \, \text{K}^{-1}$, calculate the change $\delta \lambda_m$ in the output wavelength (due to one particular mode) as the tube warms up from 20 °C to 117 °C, and also per degree change in the operating temperature. Note that $\delta L/L = \alpha \delta T$, and $L' = L(1 + \alpha (T' - T))$. Change in mode wavelength $\delta \lambda_m$ with the change δL in the cavity length L is called *mode sweeping*.

PHYSICAL CONSTAINTS AND USEFUL INFORMATION

 $h = h/(2\pi) = 1.05459 \times 10^{-31} \text{ J s}$ $h = 6.62608 \times 10^{34} \text{ J s}$ $m_s = 9.1091 \times 10^{31} \text{ kg}$ $e = 1.6021 \times 10^{19} \text{ C}$ $c = 2.9979 \times 10^{4} \text{ m s}^{-1}$ $\mu_{\rm s} = 4\pi \times 10^{-7} \, {\rm H \ m^{-1}}$ $E_0 = 8.8542 \times 10^{-12} \text{ F m}^{-1}$ $k = 1.3807 \times 10^{23} \text{ J K}^{-1}$ $N_{A} = 6.0221 \times 10^{23} \text{ mol}^{-1}$

Gas constant, $R = N_1 k = 8.3144 \text{ J K}^{-1} \text{ mol}^{-1} = 0.083144 \text{ L.bar K'mol}^{-1}$ Mass of proton = $1.87495 \times 10^{-27} \text{ kg}$

Mass of hydrogen atom = 1.6736×10^{27} kg

Acceleration due to gravity (at 45° latitude), g =9.81 m s²

STINUTS STINU Electrical capacitance Electrical inductance Electrical resistance Electric current rrequency ressure Electrical conductance enperature DERIVED SI UNITS Magnetic flux density ġ inergy lagnetic flux lectric charge ectric potential difference siemen farad henry joule newton weber tesla ohm kdvin meter kilogram second W=J s'1=kg m' C = As \(\Omega = \kg \text{m}^2 \text{A}^2 \text{s}^3\) \(\S=1/\Omega = \kg \text{m}^2 \kg \text{kg}^1 \text{m}^2\) \(\Fine = \kg \text{m}^2 \text{s}^1 \text{A}^2\) \(\Fine = \kg \text{m}^2 \text{s}^1 \text{A}^2\) \(\Fine = \kg \text{m}^2 \text{s}^1 \text{A}^2\) N = kg m s⁻² $V = N m C^{1} = kg m^{2} s^{3} A^{-1}$ $Hz = s^{-1}$ *> Pa=N m T = Wb m. $V_{S} = kg m^{2} A^{-1} s^{-2}$ $v_{S} = kg m^{2} A^{-1} s^{-2}$ $v_{S} = kg A^{-1} s^{-2}$

EE372.3 Midterm Exam-B (2001) Page 2

ELECTRICAL ENGINEERING EE372.3

Final Examination Part B

Instructor: S.O. Kasap

December 18, 2001

Total time allowed: 3 hours for Parts A and B. Time allowed: Part B is nominally 11/2 hour.

course notes and handouts are allowed. Calculators are allowed. Instructions: Open book examination. Only the course textbook and one three-ring binder containing

Answer any 3 questions from 4 questions. If you answer more than 3 questions, only the first three will be marked. All questions carry equal marks. Marks for a part-question depend on the difficulty of the question, All answers must be given in conventional units. State clearly all assumptions made in your missing units will be heavily penalized. Mention the source of materials data used derivations. Method of solution must be clearly shown. Numerical mistakes, incorrect, unconventional or

Important: You must hand in Part A before you can start Part B. Write your answers in the university answer book.

Note: You may spend more or less time on Part B; but the total exam time is 3 hours

- for P in Si is 0.045 eV below the conduction band edge energy, E An n-type Si sample has been doped with 5×10^{13} phosphorus (P) atoms cm⁻³. The donor energy level

- Calculate the room temperature conductivity of the sample.

 Where is the Fermi level with respect to the intrinsic sample?

 Determine the temperature above which the sample behaves as if intrinsic. Where is the Fermi level
- at this temperature? Fermi level at this temperature? Determine the lowest temperature (°C) above which nearly all the donors are ionized. Where is the
- What is the useful temperature range for a pn junction device such as a diode that uses this n-type
- type with approximately the same conductivity. Calculate the necessary minimum acceptor doping (i.e. N_s) that is required to make this sample p-
- 2. Consider a long pn junction diode with an acceptor doping, N_{r} of 10^{17} cm³ on the p-side and donor concentration of N_{r} on the n-side. The diode is forward biased and has a voltage of 0.6 V across it. The diode cross-sectional area is 1 mm³. The minority carrier recombination time, r_{r} depends on the dopant concentration, N m (cm⁻¹), through the following approximate relation

11 $1+2\times10^{-17}N_{\text{dopper}}$

- a Suppose that $N_s = 10^{15}$ cm⁻³. Then the depletion layer extends essentially into the n-side and we have to consider minority carrier recombination time, τ_{ij} in this region. Calculate the diffusion and recombination contributions to the total diode current. What is your conclusion?

 b. Suppose that $N_i = N_j = 10^{10}$ cm⁻³. Then W extends equally to both sides and, further, $\tau_i = \tau_{ij}$.
- Calculate the diffusion and recombination contributions to the diode current. What is your conclusion?

EE372.3 Final Exam (2001) Page 1

(17) (3.) Consider an idealized prep bipolar transistor with the properties listed below in the table. Assume that the base region has a relatively uniform doping. The emitter and collector donor concentrations are mean values. The cross sectional area is 0.0001 cm² (100 μm × 100 μm). The transistor is biased to operate in the normal active mode. The collector current is 1 mA. The base-collector voltage is 12V

Properties of an pap bipolar transistor

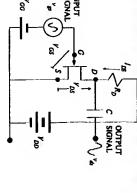
10 µm	Emitter width
1×10 ¹⁴ cm ⁻³	Emitter doping
10 ns	Electron lifetime in emitter
4 µm	Base width
5×10 ¹³ cm ⁻³	Base doping
300 ns	Hole lifetime in base
5×1013 cm-3	Collector doping

- a Calculate the depletion layer width extending from the collector into the base and from the emitter into the base. What is the width, W_{p_i} of the neutral base region?

 b Calculate α and hence β for this transistor assuming that the emitter injection efficiency γ is unity.
- Comment on how these should depend on V_{G} :

 e What is the emitter injection efficiency γ^{0}
- What are the emitter and base currents? What are α and β taking into account the emitter injection efficiency.
- f What is the emitter-base voltage?
 f What are r_u and C_u if this transistor were connected in the CE (common emitter) configuration with the same collector current and the same voltage across the BC junction?
 NOTE: Assume that the emitter current is due to minority carrier diffusion and not recombination in the
- [17] (4.) Consider an *n*-channel JFET which has a pinch-off voltage (V_p) of 3 V an $I_{ON} = 30$ mA. It is used in a common source configuration in which the gate to source bias voltage is V_{OC} and the battery voltage is V_{DO} and suppose that a small signal voltage gain of -20 is needed and you have to keep $V_{DC} = \frac{1}{2}V_{DO}$. Given that you only have $V_{DO} = 30$ V, what should be the bias gate-source voltage V_{CO} , the drain resistance $V_{DC} = \frac{1}{2}V_{CO}$.
- R_D , and the drain current I_D If an ac signal of 3V peak-to-peak is applied to the gate in series with the dc bias voltage, what
- will be the ac output voltage peak-to peak? What is the voltage gain for positive and negative input signals? Sketch the input and output signal waveforms and mark the various voltagve levels?

 What would be the input current and hence the input impedance of the JFET?



EE372.3 Final Exam (2001) Page 2

Student Person

UNIVERSITY OF SASKATCHEWAN COLLEGE OF ENGINEERING

ELECTRICAL ENGINEERING EE317.3



Instructor: S.O. Kasap Time allowed: Part A is I hour.

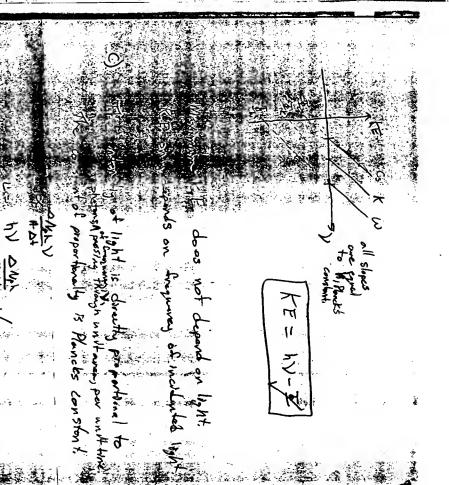
October 24, 2000

Note: Closed book examination. No calculators are allowed for this part. Answer any 2 questions from 4 questions. All questions carry equal marks. Marks for part-questions are shown in [] in the left hand margin. All answers must be given in conventional units. All sketches must be clearly labeled and self-explanatory. Diagrams that are not properly and clearly labeled and are subject to ambiguity will be heavily penalized. State clearly all assumptions made in your derivations. Unless otherwise stated all % are in weight % (%). Write your answers in this question book. You can use both sides of the paper for your answers.

Note: You must hand in this exam question book (Part A) before you can start on Part B.

[10] ত <u></u> ج ا (ii) Illuminated with the same interestly but different frequency light.

(b) How is the maximum kinetic energy of the photo-emitted electrons determined? Sketch the dependence of the maximum kinetic energy of the photoemitted electrons on the frequency of light for different cathode materials. How does the maximum kinetic energy depend on the intensity of when the photocathode is L-light intersit (a) Sketich the current-voltage characteristics for both negative and positive anode voltages Consider the photoelectric experiment. (c) What is the intensity of light? What is the conclusion from this experiment? hoping Vallage 74 now lluminated with the same frequency but different intensity light, Maximum the same of the book of the The second of the continuent of the second o Ļ 7 Š . The state of 12-V-K 3. 2. P.F. gain



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- <u>@</u> 3. (a) Sketch the energy band diagram of a metal and identify the various significant features in
- Œ
- your diagram.

 (b) Sketch the energy band diagram of a metal when a voltage difference is applied across it. How does conduction occur? Why are metals conductors.

 (c) Sketch the energy band diagram of a semiconductor and identify the various significant features in your diagram. Why are semiconductors insulators at low temperatures? What would happen if a photon of energy $h_{\nu} > E_{g}$ is incident on this semiconductor?

Jana .

The Er 3 doped fiker amplifier (EDFA) is based on

the principle of Stamplated emission. For stamplated emission to occur, population inversion is needed Population inversion is a greater number of e- at an energy level higher than ground is a greater number of e- at an energy level higher than ground state. No 7 N1: Population inversion is created by a pumping mechanism. In the case of EDFA is created by a pumping mechanism. In the case of EDFA palas of well-ength 980nm optical excite the e- to an energy of 1.27 eV and 1.54 eV culled E3 and E3, respectably.

These excited E7 are then decays et without radiative emission to E2. These is where stimulated emission occurs. Applicances of 7 = 1550nm, which has an energy Ez-E, influences the e- at the Ez to fall to E1, AMI emitting photons of some of tengths, direction, and in phase with orginal Andrew as 5 town in Fig. 1 below

R=1550m R=1550m Qualité decuy

HAMPARANIN Socilar

This can be used in optical communications
using the follow diagram.

Sphal Mountains and Solder

Synal State State of Solder

7=1550

R=980nn

Cig Z.

ELECTRICAL ENGINEERING EE317.3

Midterm Examination Part B (Open Book)

Instructor: S.O. Kasap
Time allowed: Part B is 1 hour

October 24, 2000

Note: Open book examination. Calculators are allowed. Answer any 2 questions from 3 questions. All questions carry equal marks. Marks for part-questions are shown in [] in the left hand margin. All answers must be given in conventional units. State clearly all assumptions made in your derivations. Method of heavily penalized. Mention the source of materials data used. solution must be clearly shown. Numerical mistakes, incorrect, unconventional or missing units will be

Important: You must hand in Part A before you can start Part B. Write your answers in the university answer book.

- $[12](\mathbf{i}.)$ 1.) a In a photoelectric experiment, it is found that an infrared (IR) radiation of wavelength 8400Å is the longest wavelength radiation which can cause photoemission of electrons from a photocathode made of Sb-K-Na-Cs. If a blue radiation of wavelength 4500Å is incident onto this photocathode, what will be the kinetic energy of the photoemitted electrons in electron volts? What is the voltage required on the anode to extinguish the photocurrent?
- [13] b Suppose that the blue light of wavelength 4500Å has an intensity of 10 mW/cm². Suppose that the photocathode is a disk of diameter 3 mm. Suppose that the incident radiation illuminates the whole photocathode and a large positive voltage is applied to the anode to collect all the photoemitted electrons. Suppose that the quantum efficiency (1) of the photocathode is 20%. What is be the photoelectric current? Quantum efficiency = (Number of electrons emitted)/(Number of photons absorbed)

[Reminder: $1\dot{A} = 10^{-10}$ m]

- <u>ত</u> 2. a /A projectile electron with a velocity 2.5×10^6 m s⁻¹ collides with a hydrogen atom in a gas discharge tube. Find to which n-th energy level the electron in the hydrogen atom gets excited to and the Bohr radius of the excited electron.
- 3 b \Calculate the possible wavelengths of radiation (in Å) that will be emitted from the excited H-atom in the above example as the electron returns to its ground state.

[Reminder: $1A = 10^{-10}$ m]

- <u>ত</u> c $^{\prime}$ In a gas discharge tube, He $^{+}$ ions are to be further ionized to He $^{++}$ via impact ionization with electrons accelerated by an applied voltage. Calculate the minimum theoretical voltage required to achieve the ionization.
- A particular He-Ne laser operating at 632.8 nm has a tube that is 60 cm long. The operating temperature is 127 °C
- Estimate the Doppler broadened linewidth ($\Delta \lambda$) in the output spectrum.
- $\overline{\alpha}$ are therefore allowed? What are the mode number m values that satisfy the resonant cavity condition? How many modes
- 3 What is the separation Δv_{\perp} in the frequencies of the modes? What is the mode separation $\Delta \lambda_{\perp}$ in

EE317.3 Midterm Exam-B (2000) Page

3 wavelength of a given mode changes by &l,, d Show that if during operation, the temperature changes the length of the cavity by &L, the

 $\delta \lambda_m = \frac{\lambda_m}{2} \delta L$

Given that typically a glass has a linear expansion coefficient $\alpha \approx 10^6 \, \mathrm{K}^{-1}$, calculate the change $\delta \lambda_n$ in the output wavelength (due to one particular mode) as the tube warms up from 20 °C to 125 °C, and also per degree change in the operating temperature. Note that $\delta L/L = \alpha \delta T$, and $L' = L[1 + \alpha(T' - T)]$. Change in mode wavelength $\delta \lambda_n$ with the change δL in the cavity length L is called mode sweeping.

EE317.3 Midterm Exam-B (2000) Page 2

ELECTRICAL ENGINEERING EE317.3

Midterm Examination Part A (Closed Book)

Instructor: S.O. Kasap

Time allowed: Part A is 1 hour.

October 30, 1998

Note: Closed book examination. No calculators are allowed for this part. Answer any 2 questions from 4 questions. All questions carry equal marks. Marks for part-questions are shown in [] in the left hand margin. All answers must be given in conventional units. All sketches must be clearly labeled and selfexplanatory. Diagrams that are not properly and clearly labeled and are subject to ambiguity will be heavily penalized. State clearly all assumptions made in your derivations. Unless otherwise stated all % are in weight % (*/o). Write your answers in this question book. You can use both sides of the paper for your

Note: You must hand in this exam question book (Part A) before you can start on Part B.

	1.	Consider the photoelectric experiment.
[10]		(a) Sketch the current-voltage at

- (a) Sketch the current-voltage characteristics for both negative and positive anode voltages when the photocathode is
 - illuminated with the same frequency but different intensity light,
 - illuminated with the same intensity but different frequency light.
- (b) How is the maximum kinetic energy of the photo-emitted electrons determined? [10] Sketch the dependence of the maximum kinetic energy of the photoemitted electrons on the frequency of light for different cathode materials. How does the maximum kinetic energy depend on the intensity of light? LE does not depend on light intensity
- (c) What is the intensity of light? What is the conclusion from this experiment? [5]
 - (a) Explain briefly the significance of the quantum numbers n, ℓ , m_{ℓ} , m_{s} . What are the [7] allowed values of n, ℓ , m $_\ell$, m $_{\rm S}$? Show the ordering of the energy levels for an electron in a many-electron atom from n = 1 to n = 4 level (including n = 4). Note: 4s is above 3p and below 3d; but 4p is above 3d. 5'2p' 555
 - (b) State the Pauli Exclusion Principle and Hund's rule. [4] [14]
 - (c) Draw the energy diagrams for the electronic structure of
 - atomic silicon (atomic number 14) and
 - atomic nitrogen (atomic number 7).

Ensure that your diagrams are clear and that each electron can be assigned its quantum numbers appropriately.

[Note: You can use a box to represent an orbital wavefunction, ψ_{n,ℓ,m_ℓ} . Relative energies of the boxes must, however, be shown]

- 3. (a) Sketch the energy band diagram of a metal and identify the various significant features
- (b) Sketch the energy band diagram of a metal when a voltage difference is applied across it. How does conduction occur?
- (c) Sketch the energy band diagram of a semiconductor and identify the various significant features in your diagram.
- Explain with clear diagrams the basic principle of operation of the Er3+ ion doped fiber amplifier. Sketch schematically how this may be used in optical communications.

ELECTRICAL ENGINEERING EE317.3

Midterm Examination Part B (Open Book)

Instructor: S.O. Kasap
Time allowed: Part B is I hour

October 30, 1998

Note: Open book examination. Calculators are allowed. Answer any 2 questions from 3 questions. All questions carry equal marks. Marks for part-questions are shown in [] in the left hand margin. All answers must be given in conventional units. State clearly all assumptions made in your derivations. Method of solution must be clearly shown. Numerical mistakes, incorrect, unconventional or missing units will be heavily penalized. Mention the source of materials data used.

answer book. Important: You must hand in Part A before you can start Part B. Write your answers in the university

- No be 3.9 cm²V⁻¹s⁻¹ at 27° C. Atomic weight and density of Sn are given as 118.7 and 7.30 g cm⁻³ respectively. From Hall effect measurements, the electron drift mobility in tin (Sn, valency IV) has been determined
- [12] Ċ (a) Assuming that each Sn atom contributes 4 conduction electrons, calculate the resistivity of Sn at 0°
- <u>[3]</u> (b) Consider a thin tin bar of lenght L=2 cm, width W=0.5 cm, depth D=1 mm, carrying a current of 5 mA and placed in a magnetic field of flux density B=0.2 T. The current flows along the length L and the magnetic field is along depth D. The resulting Hall voltage is measured across the width W. What is the Hall voltage? Why is the voltage "small"?
- A multialkali metal metal is to be used as the photocathode material in a photocernissive electron tube.
 The work function of the metal is 1.5 eV. Suppose that blue light of wavelength 450 nm with an intensity
- of 100 mW cm⁻² is incident on the photocathode.
- [13] photoelectric current density assuming that the quantum efficiency (1) is 20%. Note: Quantum efficiency is defined by (a) If the emitted electrons are collected by applying a positive bias to the anode, what will be the

- <u>∓</u>∞ the same photocurrent, assuming that the quantum efficiency is the same. Quantum efficiency = (Number of electrons emitted) / (Number of photons absorbed)
 (b) What should be the voltage and its polarity to extinguish the current?
 (c) What should be the intensity of an incident red light beam of wavelength 700 nm that would give
- (a) Show that the wavelengths of radiation emitted (or absorbed) from a hydrogenic atom obey the equation (Balmer-Rydberg Formula):

[6]

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EE217.3 Final Exam (1997) Page 2

EE317.3 Midterm Exam-B (1998) Page

quantum numbers with $n_2 > n_1$ where R_{∞} is the Rydberg constant and has the value 1.097373×10⁷ m⁻¹, and n_2 and n_1 are principal

- <u>=</u> (b) The light from the sun includes extremely sharp "dark lines" at certain wavelengths superimposed on a bright continuum at all other wavelengths as discovered by Josef von Fraunhofer in 1829. One of lines from the Hydrogen atom spectrum (they are called the H_{α} and H_{β} Fraunhofer lines). Such lines these "dark lines" occurs in the orange range and another in the blue. Fraunhofer measured their wavelengths to be 6563Å and 4861Å, respectively. With the aid of Table Q.3, show that these are specti
- provided us with the first clues to the chemical composition of the sun.

 (c) Radio telescopic studies of B. Höglund and P.G. Mezger (Science, 150, 339, 1965) have detecte a 5009MHz electromagnetic radiation in space. Show that this radiation comes from excited hydrogen atoms as they undergo transitions from n = 110 to 109. What is the size of such an excited hydrogen atom. (in rum)?

Table Q.3
Hydrogen Atom Spectral Series and Rydberg Integers

Lyman Balmer Paschen Brackett Pfund	Series
-444	n _t
2.3.4 3.4.5 4.5.6 5.6.7 6,7.8	n_2
ultraviolet visible infrared infrared infrared	Spectral Region

!

UNIVERSITY OF SASKATCHEWAN COLLEGE OF ENGINEERING

ELECTRICAL ENGINEERING EE317.3

Midterm Examination Part A (Closed Book)



Time allowed: Part A is 1 hour. Instructor: S.O. Kasap

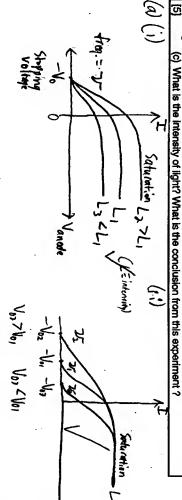
October 25, 1999

Note: Closed book examination. No calculators are allowed for this part. Answer any 2 questions from 4 questions. All questions carry equal marks. Marks for part-questions are shown in [] in the left hand margin. All answers must be given in conventional units. All sketches must be clearly labeled and selfexplanatory. Diagrams that are not properly and clearly labeled and are subject to ambiguity will be heavily penalized. State clearly all assumptions made in your derivations. Unless otherwise stated all % are in weight % ("/o). Write your answers in this question book. You can use both sides of the paper for your answers.

Note: You must hand in this exam question book (Part A) before you can start on Part B.

when the photocathode is (a) Sketch the current-voltage characteristics for both negative and positive anode voltages Consider the photoelectric experiment.

(i) Illuminated with the same frequency but different intensity light,
(ii) Illuminated with the same intensity but different frequency light.
(b) How is the maximum kinetic energy of the photo-emitted electrons determined? Sketch the dependence of the maximum kinetic energy of the photoemitted electrons on the frequency of light for different cathode materials. How does the maximum kinetic energy depend on the intensity of



he max. the work function the work function (The energy determined by ¥ STOCK KMS ant Intensity phoneumade metal. KEm=hr-I metal). max KE. The frequency of incident to remove the electron Only travency de pendent on photoconitted

values of n, ℓ , m_{ℓ} , m_{g} ? Show the ordering of the energy jevels for an electron in a many-ejectron (a) Explain briefly the significance of the quantum numbers n, ℓ , m_{r} , m_{s} . What are the allowed

atom from n = 1 to n = 4 level (Including n = 4).

Note: 4s is above 3p and below 3d; but 4p is above 3d.

(b) State the Paull Exclusion Principle and Hund's rule.

(c) Draw the energy diagrams for the electronic structure of

<u>-</u>atomic silicon (atomic number 14) and atomic nitrogen (atomic number 7).

appropriately. Relative energies of [Note: You can use a box to represent an orbital wavefunction, ψ_{n,ℓ,m_ℓ} . Relative energies of Ensure that your diagrams are clear and that each electron can be assigned its quantum numbers

the boxes must, however, be shown

Your Last Name

at Ex Than E, C population inversion) can be achieved via at Ex Than E, Then stimulated emission will overcome an electron that is excited from energy E, to E, is influen by a photon of energy E, E, the electron will drop to E, and emit a photon of energy E, E, that is in phase with the stimulathy photon. It were electrons (atoms) are [25] 4. Explain with clear diagrams the basic principle of operation of the Er* ion doped fiber amplifier. Sketch achematically how this may be used in optical communications. The Er doped fiber amplifier works via the principle emission. This principle states that when

980m drap to the long-lived the energy are excited to

(for E,3+)

incident light of

signals with the following setup:

ELECTRICAL ENGINEERING EE317.3

Midterm Examination Part B (Open Book)

October 25, 1999

Note: Open book examination. Calculators are allowed. Answer any 2 questions from 3 questions. All questions carry equal marks. Marks for part-questions are shown in [] in the left hand margin. All answers must be given in conventional units. State clearly all assumptions made in your derivations. Method of solution must be clearly shown. Numerical mistakes, incorrect, unconventional or missing units will be Instructor: S.O. Kasap
Time allowed: Part B is I hour

Important: You must hand in Part A before you can start Part B. Write your answers in the university

heavily penalized. Mention the source of materials data used.

- Ξ
- [14] 3 1. Consider the photoelectric experiment.

 (i) Sketch the I-V characteristics for both negative and positive anode voltage when the photoesthode is (ii) Illuminated with the same frequency but different intensity light.

 (ii) Illuminated with the same intensity but different frequency light.

 (iii) Illuminated with the same intensity but different frequency light.

 (iv) Sketch the dependence of the maximum kinetic energy of the photoemitted electrons on the frequency of light for different cathode materials. How does the maximum kinetic energy depend on the intensity of light? What is the conclusion from this experiment?

 (c) A multialkali metal (e.g. Sb-K-Na/Cs) metal is to be used as the photoemistion is photoemission is
- (i) If violet radiation of wavelength 390nm is incident on to this photocathode, what will be the kinetic energy of the photocanitted electrons in electron volts? What should be the voltage required on the opposite electrode to extinguish the external photocurrent? 420mm.
- (ii) Suppose that the violet light of wavelength 390nm has an intensity of 50 mW cm⁻². If the emitted electrons are collected by applying a positive bias to the anode, what will be the photoelectric current density assuming that the quantum efficiency (1) is 20%.

Note: Quantum efficiency is defined by

6

equation (Balmer-Rydberg Formula):

Quantum efficiency = (Number of electrons emitted)/(Number of photons absorbed

(a) Show that the wavelengths of radiation emitted (or absorbed) from a hydrogenic atom obey the

$$\lambda^{-1} = R_{oo} Z^2 [n_1^{-2} - n_2^{-2}] \tag{2.1}$$

quantum numbers with $n_2 > n_1$. where R_{∞} is the Rydberg constant and has the value 1.097373×10^7 m⁻¹, and n_2 and n_1 are principal

(b) The light from the sun includes extremely sharp "dark lines" at certain wavelengths superimposed on a bright continuum at all other wavelengths as discovered by Josef von Fraunhofer in 1829. One of these "dark lines" occurs in the orange range and another in the blue. Fraunhofer measured their wavelengths to

be 6563Å and 4861Å, respectively. With the aid of Table Q.2, show that these are spectral lines from the Hydrogen atom spectrum (they are called the H_{α} and H_{β} Fraunhofer lines). Such lines provided us with the

first clues to the chemical composition of the sun.

2 (c) Radio telescopic studies of B. Höglund and P.G. Mezger (Science, 150, 339, 1965) have detected a 5009MHz electromagnetic radiation in space. Show that this radiation comes from excited hydrogen atoms as they undergo transitions from n = 110 to 109. What is the size of such an excited hydrogen atom (in nm)?

Hydrogen Atom Spectral Series and Rydberg Integers Table Q.2

Lyman Balmer Paschen Brackett Pfund	Scrica
-4848	71
2,3,4, 3,4,5, 4,5,5, 5,6,7, 6,7,8,	<i>n</i> ₂
ultraviolet visible infrared infrared infrared	Spectral Region

temperature is 120 °C A particular He-Ne laser operating at 632.8 nm has a tube that is 50 cm long. The operating

Estimate the Doppler broadened linewidth ($\Delta\lambda$) in the output spectrum.

20 **G**E therefore allowed? What are the mode number m values that satisfy the resonant cavity condition? How many modes are

3 (c) What is the separation Δυ, in the frequencies of the modes? What is the mode separation Δλ, in wavelength.

3 a given mode changes by &... (d) Show that if during operation, the temperature changes the length of the cavity by &, the wavelength of

 $\delta\lambda_m = \frac{\lambda_m}{\lambda} \delta L$

output wavelength (due to one particular mode) as the tube warms up from 20 °C to 130 °C, and also per degree change in the operating temperature. Note that $\delta L/L = \alpha \delta T$, and $L' \approx L[1 + \alpha (T' - T)]$. Change in mode wavelength $\delta \lambda_n$ with the change δL in the cavity length L is called mode sweeping. Given that typically a glass has a linear expansion coefficient $\alpha = 10^6 \,\mathrm{K}^{-1}$, calculate the change $\delta \lambda_{\rm m}$ in the

PHYSICAL CONSTANTS AND USEFUL INFORMATION

 $m_e = 9.1091 \times 10^{-31} \text{ kg}$ $h = 6.62608 \times 10^{-34} \text{ J s}$ $e = 1.6021 \times 10^{-19} \text{ C}$ $c = 2.9979 \times 10^8 \text{ m s}^{-1}$ $h = h/(2\pi) = 1.05459 \times 10^{-31} \text{ J s}$

 $N_A = 6.0221 \times 10^{23} \text{ mol}^{-1}$ $k = 1.3807 \times 10^{-23} \text{ J K}^{-1}$ $\varepsilon_o = 8.8542 \times 10^{-12} \text{ F m}^{-1}$ $\mu_o = 4\pi \times 10^{-7} \,\mathrm{H m^{-1}}$

Mass of hydrogen atom = 1.6736×10^{-27} kg Acceleration due to gravity (at 45° latitude), $g = 9.81 \text{ m s}^{-2}$ Gas constant, $R = N_1 k = 8.3144 \text{ J K}^{-1} \text{ mol}^{-1} = 0.083144 \text{ L.bar K} \cdot \text{mol}^{-1}$ Mass of proton = $1.67495 \times 10^{-27} \text{ kg}$

SLING

Length INITS Electric charge Temperature
DERIVED SI UNITS Electric current coulomb ohm ampere kelvin meter kilogram second

W=J s'=kg m' 2 S.3 $V = N m C^{-1} = kg m^2 s^{-3} A^{-1}$ $Hz = s^{-1}$ $Wb = V s = kg m^{2} A^{-1} s^{-2}$ $T = Wb m^{2} = V s m^{2} = kg A^{-1} s^{-2}$ $\Omega = V/A = kg m^2 A^2 s^3$ S = 1/\Omega $F = A_S V^1 = A^2 S^4 k g^1 m^2$ $H = V S A^1 = k g m^2 S^1 A^2$ $J = k g m^2 S^2 = N m$ s m ga

Force Energy

siemen farad henry joule newton weber tesla pascal

Electric potential difference

Power Pressure

Magnetic flux density Magnetic flux Electrical resistance
Electrical conductance
Electrical capacitance
Electrical inductance

EE317.3 Midterm Exam-B (1998) Page 3

UNIVERSITY OF SASKATCHEWAN COLLEGE OF ENGINEERING

ELECTRICAL ENGINEERING EE317.3 Midtern Examination
Part B

Time allowed: Part B is nominally 11/2 hour. Instructor: S.O. Kasap

December 20, 1999

Total time allowed: 3 hours for Parts Å and B.

Note: Open book examination. Only the course textbook is allowed; no other material is permitted.

Calculators are allowed. Answer any 3 questions from 4 questions. If you answer more than 3 questions, only the first three will be marked. All questions carry equal marks. Marks for a part-question depend on the difficulty of the question. Marks for part-questions are shown in [] in the left hand margin. All answers must be given in conventional units. State clearly all assumptions made in your derivations. Method of solution must be clearly shown. Numerical mistakes, incorrect, unconventional or missing units will be heavily penalized. Mention the source of materials data used.

answer book. Important: You must hand in Part A before you can start Part B. Write your answers in the university

 Ξ (1) (a) Consider the metals in Table Q1 from groups I, II and III in the Periodic Table. Calculate the Fermi energies at absolute zero and at room temperature (300 K), and compare the values with the experimental values. What is your conclusion?

Metal	Group	M (g/mol)	Density (g cm²)	E_F (eV) [Calculated]	E _F (eV) Experiment
5	1	63.55	8.96		6.5
2	Ħ	65.38	7.14	•	11.0
≥	B	27	2.70	•	= .8·

<u>=</u> (b) Aluminum is a Valency III metal with the Fermi energy E_r in Table Q.1. Given its resistivity at room temperature (See Table in Textbook), the atomic concentration of aluminum (from its density) and the valency (III) find the mean free path and the drift mobility of conduction electrons. State your assumptions in your derivations and calculations.

2)
An n-type Si sample has been doped with 10" arsenic (P) atoms cm³. The donor energy level for P in Si is 0.045 eV below the conduction band edge energy.

(a) Calculate the room temperature conductivity of the sample.

Estimate the temperature above which the sample behaves as if intrinsic.

Estimate the lowest temperature (°C) above which nearly all (most) of the donors are ionized.

ලලලා What is the useful temperature range for a Hall effect device that uses this n-type semiconductor to

measure a magnetic field; calibration should not change with the temperature.

(e) Calculate the necessary acceptor doping that is required to make this sample p-type with approximately the same conductivity. Note: You may have to use interpolation.

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3. (a) GaAs has an effective density of states at the conduction conduction band (CB) N_c of 4.7×10¹⁷ cm³ and an effective density of states at the valence band (VB) edge N_c of 7×10¹⁸ cm³. Given its bandgap E_c of 1.42 eV calculate the intrinsic concentration and the intrinsic resistivity at room temperature (take as 300 K). Where is the Fermi level? Assuming that N_c and N_c scale as T²⁴, what would be the intrinsic concentration at 100 °C? If this GaAs crystal is doped with 10¹⁸ donors cm³ (such as Te), where is the new Fermi level and what is the resistivity of the sample? The drift mobilities in GaAs are shown in Table Q.3.

Table Q.3: Dopant impurities scatter carriers and reduce the drift mobility (μ_{ϵ} for electrons and μ_h for holes).

Dopant concentration (cm ⁻³)	٥	1015	1016	1017	1014
μ, (cm² V-1 s-1)	8500	8000	7000	5000	2400
$\mu_{*} (cm^{2} V^{-1} s^{-1})$	400	380	310	250	160

[10] (b) State your assumptions in the following calculations:

(i) Calculate the thermal velocity of the conduction band electrons in GaAs (relevant effective mass is that for transport). Is this greater or smaller than the mean speed of the conduction electrons in a metal? Why is their such a big difference?

(ii) Calculate the mean free time and mean free path between electron scattering events (between electrons and lattice vibrations).

(iii) Calculate the drift velocity of the CB electrons in an applied field E of 10^5 V m 4 . What is the ratio of thermal velocity to drift velocity? What is your conclusion?

4. Consider a long pn junction diode with an acceptor doping, N_e , of 10^{18} cm³ on the p-side and donor concentration of N_d on the n-side. The diode is forward biased and has a voltage of 0.6 V across it. The diode cross-sectional area is 1 mm². The minority carrier recombination time, τ , depends on the dopant concentration, N_{dopant} (cm³), through the following approximate relation 5×10^{-7}

 $\tau = \frac{3}{(1+2\times10^{-17}N_{\text{dopunt}})}$

[8] (a) Suppose that $N_s = 10^{15}$ cm³. Then the depletion layer extends essentially into the *n*-side and we have to consider minority carrier recombination time, τ_n in this region. Calculate the diffusion and recombination contributions to the total diode current gievn that when $N_s = 10^{18}$ cm⁻³, $\mu_s \approx 250$ cm⁻² V⁻¹ s⁻¹, and when $N_s = 10^{18}$ cm⁻³, $\mu_s \approx 450$ cm⁻² V⁻¹ s⁻¹. What is your conclusion?

[9] (b) Suppose that $N_d = N_d$. Then W extends equally to both sides and, further, $\tau_c = \tau_c$. Calculate the diffusion and recombination contributions to the diode current given that when $N_d = 10^{16}$ cm³, $\mu_c \approx 250$ cm² V¹ s¹, and when $N_d = 10^{16}$ cm³, $\mu_b \approx 130$ cm² V¹ s¹. What is your conclusion? State all your assumptions.

Gas constant, $R = N_s k = 8.3144 \text{ J K}^{-1} \text{ mol}^{-1} = 0.083144 \text{ L.bar K' mol}^{-1}$ Mass of proton = $1.67495 \times 10^{-27} \text{ kg}$ $h = 6.62608 \times 10^{-34} \text{ J/s}$ $m_e = 9.1091 \times 10^{-31} \text{ kg}$ PHYSICAL CONSTANTS AND USEFUL INFORMATION $c = 2.9979 \times 10^8 \text{ m s}^4$ STINITIS $\hbar = h/(2\pi) = 1.05459 \times 10^{-31} \text{ J s}$ $e = 1.6021 \times 10^{-19} \text{ C}$ UNITS Acceleration due to gravity (at 45° latitude), $g = 9.81 \text{ m s}^{-2}$ Mass of hydrogen atom = 1.6736×10^{-27} kg Energy Frequency Electric potential difference Pressure Magnetic flux density Magnetic flux Electrical inductance Electrical capacitance Electrical conductance Temperature
DERIVED SI UNITS Electric current ectrical resistance pascal kilogram second newton S E henry coulomb $N_A = 6.0221 \times 10^{23} \text{ mol}^{-1}$ $k = 1.3807 \times 10^{-23} \text{ J K}^{-1}$ $\varepsilon_o = 8.8542 \times 10^{-12} \text{ F m}^{-1}$ $\mu_o = 4\pi \times 10^{-7} \text{ H m}^{-1}$ Wb = $V s = kg m^2 A^{-1} s^2$ $T = Wb m^2 = V s m^2 = kg A^{-1} s^2$ $Pa = N m^2$ $F = A_s V^1 = A^2 s^4 kg^1 m^2$ $H = V_s A^1 = kg m^2 s^1 A^2$ $J = kg m^2 s^2 = N m$ $S = 1/\Omega$ W=J s^{1} =kg $m^{2} s^{3}$ V=N m C^{1} = kg $m^{2} s^{3}$ A¹ $\Omega = V/A = kg m^2 A^2 s^3$ C # As $N = kg m s^2$ Hz = s'

SOME CONVERSION FACTORS

ENERGY

1 kJ mole⁻¹ = 0.2389 kcal mol⁻¹ = 0.010363 eV atom⁻¹
1 kcal mole⁻¹ = 4.1840 kJ mol⁻¹ = 0.043360 eV atom⁻¹
1 eV atom⁻¹ = 96.490 kJ mol⁻¹ = 23.062 kcal mol⁻¹
1 ft lb = 1.356 J
1 BTU = 1055 J
1 erg = 10⁻⁷ J
1 kWh = 3.600 × 10⁶ J

PHYSICAL CONSTANTS AND USEFUL INFORMATION

 $h = 6.6256 \times 10^{-34} \text{ J.s}$ m_e = 9.1091 x 10⁻³¹ kg e = 1.6021 x 10⁻¹⁹ C c=2.9979 x 108 m.s⁻¹ Eo = 8.8544 x 10⁻¹² F.m⁻¹ $k = 1.3805 \times 10^{-23} \text{ J.K-1}$ $\mu_0 = 4\pi \times 10^{-7} \text{ H.m}^{-1}$ NA = 6.0220 x 10²³ mol-1

 $h = h/2\pi = 1.05459 \times 10^{-31} \text{ J.s}$

Bohr Magneton = $\beta = 9.2741 \times 10^{-24} \text{ J.T}^{-1}$ Accelaration due to gravity (at 45° latitude), g=9.81 m.s-2 Franck-Wiedemann-Lorentz coefficient = 2.32x10-8 W.Q.K-2 Bohr radius a_o = 52.918 pm Mass of hydrogen atom ~ 1.66×10⁻²⁷ kg Mass of proton = 1.67495x10-27 kg Rydberg constant, R₂₀=1.0974x10⁷ m⁻¹; R₃₀=3.2880x10¹⁵ s⁻¹ Gas constant, R = NAk = 8.3144 J.K-1.mol-1 = 0.083144 L.bar.K-1.mol-1

Energy STINUTS MATERIALS DATA Frequency Electric potential difference Electric charge Force Time Mass Length Pressure Electric current DERIVED UNITS Temperature Mn in Au metrbo Cu in Au metrix Zn in Cu matrix Sn in Cu matrix Ni in Cu metrix Mn in Cu metro Au in Cu metro (Element in matrix) Solute in Solvent Table of Nordheim Coefficient (at 20°C) for Dilute Alloya Š meter m kilogram second pascal empere kelvin K hertz oule newton coulomb 450 2410 300 2900 5500 2900 1250 70.m. 790 Nordheim Coefficient V = N.m.C⁻¹ = kg.m².s⁻³.A⁻¹ $Hz = 8^{-1}$ J = kg.m².s⁻²= N.m C = A s Pa=N.m-2 N = kg.m.s-2 30 26 00 100 24 Maximum Solubility at 25°C

EE317.3 Midterm Examination 1997

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Sn in Au matrix Ni in Au metrix

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Zn in Au matrix

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NOTES

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7 = 9Hue = X
α = enμ<sub>e</sub> + epμ<sub>h</sub>
                        σ = enμ<sub>d</sub> = e<sup>2</sup>nπ
                                                                                                                                                                                                                                                                                                   n_v(v)=4\pi N(m/2\pi kT)^{3/2}v^2 \exp(-mv^2/2kT)
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                                                                                                                  Vot = Fot Fx
                                                                                                                                           Vox = erEx/me
                                                                                                                                                                                                                                                                         n_E(E)=2\pi N(\pi kT)^{-3/2}E^{1/2}\exp(-E/kT)
                                                                                                                                                                                                                                                                                                                                 C<sub>V</sub>=[∂U/∂T]<sub>V</sub>=3R=25J.K<sup>-1</sup>.mole<sup>-1</sup>
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\frac{1}{2}m \ \nabla^2 = \frac{3}{2}k \ T
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GENERAL PHYSICS
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σ = enμ<sub>e</sub> + epμ<sub>h</sub>
                          σ = enμ<sub>d</sub> = e2m
                                                                                                                 Vax = Hd Ex
                                                                                                                                        Vox = erEx/m.
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\frac{1}{2}m \sqrt{2}=\frac{2}{2}k T
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GENERAL PHYSICS
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 $t = \frac{1}{SuN_{e}}$ $1/\tau = 1/\tau_{f} + 1/\tau_{f}$ $1/\mu_{d} = 1/\mu_{L} + 1/\mu_{f}$

α₀ = δρ

 $\rho = \rho_T + \rho_B$

 $\rho = \rho_0 [1 + \alpha_0 (T-T_0)]$

 $\rho_{\rm I} = C \times (1-X)$

 $\rho = \rho_{\text{metrix}} + \text{CX}(1-\text{X})$ $R_{\text{eff}} = L_{\alpha}\rho_{\alpha}/A + L_{\beta}\rho_{\beta}/A$

 $\rho_{\phi ff} = \chi_{\alpha} \rho_{\alpha} + \chi_{\beta} \rho_{\beta}$ $\sigma_{\phi ff} = \chi_{\alpha} \sigma_{\alpha} + \chi_{\beta} \sigma_{\beta}$

 $\rho_{\text{eff}} = \rho_{\text{c}} (1 + \frac{1}{2} \chi_{\text{d}}) / (1 - \chi_{\text{d}})$

 $\rho_{eff} = \rho_{c} (1-\chi_{d}) / (1+2\chi_{d})$

 $I_{ac} = \rho/A = \rho/(2\pi a\delta)$ $F = QV \times B$ $F_{H} = \frac{E_{y}}{J_{x} B_{z}}$ $F_{H} = -\frac{\delta Q}{\delta n}$ $Q = \frac{\delta Q}{\delta x} = -Ax\frac{\delta I}{\delta x}$ $I = -A\sigma(\delta V/\delta x)$ $t = \frac{1}{SuN_0}$ $1/t = 1/t_T + 1/t_1$ $1/\mu_d = 1/\mu_L + 1/\mu_1$ $\delta = \frac{1}{\sqrt{\frac{1}{2}\omega\sigma\mu}}$ $\alpha_0 = \frac{\delta \rho}{\rho_0 \delta T}$ $\rho = \rho_T + \rho_R$ Tph = ANph $I = \Gamma_{\rm ph} h_0$ QUANTUM PHYSICS $\sigma_{\phi ff} = \chi_{\alpha} \sigma_{\alpha} + \chi_{\beta} \sigma_{\beta}$ $\rho = \rho_{matrix} + CX(1-X)$ $\rho_{\rm I}$ = C X (1-X) $\rho = \rho_0 [1 + \alpha_0 (T-T_0)]$ p=h/\lambda p=\hk $\rho_{\text{eff}} = \rho_{\text{c}} (1 - \chi_{\text{d}}) / (1 + 2\chi_{\text{d}})$ $\rho_{\text{eff}} = \chi_{\alpha}\rho_{\alpha} + \chi_{\beta}\rho_{\beta}$ $R_{eff} = L_{\alpha}\rho_{\alpha}/A + L_{\beta}\rho_{\beta}/A$ $\Psi(x,t) = \psi(x) \exp(-\frac{jEt}{\hbar})$ $\frac{K}{\sigma T} = C_{WFL} = 2.45 \times 10^{-8} \text{ W.}\Omega.\text{K}^{-2}$ $\rho_{\text{eff}} = \rho_{\text{c}} (1 + \frac{1}{2} \chi_{\text{d}}) / (1 - \chi_{\text{d}})$

ρ=ħ/λ p=λk $\Psi(x,t) = \psi(x) \exp(-\frac{\int Et}{h})$ /= [phho AAT չ<u>=</u> ኢ

OUANTUM PHYSICS

 $\frac{K}{\sigma T} = C_{WPL} = 2.45 \times 10^{-8} \text{ W.O.K}^{-2}$

 $R_{H} = \sum_{i,j} E_{ij}$ $R_{H} = -\sum_{i,j} A_{ij}$ $Q_{ij} = \sum_{i,j} A_{ij} A_{ij}$ $Q_{ij} = A$

 $\delta = \frac{1}{\sqrt{\frac{1}{2}\omega\sigma\mu}}$ $\Gamma_{ac} = \rho/A = \rho/(2\pi a\delta)$ $F = QV \times B$

 $\frac{d^{2}\psi}{dx^{2}} + \frac{2m}{\hbar^{2}} [E-V] \psi = 0$

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T = \frac{1}{1 + D \sinh^2(\alpha a)}
D = \frac{V_0^2}{4E(V_0 - E)}
T = T_0 \exp(-2\alpha a)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           \alpha^2 = \frac{2m(V_0 - E)}{\hbar^2}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            k^2 = \frac{2mE}{r^2}
                                                                                                                                                                                                                                                                                                    r_{\text{max}} = \frac{n^2 \mathbf{e}_0}{Z}; \mathbf{e}_0 = \text{Bohr radius}

L = \hbar \sqrt{\ell \ell (\ell+1)} L_z = m_\ell \hbar
                                                                                                                                                                                                                                                                                                                                                                                                                                           \mathsf{P}_{\mathsf{n},\ell}(r)\delta r = \mathsf{IR}_{\mathsf{n},\ell}(r)\mathsf{I}^2r^2\delta r
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         V(r) = -Ze^2 / 4\pi \epsilon_0 r
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             E_{n_1 n_2 n_3} = h^2 (n_1^2 + n_2^2 + n_3^2) / 8ma^2 = h^2 N^2 / 8ma^2
                                                                                  MODERN THEORY OF SOLIDS AND SEMICONDUCTORS N_1/N_2 = \exp[-(E_1 - E_2)/kT]
                                                                                                                                                                                   S= h \[s(s+1)] = (h \sqrt{3})/2
                                                                                                                                                                                                                                \Delta \ell = \pm 1 and \Delta m_{\ell} = 0, \pm 1.
                                                                                                                                                                                                                                                                                                                                                                                                   E_n = -me^4 Z^2/8\epsilon_0^2 h^2 n^2 = E_n = -Z^2 E_1/n^2 = -Z^2(13.58eV)/n^2
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        \psi(r,\theta,\phi) = \psi_{n,\zeta m_{\ell}}(r,\theta,\phi) = \mathsf{H}_{n,\ell}(r)\mathsf{Y}_{l,m_{\ell}}(\theta,\phi)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            ∆x∆p≥h and
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 E_n = \hbar^2 \pi^2 n^2 / 2 ma^2 = h^2 n^2 / 8 ma^2
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            18E(V<sub>0</sub>-E)
1 + exp(<del>E-EF</del>)
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D = \frac{V_0^2}{4E(V_0 - E)}T = T_0 \exp(-2\alpha a)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         \alpha^2 = \frac{2m(V_0 - E)}{h^2}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 S = 1 1(s(s+1)] = (1 13) /2
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              N_1/N_2 = exp[-(E_1-E_2)/kT]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                S_z = m_s h
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         \Delta \ell = \pm 1 and \Delta m_{\ell} = 0, \pm 1.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  \Gamma_{\text{max}} = \frac{P^2 \mathbf{a}_0}{Z}; \mathbf{a}_0 = \text{Bohr radius}

\Gamma_{\text{max}} = \frac{P^2 \mathbf{a}_0}{Z}; \Gamma_{\text{max}} = \frac{P^2 \mathbf{a}_0}{Z}; \Gamma_{\text{max}} = \frac{P^2 \mathbf{a}_0}{Z}; \Gamma_{\text{max}} = \frac{P^2 \mathbf{a}_0}{Z}; \Gamma_{\text{max}} = \frac{P^2 \mathbf{a}_0}{Z}; \Gamma_{\text{max}} = \frac{P^2 \mathbf{a}_0}{Z}; \Gamma_{\text{max}} = \frac{P^2 \mathbf{a}_0}{Z}; \Gamma_{\text{max}} = \frac{P^2 \mathbf{a}_0}{Z}; \Gamma_{\text{max}} = \frac{P^2 \mathbf{a}_0}{Z}; \Gamma_{\text{max}} = \frac{P^2 \mathbf{a}_0}{Z}; \Gamma_{\text{max}} = \frac{P^2 \mathbf{a}_0}{Z}; \Gamma_{\text{max}} = \frac{P^2 \mathbf{a}_0}{Z}; \Gamma_{\text{max}} = \frac{P^2 \mathbf{a}_0}{Z}; \Gamma_{\text{max}} = \frac{P^2 \mathbf{a}_0}{Z}; \Gamma_{\text{max}} = \frac{P^2 \mathbf{a}_0}{Z}; \Gamma_{\text{max}} = \frac{P^2 \mathbf{a}_0}{Z}; \Gamma_{\text{max}} = \frac{P^2 \mathbf{a}_0}{Z}; \Gamma_{\text{max}} = \frac{P^2 \mathbf{a}_0}{Z}; \Gamma_{\text{max}} = \frac{P^2 \mathbf{a}_0}{Z}; \Gamma_{\text{max}} = \frac{P^2 \mathbf{a}_0}{Z}; \Gamma_{\text{max}} = \frac{P^2 \mathbf{a}_0}{Z}; \Gamma_{\text{max}} = \frac{P^2 \mathbf{a}_0}{Z}; \Gamma_{\text{max}} = \frac{P^2 \mathbf{a}_0}{Z}; \Gamma_{\text{max}} = \frac{P^2 \mathbf{a}_0}{Z}; \Gamma_{\text{max}} = \frac{P^2 \mathbf{a}_0}{Z}; \Gamma_{\text{max}} = \frac{P^2 \mathbf{a}_0}{Z}; \Gamma_{\text{max}} = \frac{P^2 \mathbf{a}_0}{Z}; \Gamma_{\text{max}} = \frac{P^2 \mathbf{a}_0}{Z}; \Gamma_{\text{max}} = \frac{P^2 \mathbf{a}_0}{Z}; \Gamma_{\text{max}} = \frac{P^2 \mathbf{a}_0}{Z}; \Gamma_{\text{max}} = \frac{P^2 \mathbf{a}_0}{Z}; \Gamma_{\text{max}} = \frac{P^2 \mathbf{a}_0}{Z}; \Gamma_{\text{max}} = \frac{P^2 \mathbf{a}_0}{Z}; \Gamma_{\text{max}} = \frac{P^2 \mathbf{a}_0}{Z}; \Gamma_{\text{max}} = \frac{P^2 \mathbf{a}_0}{Z}; \Gamma_{\text{max}} = \frac{P^2 \mathbf{a}_0}{Z}; \Gamma_{\text{max}} = \frac{P^2 \mathbf{a}_0}{Z}; \Gamma_{\text{max}} = \frac{P^2 \mathbf{a}_0}{Z}; \Gamma_{\text{max}} = \frac{P^2 \mathbf{a}_0}{Z}; \Gamma_{\text{max}} = \frac{P^2 \mathbf{a}_0}{Z}; \Gamma_{\text{max}} = \frac{P^2 \mathbf{a}_0}{Z}; \Gamma_{\text{max}} = \frac{P^2 \mathbf{a}_0}{Z}; \Gamma_{\text{max}} = \frac{P^2 \mathbf{a}_0}{Z}; \Gamma_{\text{max}} = \frac{P^2 \mathbf{a}_0}{Z}; \Gamma_{\text{max}} = \frac{P^2 \mathbf{a}_0}{Z}; \Gamma_{\text{max}} = \frac{P^2 \mathbf{a}_0}{Z}; \Gamma_{\text{max}} = \frac{P^2 \mathbf{a}_0}{Z}; \Gamma_{\text{max}} = \frac{P^2 \mathbf{a}_0}{Z}; \Gamma_{\text{max}} = \frac{P^2 \mathbf{a}_0}{Z}; \Gamma_{\text{max}} = \frac{P^2 \mathbf{a}_0}{Z}; \Gamma_{\text{max}} = \frac{P^2 \mathbf{a}_0}{Z}; \Gamma_{\text{max}} = \frac{P^2 \mathbf{a}_0}{Z}; \Gamma_{\text{max}} = \frac{P^2 \mathbf{a}_0}{Z}; \Gamma_{\text{max}} = \frac{P^2 \mathbf{a}_0}{Z}; \Gamma_{\text{max}} = \frac{P^2 \mathbf{a}_0}{Z}; \Gamma_{\text{max}} = \frac{P^2 \mathbf{a}_0}{Z}; \Gamma_{\text{max}} = \frac{P^2 \mathbf{a}_0}{Z}; \Gamma_{\text{max}} = \frac{P^2 \mathbf{a}_0}{Z}; \Gamma_{\text{max}} = \frac{P^2 \mathbf{a}_0}{Z}; \Gamma_{\text{max}} = \frac{P^2 \mathbf{a}_0}{Z}; \Gamma_{\text
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                E_n = -me^4Z^2/8\epsilon_0^2h^2n^2 E_n = -Z^2E_1/n^2 = -Z^2(13.58eV)/n^2
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       P_{n,\ell}(r)\delta r = iR_{n,\ell}(r)i^2r^2\delta r
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            E_{n_1 n_2 n_3} = h^2 (n_1^2 + n_2^2 + n_3^2) / 8ma^2 = h^2 N^2 / 8ma^2
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 k<sup>2</sup> = 2mE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               MODERN THEORY OF SOLIDS AND SEMICONDUCTORS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         To= -
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             \psi(r,\theta,\phi) = \psi_{n,\ell m}(r,\theta,\phi) = \mathsf{R}_{n,\ell}(r)\mathsf{Y}_{l,m}(\theta,\phi)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            V(r) = -Ze^2 / 4\pi \epsilon_0 r
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            ∆x∆p≥h and
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     E_n = \hbar^2 \pi^2 n^2 / 2 ma^2 = h^2 n^2 / 8 ma^2
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            \frac{d^2\psi}{dx^2} + \frac{2m}{\hbar^2} [E-V] \psi = 0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 1+Dsinh²(αa)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             18E(V0-E)
m 3 23 23
                                                                                                                                                                                                                                                               1+ exp(E-EF)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   \Delta E \Delta t \ge h
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S = 20EF0 ₩. S=8 ΔΠphoto=ΔPphoto $d\Delta p/dt = G_{ph} - \Delta p/\tau_h$ $n=(N_cN_d)^{1/2}\exp[-(E_c-E_d)/2kT]$ p=Nvexp[-(EF-Ev)/kT] n=Ncexp[-(Ec-EF)/kT] Vo=(kT/e) fr(ppo/pno) $\Delta p_n(x) = \Delta p_n(0) \exp(-x/L_h)$ $p_n(0) = p_{no} \exp(-y/kT)$ J_=enµ_E + eD_dn/dx $d\Delta n/dt = G_{ph} - \Delta n/\tau_{\bullet}$ $n_i=(N_cN_v)^{1/2}\exp(-E_g/2kT)$ N_V=2[2πmh*kT/h²]3/2 N_C=2[2\pim_*kT/h²]3/2 noPno=npoPpo=ni2 $V_0 = (kT/e) ln(n_{no}/n_{po})$ J=[(@D_h/L_hN_d) + (@D_d/L_eN_e)]n;²[exp(eV/kT)-1] ; APn=Pn-Pno __√(D.₹.) L_h=√(D_hτ_h) $D_h/\mu_h=D_e/\mu_e=kT/e$ $J_h = ep_{\mu_h}E - eD_hdp/dx$ Set

PHYSICAL CONSTANTS AND USEFUL INFORMATION

 $c = 2.9979 \times 10^8 \text{ m s}^{-1}$ $N_A = 6.0221 \times 10^{23} \text{ mol}^{-1}$ $e = 1.6021 \times 10^{19} \text{ C}$ $k = 1.3807 \times 10^{23} \text{ J K}^{-1}$ $m_r = 9.1091 \times 10^{-31} \text{ kg}$ $h = 6.62608 \times 10^{-34} \text{ J s}$ $h = 6.62608 \times 10^{-34} \text{ J s}$ $\mu_o = 4\pi \times 10^{-7} \text{ H m}^{-1}$ $h = h/(2\pi) = 1.05459 \times 10^{-31} \text{ J s}$

Gas constant, $R = N_A k = 8.3144 \text{ J K}^{-1} \text{ moi}^{-1} = 0.083144 \text{ L.bar K}^{-1} \text{ moi}^{-1}$ Mass of proton = $1.67495 \times 10^{-27} \text{ kg}$

Mass of hydrogen atom = 1.6736×10^{27} kg Acceleration due to gravity (at 45° latitude), g = 9.81 m s⁻²

UNITS SI UNITS Length Temperature
DERIVED SI UNITS
Electric charge Electric current Magnetic flux Magnetic flux density Energy Electrical capacitance Electrical inductance Electrical conductance Electrical resistance Electric potential difference meter kilogram second coulomb siemen henry
joule
newton
weber
tesla
pascal
watt
volt
hertz C = A s $\Omega = V/A = kg m^2 A^2 s^3$ $S = 1/\Omega$ N = kg m s.* Wb = V s = kg m² A ¹ s.² T = Wb m² = V s m² = kg A¹ s.² F= A 5 V | = A² 5⁴ kg | m² H = V 8 A | = kg m² 5 | A² J = kg m² 5² = N m W=J s'=kg m² s³ A¹

1

nno=Nd, Ppo=Na